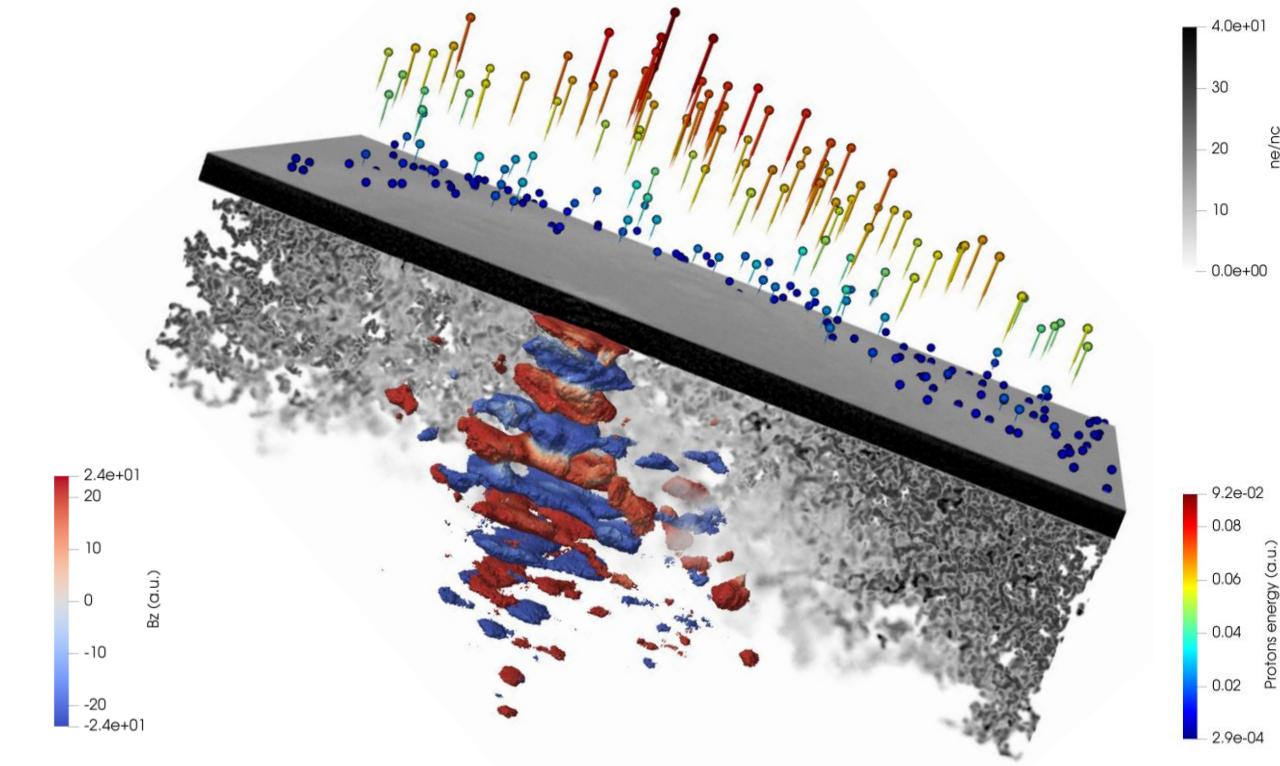




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Department of Energy

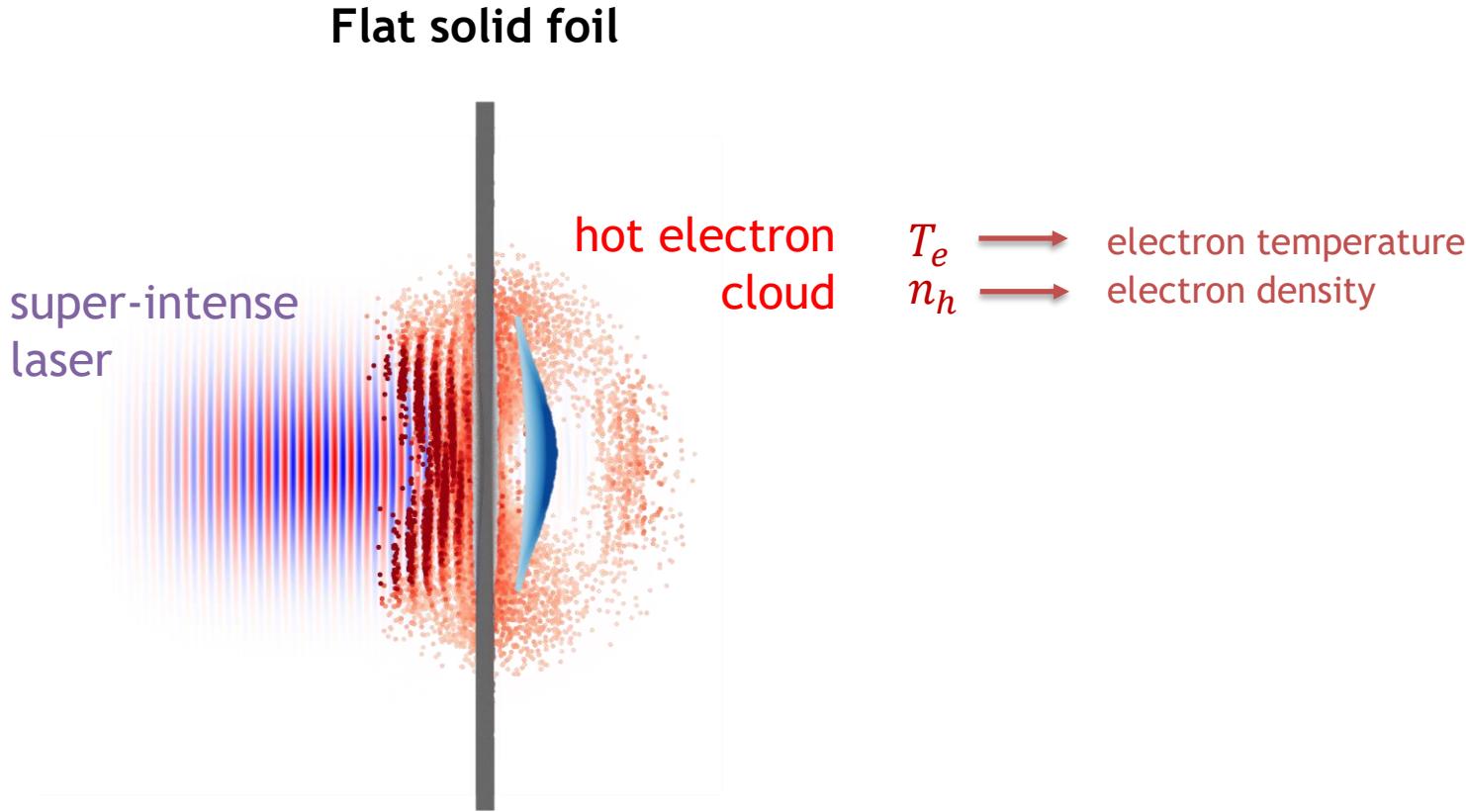


# A theoretical model of laser-driven ion acceleration from near-critical double-layer targets

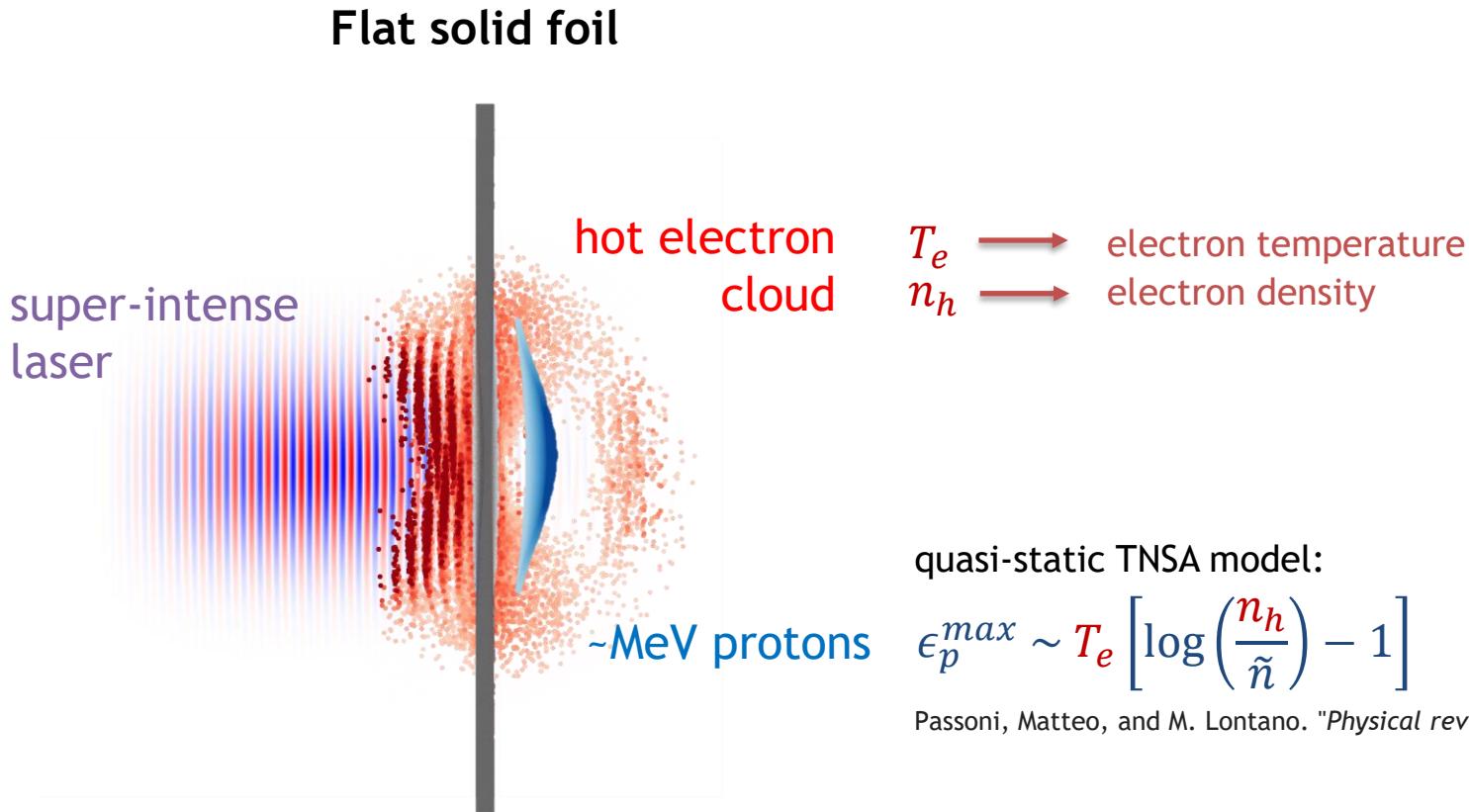
Andrea Pazzaglia, Luca Fedeli, Arianna Formenti, Alessandro Maffini, Matteo Passoni

*Department of Energy, Politecnico di Milano, Italy*

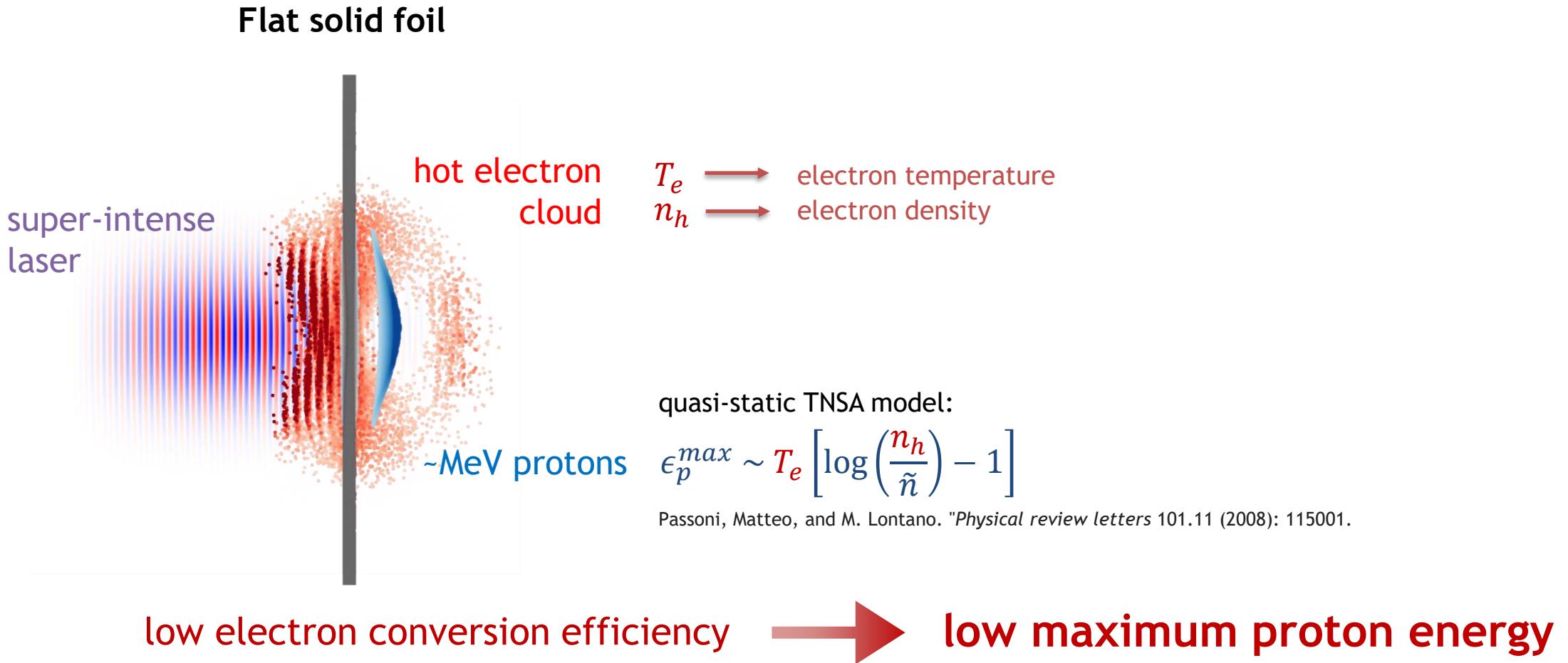
# Conventional laser-driven ion acceleration



# Conventional laser-driven ion acceleration

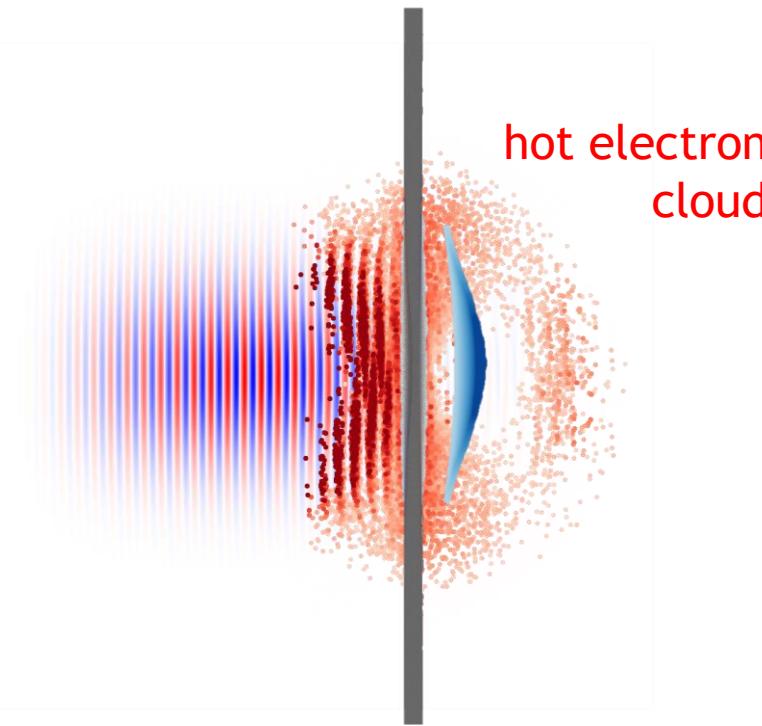


# Conventional laser-driven ion acceleration

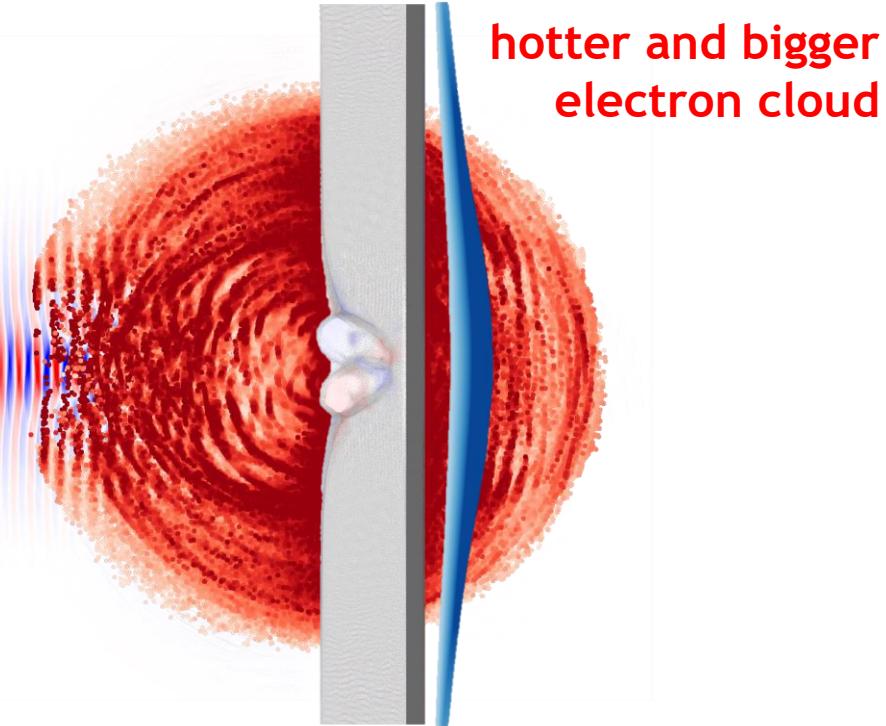


# Acceleration with the Double-Layer Target (DLT)

Flat solid foil



Near critical density layer

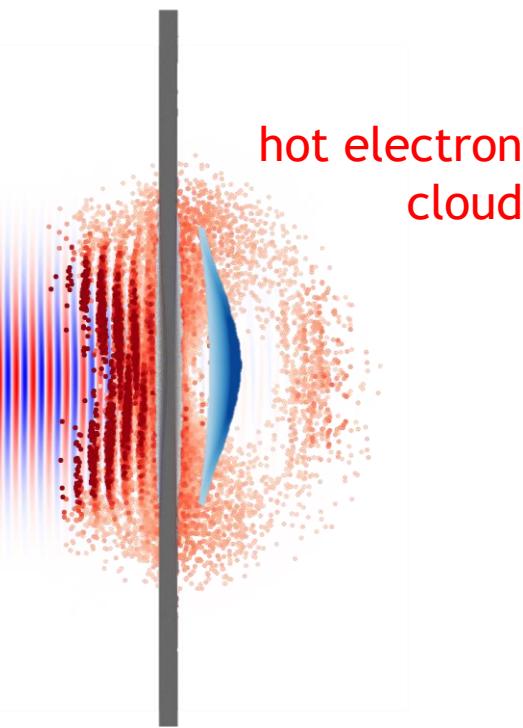


hotter and bigger  
electron cloud

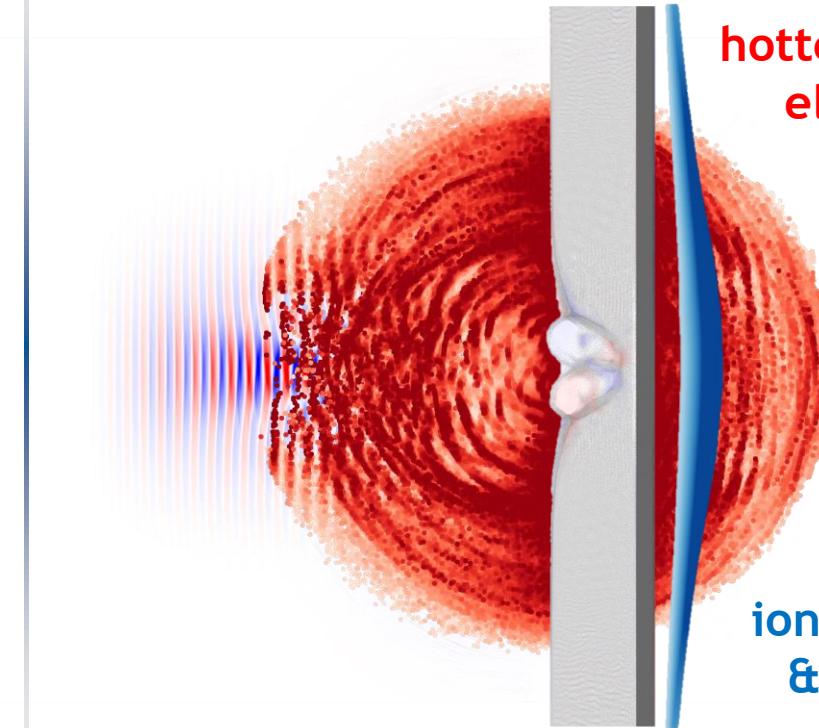
$$\begin{aligned} T_{e,DLT} &> T_e \\ n_{h,DLT} &> n_h \end{aligned}$$

# Acceleration with the Double-Layer Target (DLT)

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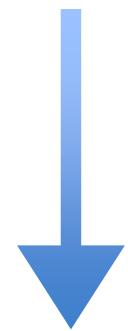


Near critical density layer



hotter and bigger  
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$$T_{e,DLT} > T_e \\ n_{h,DLT} > n_h$$



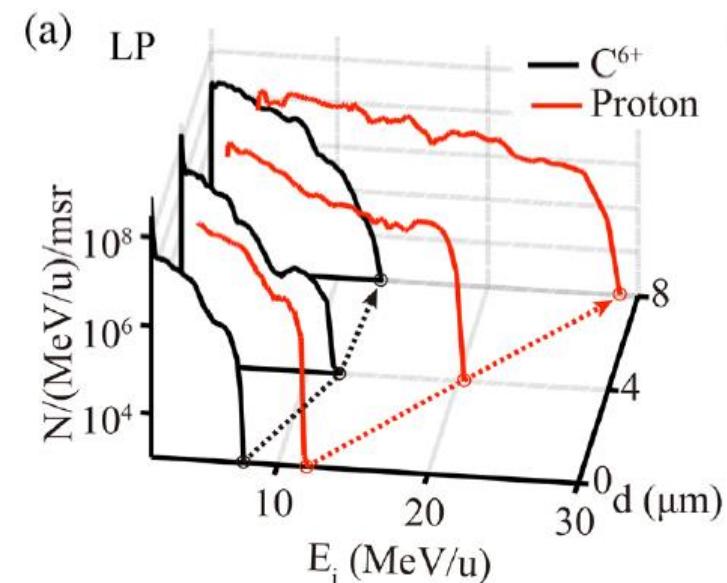
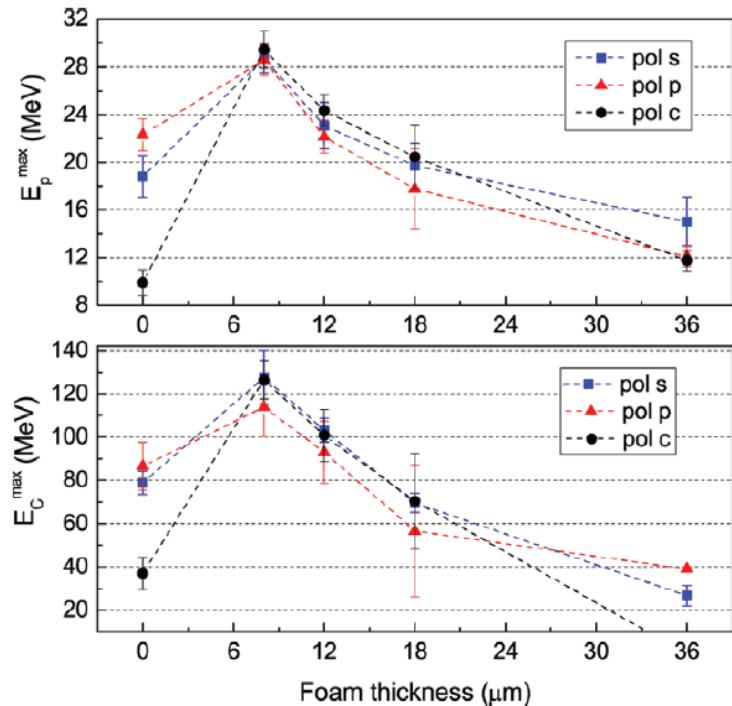
Higher  
ions energy  
& number

$$\epsilon_p^{max} \sim T_e \left[ \log\left(\frac{n_h}{\tilde{n}}\right) - 1 \right]$$

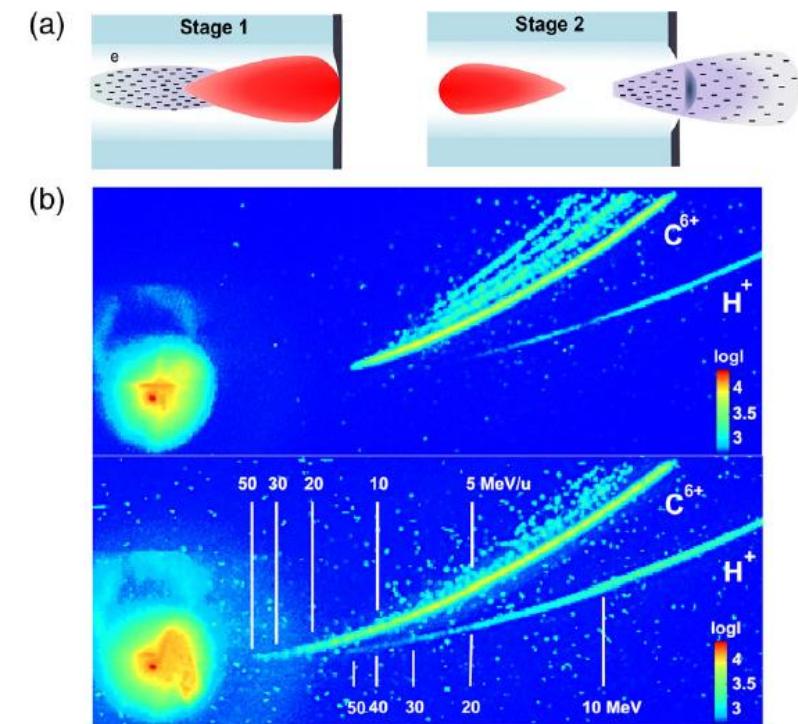
Advanced acceleration via **near-critical DLT**

# Experimental evidences

Tested by independent groups:



Bin, J. H., et al. *Physical review letters* 120.7 (2018): 074801.



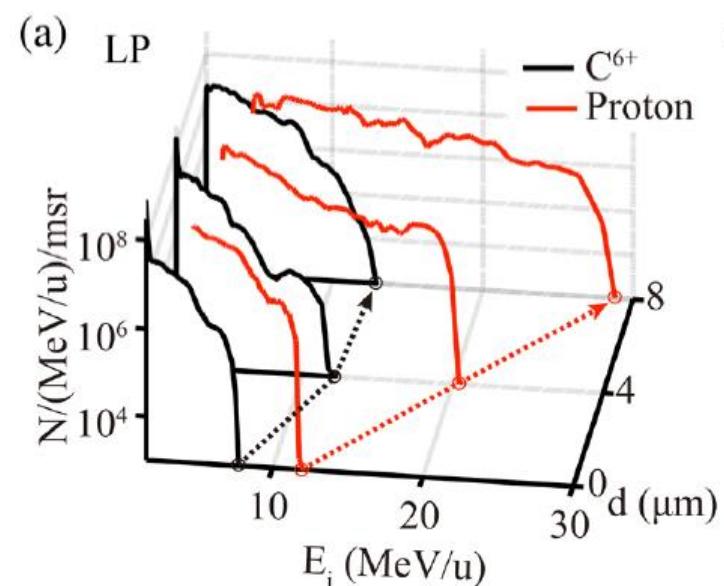
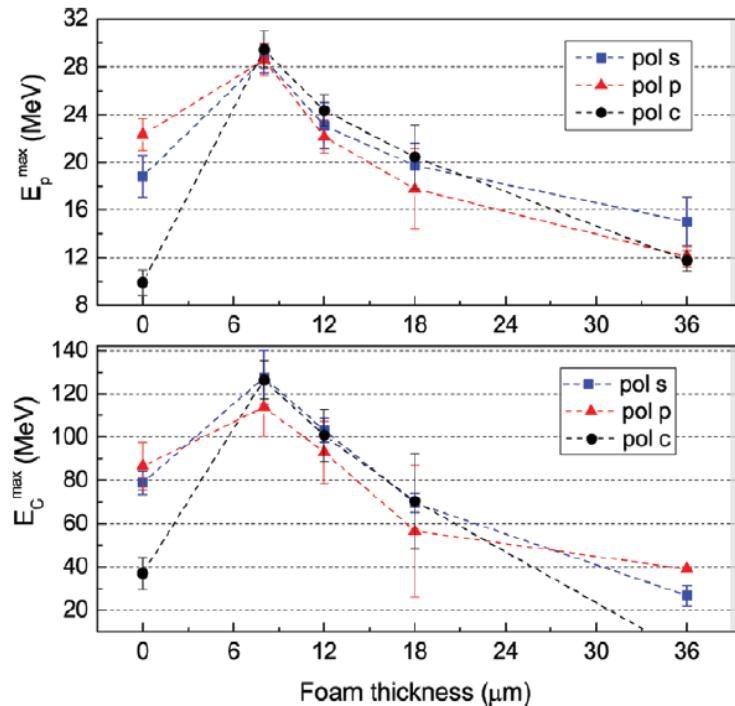
Ma, W. J., et al *Physical review letters* 122.1 (2019): 014803.

Prencipe, Irene, et al. *Plasma Physics and Controlled Fusion* 58.3 (2016): 034019.

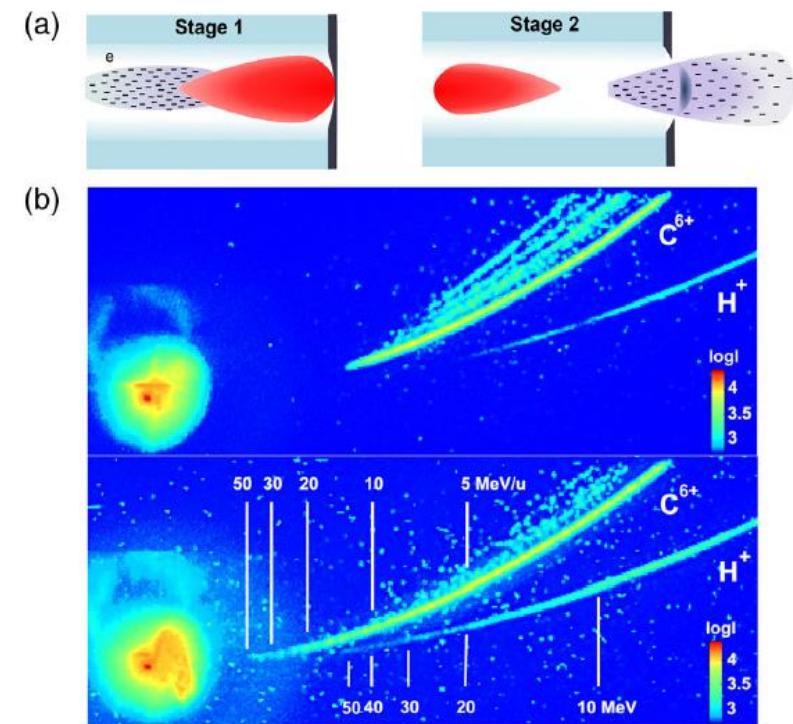
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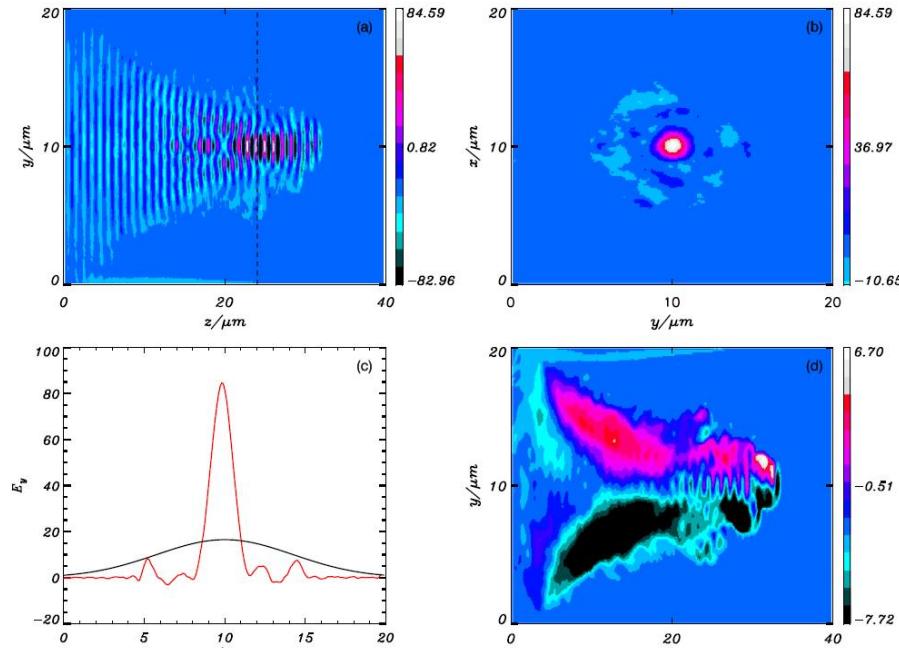


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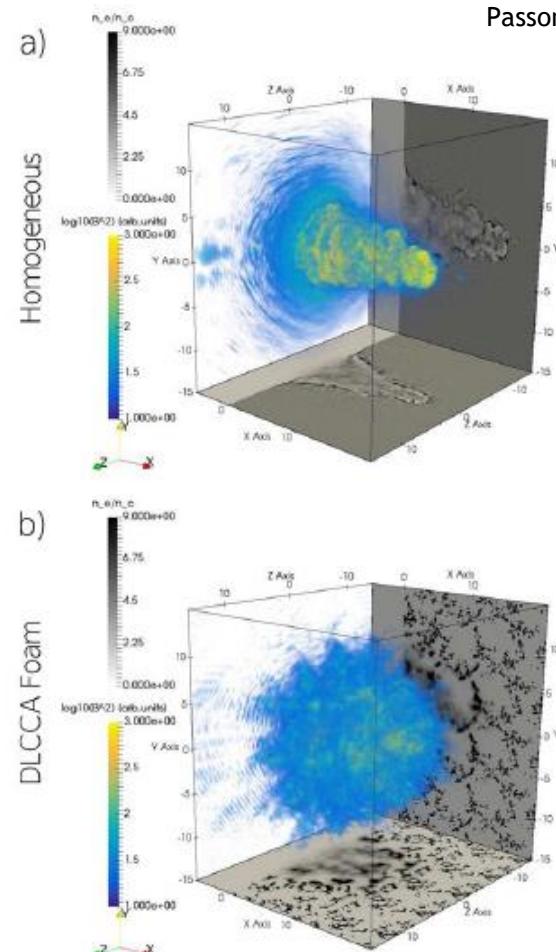
Precipice, Irene, et al. *Plasma Physics and Controlled Fusion* 58.3 (2016): 034019.  
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Have we achieved the best performances?

# PIC simulations help to understand the interaction physics

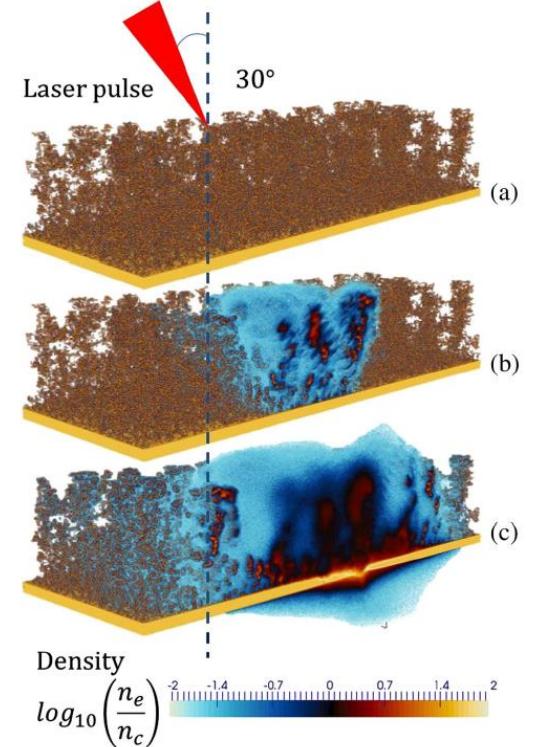


Wang, H. Y., et al. *Physical review letters* 107.26 (2011): 265002.

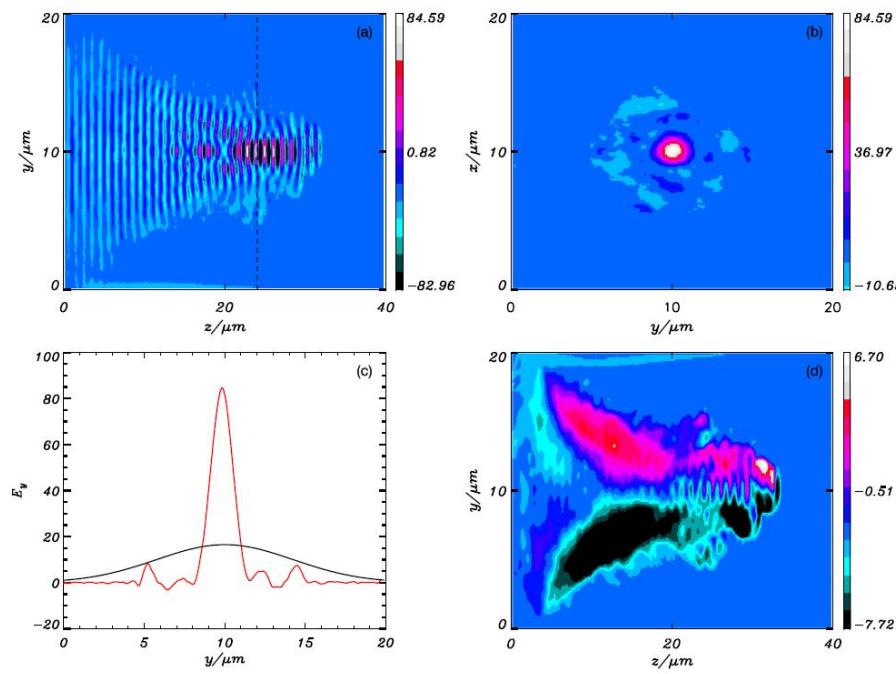


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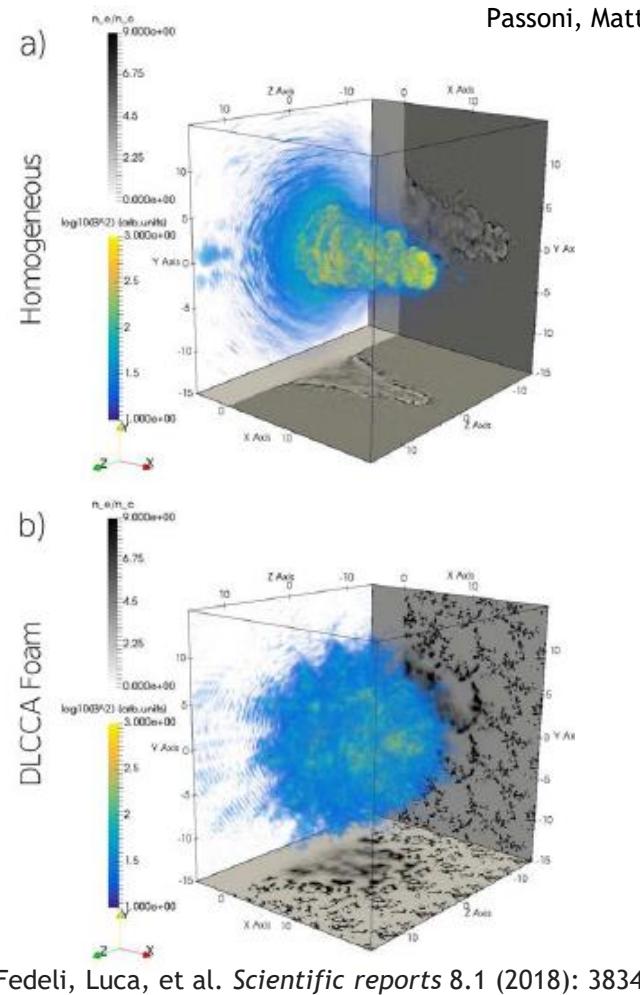
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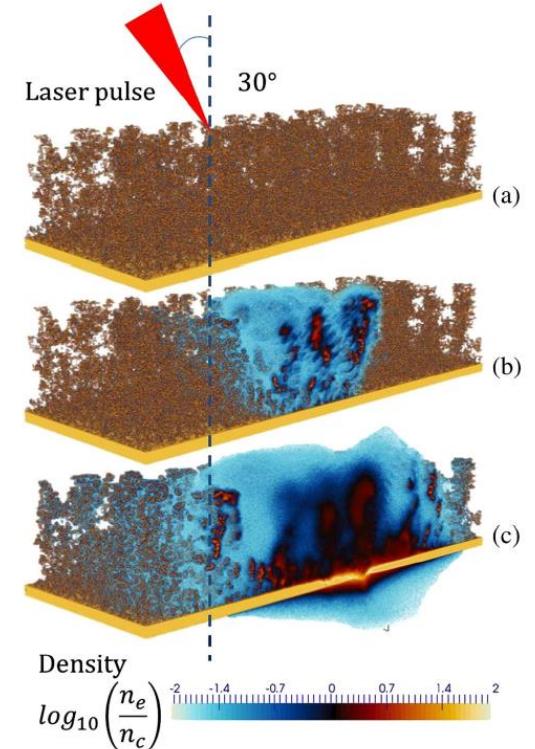


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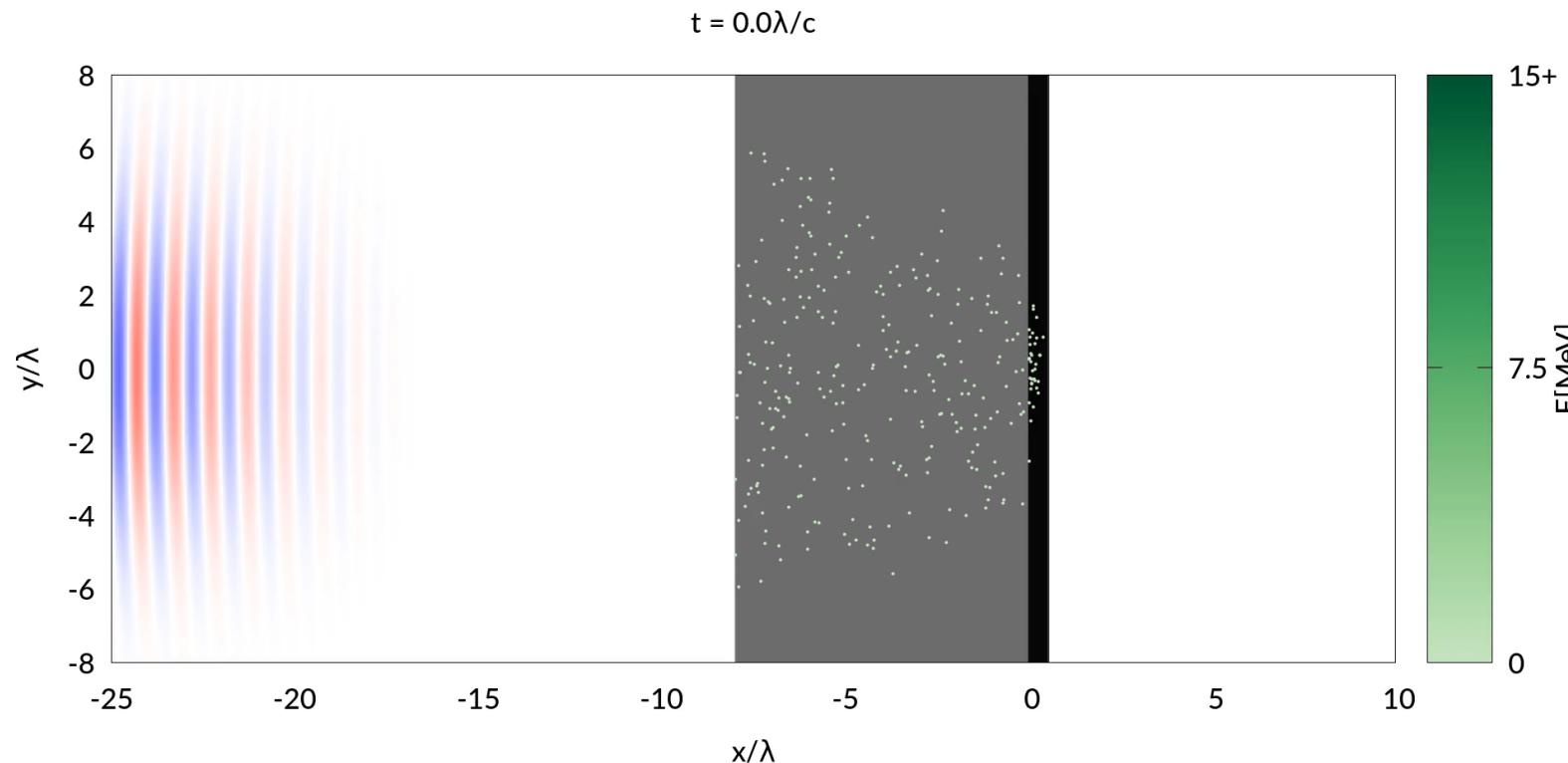
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Passoni, Matteo, et al. *Physical Review Accelerators and Beams* 19.6 (2016): 061301.



Realistic 3D PIC simulations are computationally very expensive

# From PIC simulations to a minimal model

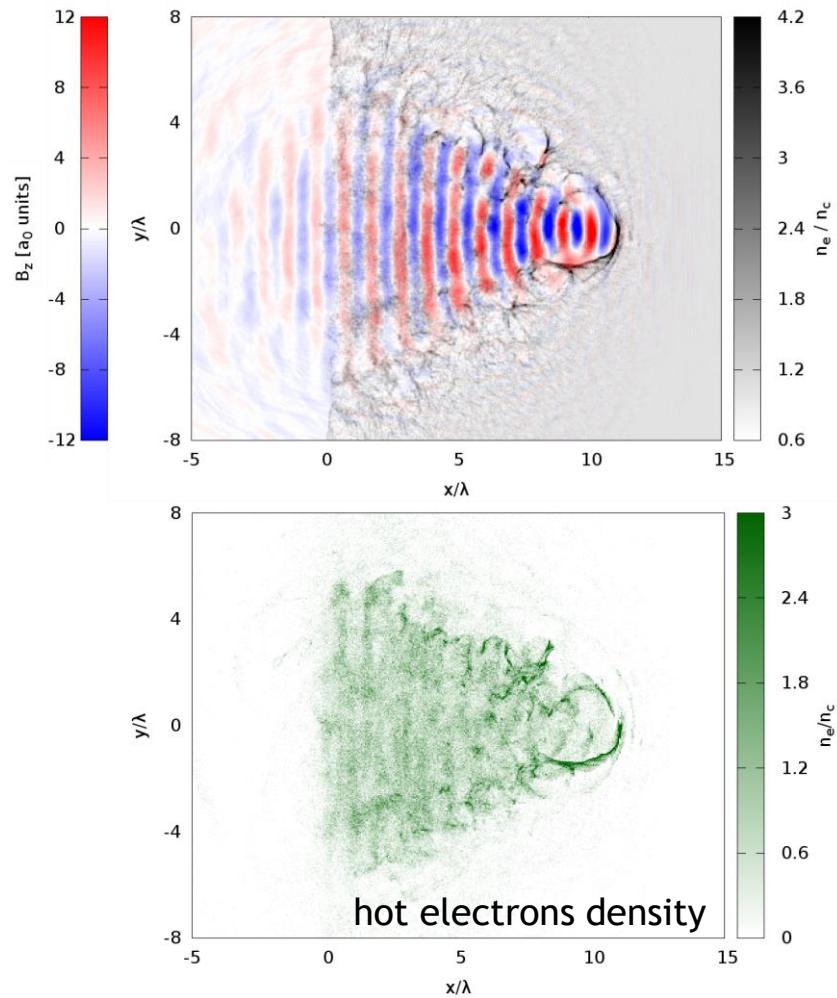


## Main observed phenomena:

- Pulse drilling a channel
- Pulse self-focusing
- Hot electrons generation
- Self-generated magnetic fields

A modellistic approach is beneficial for the DLT optimization

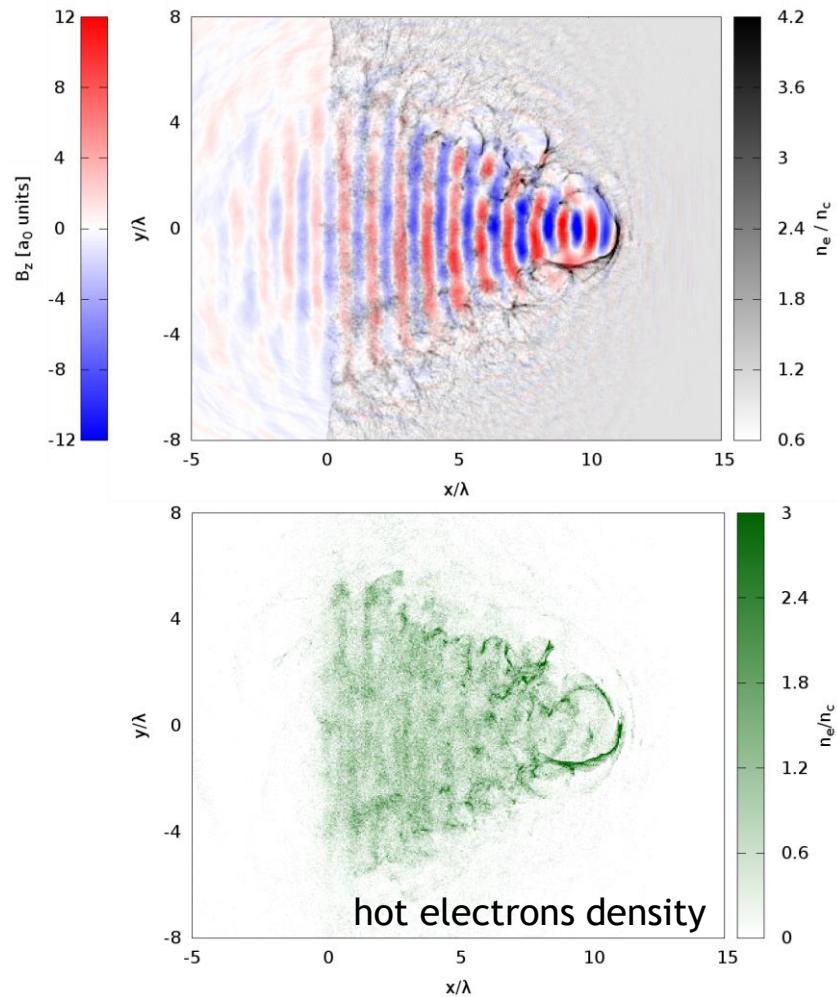
# A minimal model is proposed



## METHODS:

1. Theoretical model with free parameters
2. Parameters estimations with 2D/3D PIC simulations

# A minimal model is proposed



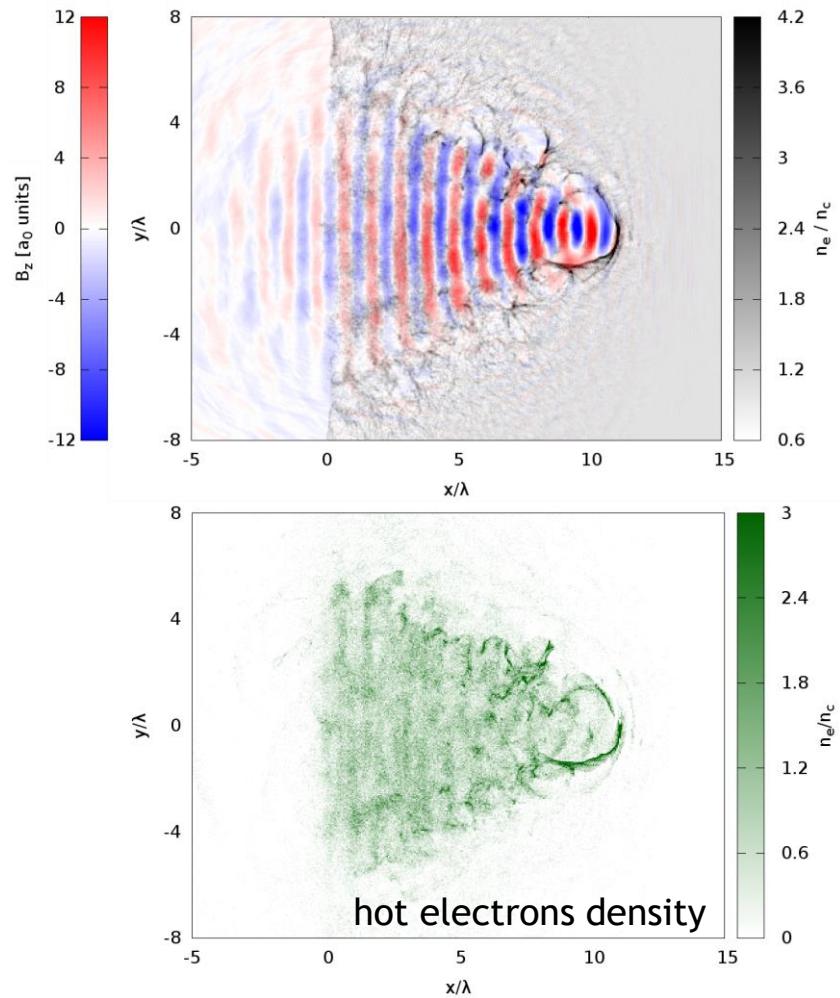
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## MODEL STEPS:

1. Laser self-focusing
2. Laser energy loss and amplification
3. Hot electrons heating
4. Ions acceleration

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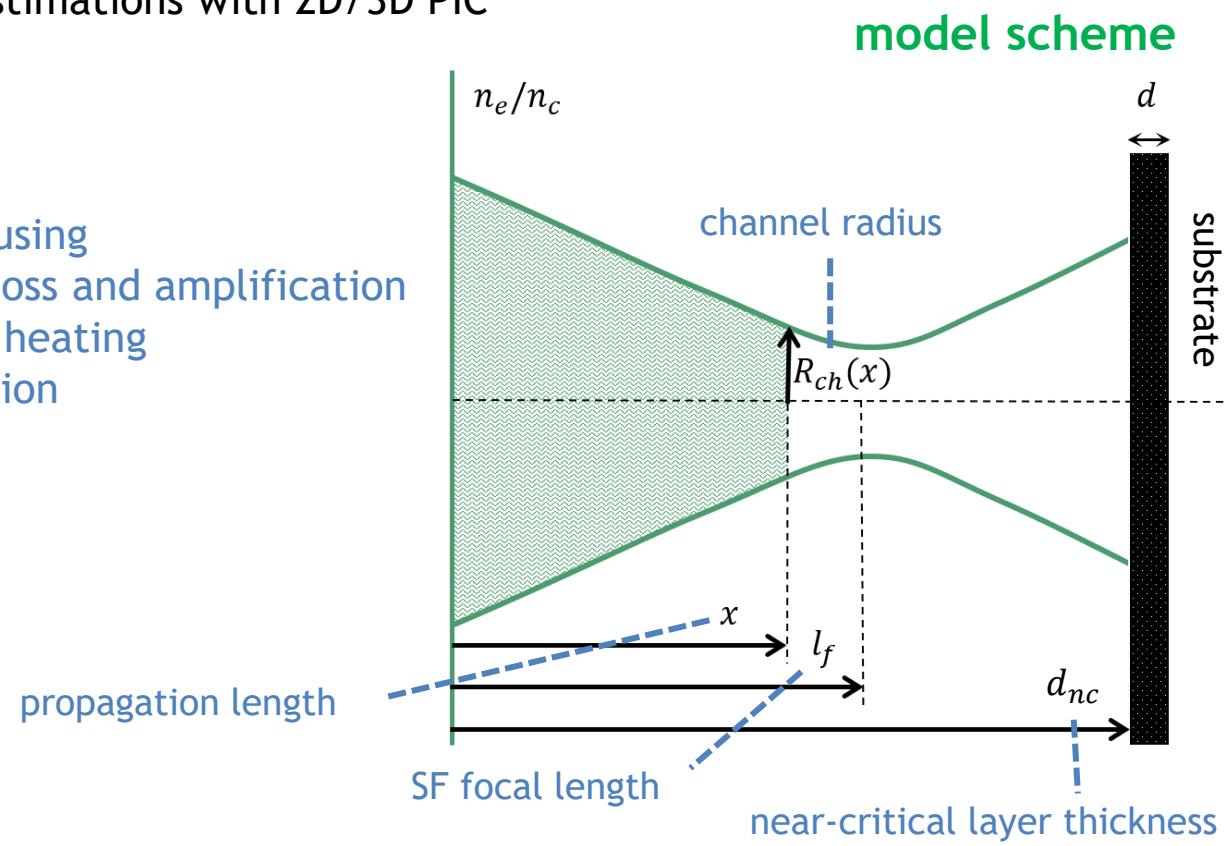


## METHODS:

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# 1<sup>st</sup> step: laser propagation into a near-critical plasma

Pulse waist focuses with  
a thin-lens law:

$$w(x) = w_m \sqrt{1 + \left(\frac{x - l_f}{x_R}\right)^2}$$

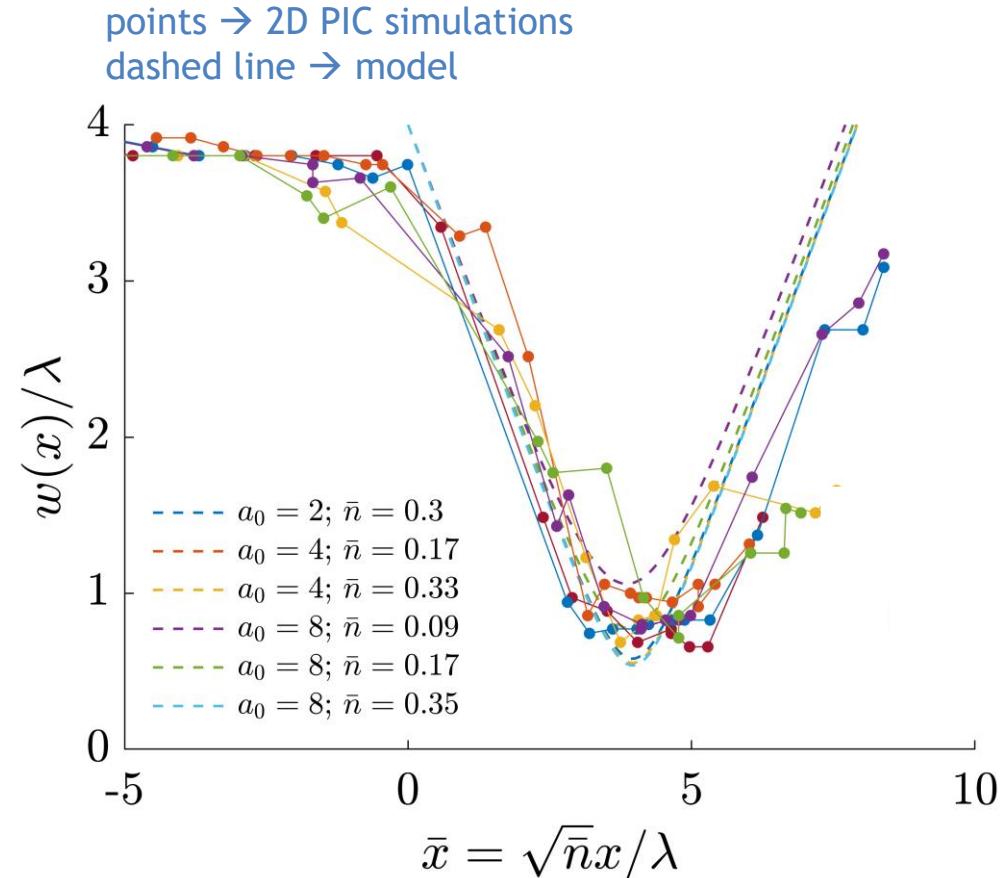
minimum waist

$$w_m = \frac{\lambda}{\pi} \frac{1}{\sqrt{\bar{n}}}$$

Wang, H. Y., et al. *Physical review letters* 107.26 (2011): 265002.

relativistic  
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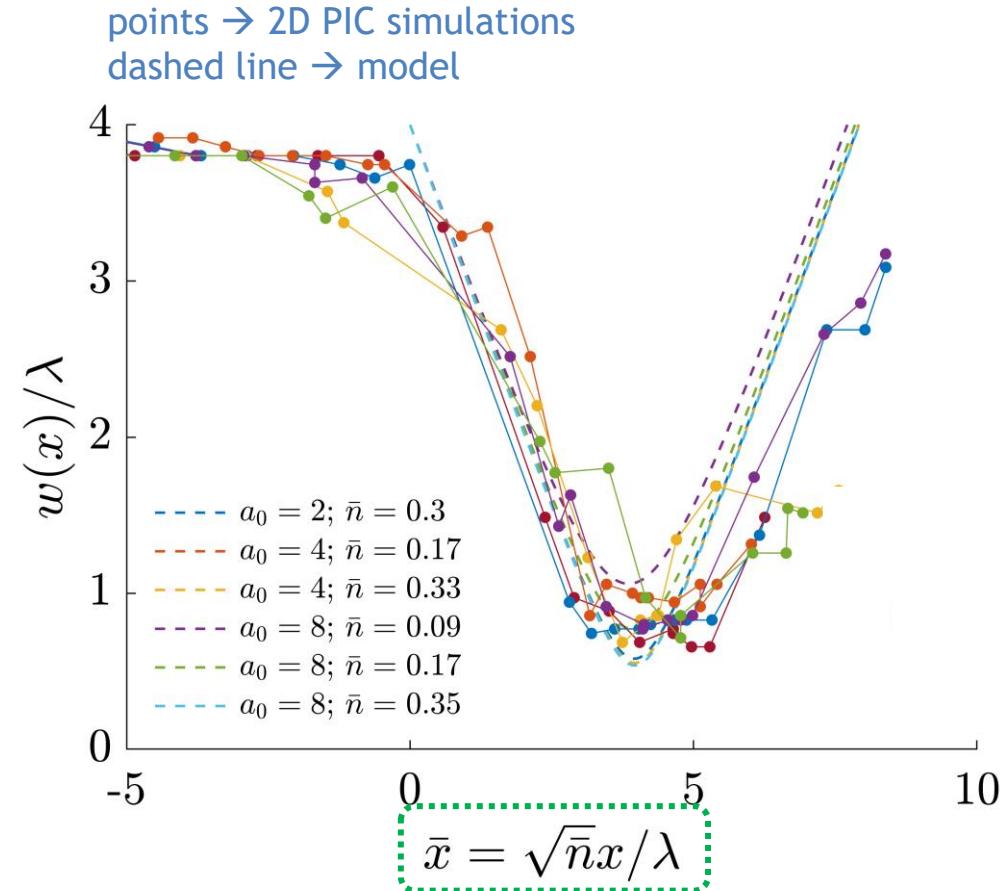
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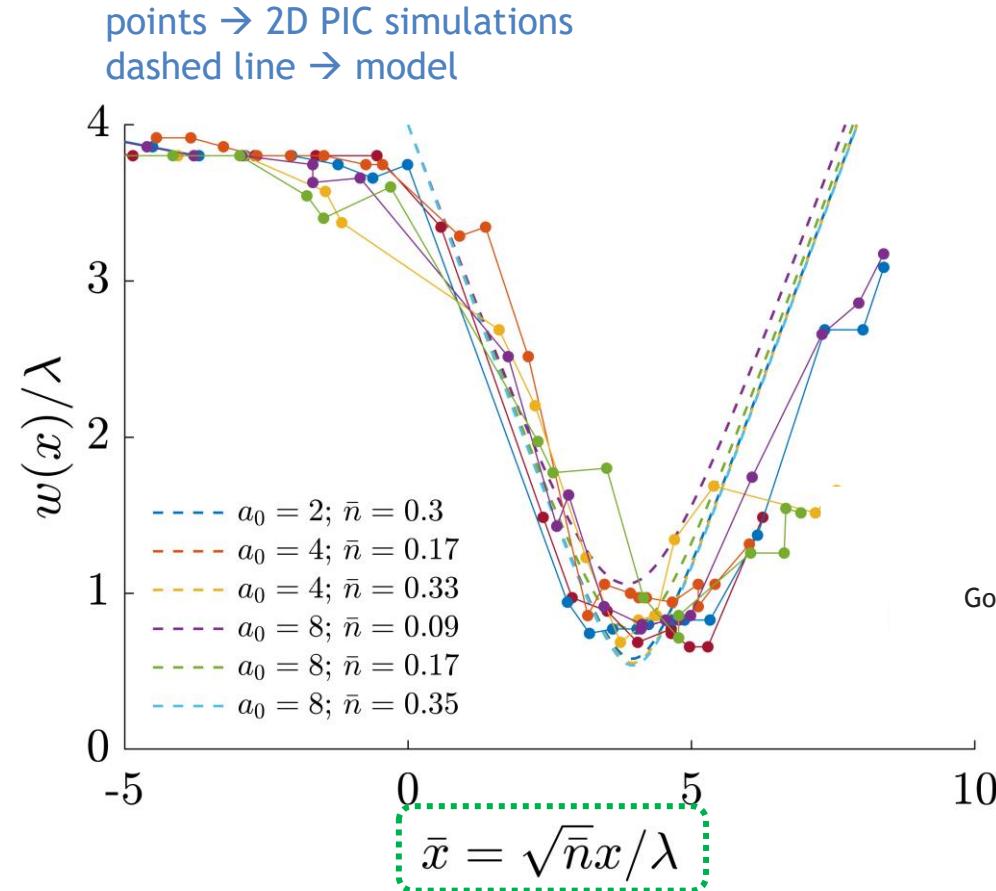
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thin-lens law can be written as:

$$w(\bar{x}) \sim \lambda \sqrt{\frac{1}{\pi^2 \bar{n}}} + \left( \bar{x} - \frac{w_0}{\lambda} \right)^2$$

$\bar{x} = \sqrt{\bar{n}}x/\lambda$

The propagation is self-similar!

Gordienko, S., and A. Pukhov. *Physics of Plasmas* 12.4 (2005): 043109.

## 2<sup>nd</sup> step: pulse energy loss and amplification

pulse energy loss equation:

$$d\varepsilon_p = -T_{nc}(x)n_e 2R_{ch}(x)dx$$

coupled with

amplification equation:

$$\bar{a}(x) = \frac{a(x)}{a_0} = \sqrt{\frac{\varepsilon_p(x)}{w(x)/w_0}}$$

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electron temperature  $T_{nc}(x) = C_{nc}[\gamma(x) - 1]m_e c^2$

corrected ponderomotive scaling

Cialfi, Lorenzo, Luca Fedeli, and Matteo  
Passoni. *Physical Review E* 94.5 (2016): 053201.

channel radius  $R_{ch}(x) = r_c w(x)$  proportional to pulse waist

## 2<sup>nd</sup> step: pulse energy loss and amplification

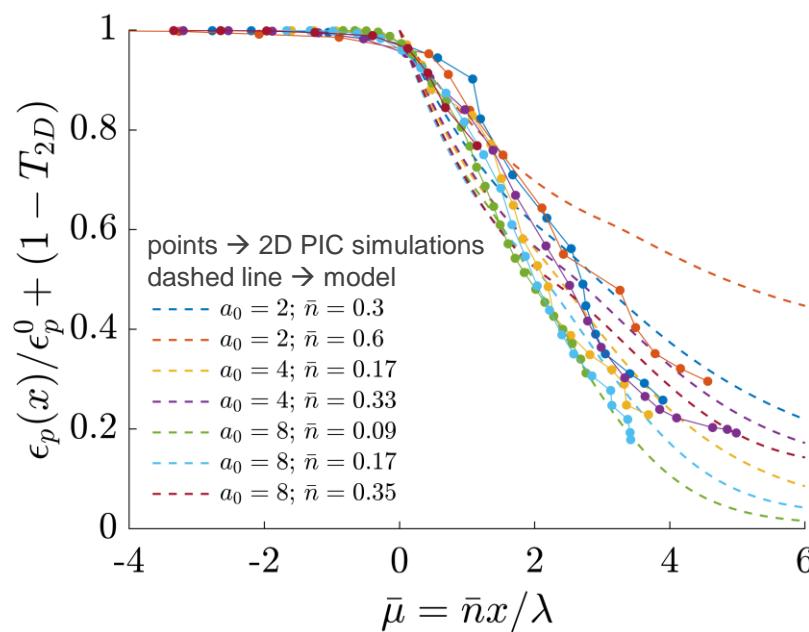
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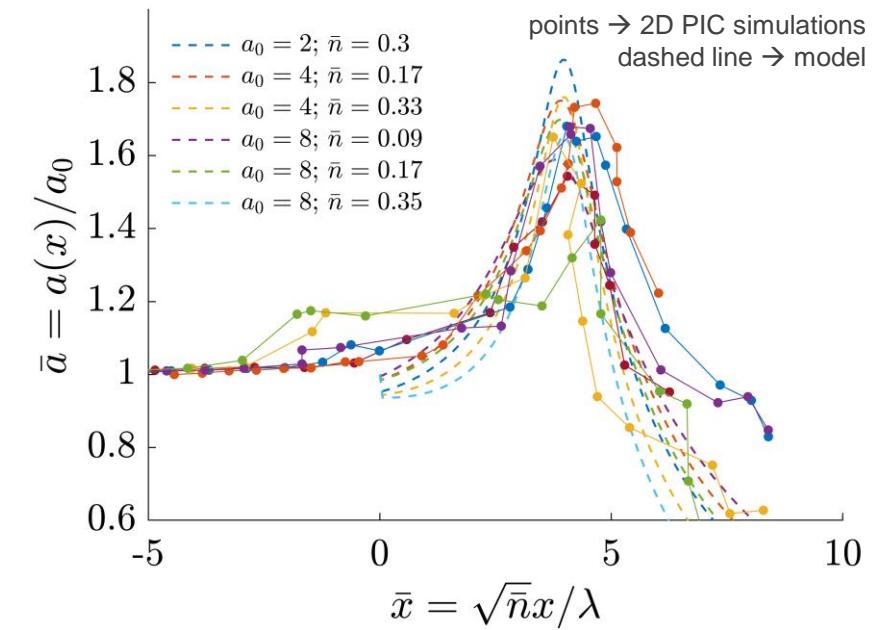


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Cialfi, Lorenzo, Luca Fedeli, and Matteo Passoni. *Physical Review E* 94.5 (2016): 053201.



Two free parameters:  $C_{nc} = 1.7$ ;  $r_c = 2.0$

## 3<sup>rd</sup> step: hot electrons heating

The energy lost by the pulse is given to the hot electrons:

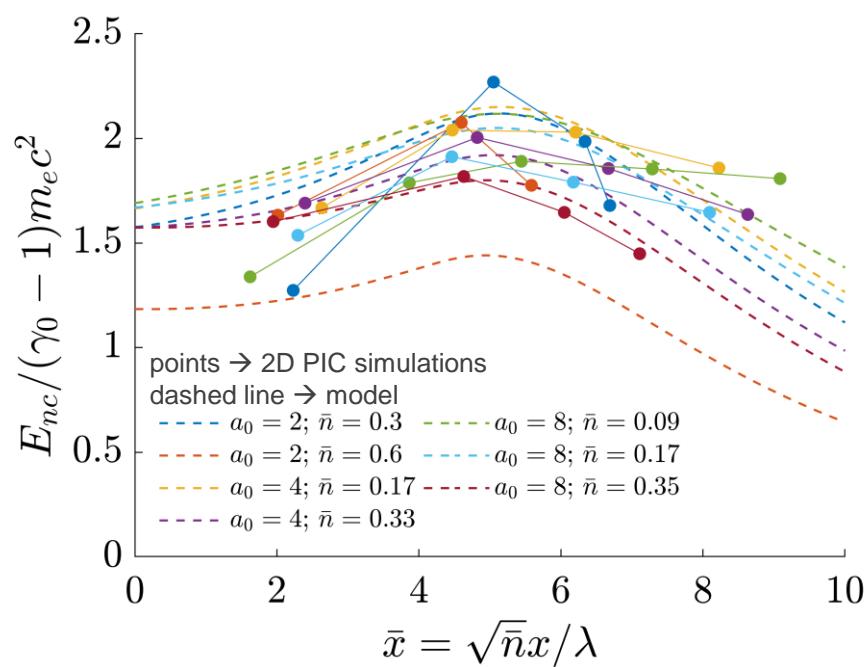
$$E_{nc}(x) = \frac{(1 - \bar{\varepsilon}_p(x)) \varepsilon_{p0}}{N_{nc}(x)}$$

→ Total number of electrons  
in the channel

### 3<sup>rd</sup> step: hot electrons heating

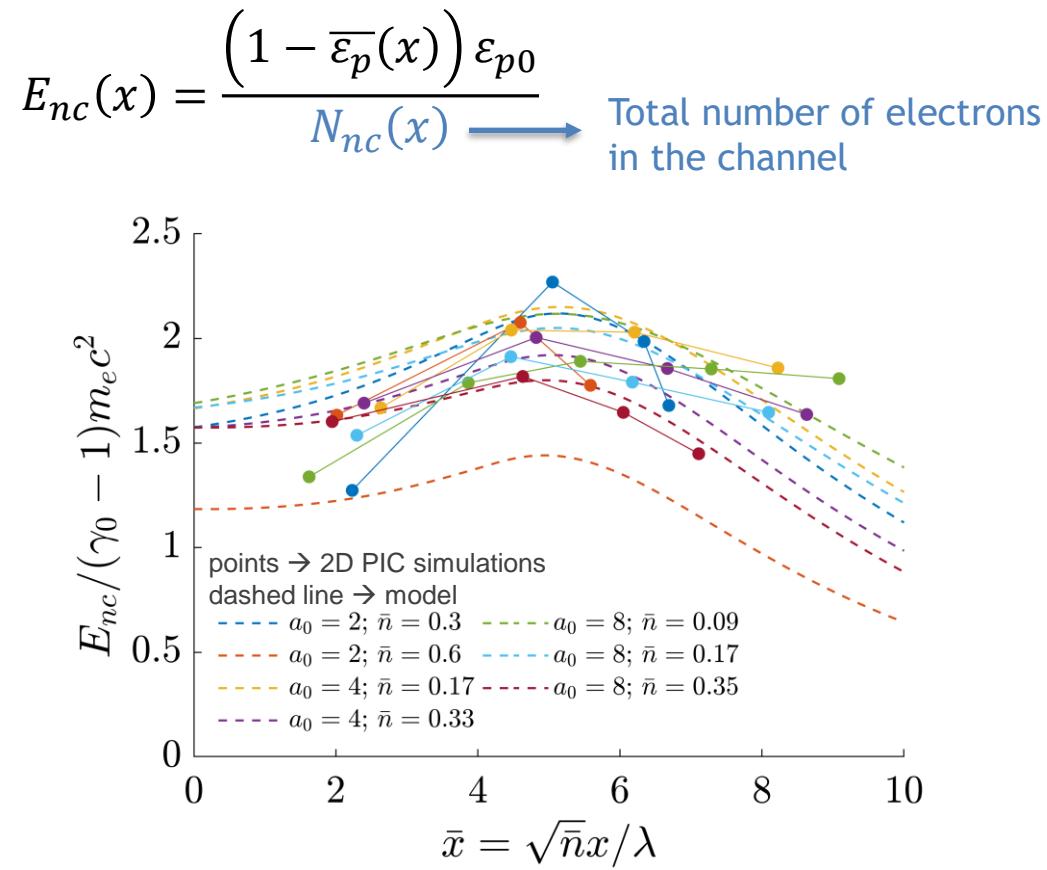
The energy lost by the pulse is given to the hot electrons:

$$E_{nc}(x) = \frac{(1 - \bar{\varepsilon}_p(x)) \varepsilon_{p0}}{N_{nc}(x)} \quad \text{Total number of electrons in the channel}$$



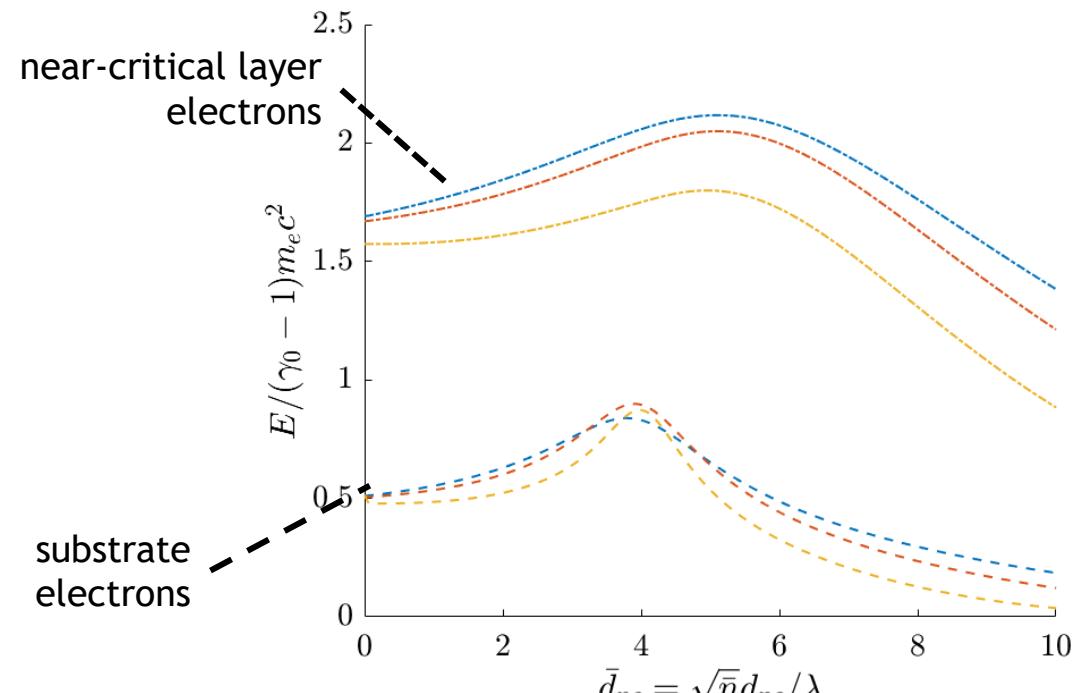
# 3<sup>rd</sup> step: hot electrons heating

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Also electrons from the substrate are considered:

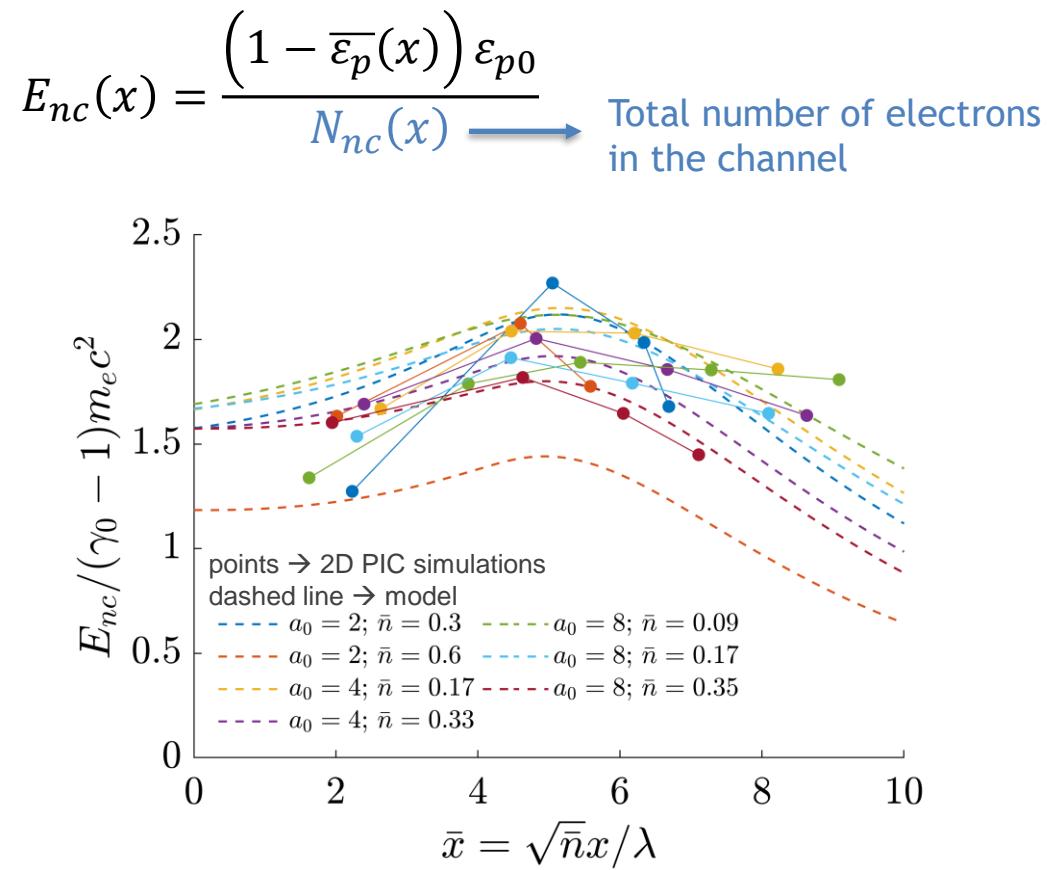
$$E_s(d_{nc}) = C_s[\gamma(d_{nc}) - 1]m_e c^2$$



Additional free parameter:  $C_s = 0.24$

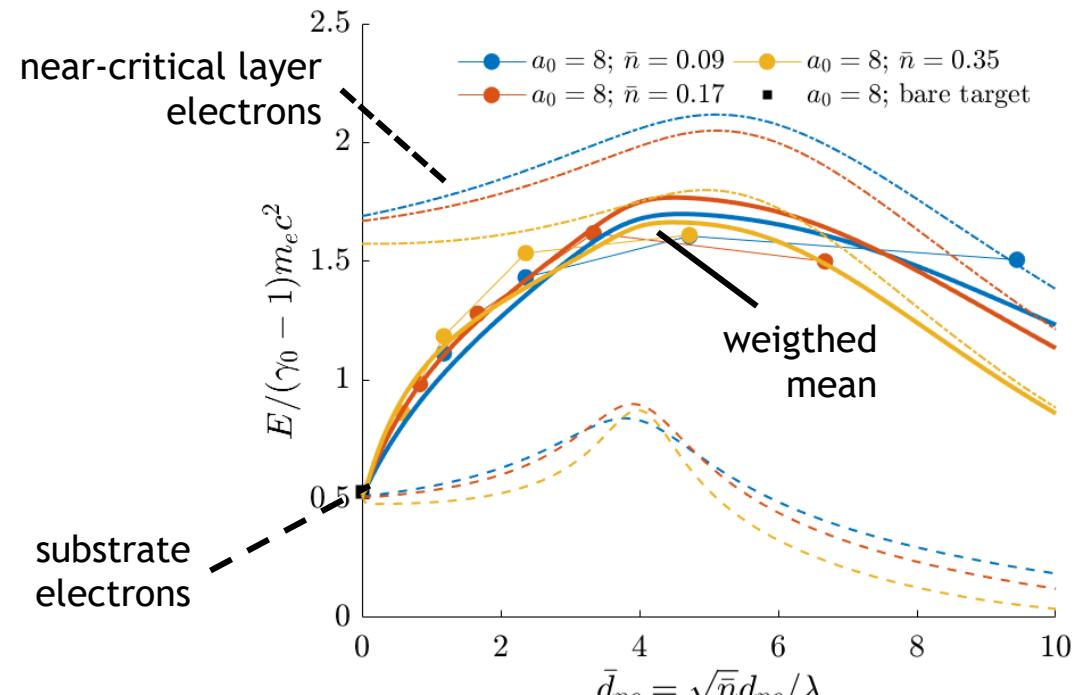
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## 4<sup>th</sup> step: proton maximum energy estimation

Quasi-static model:

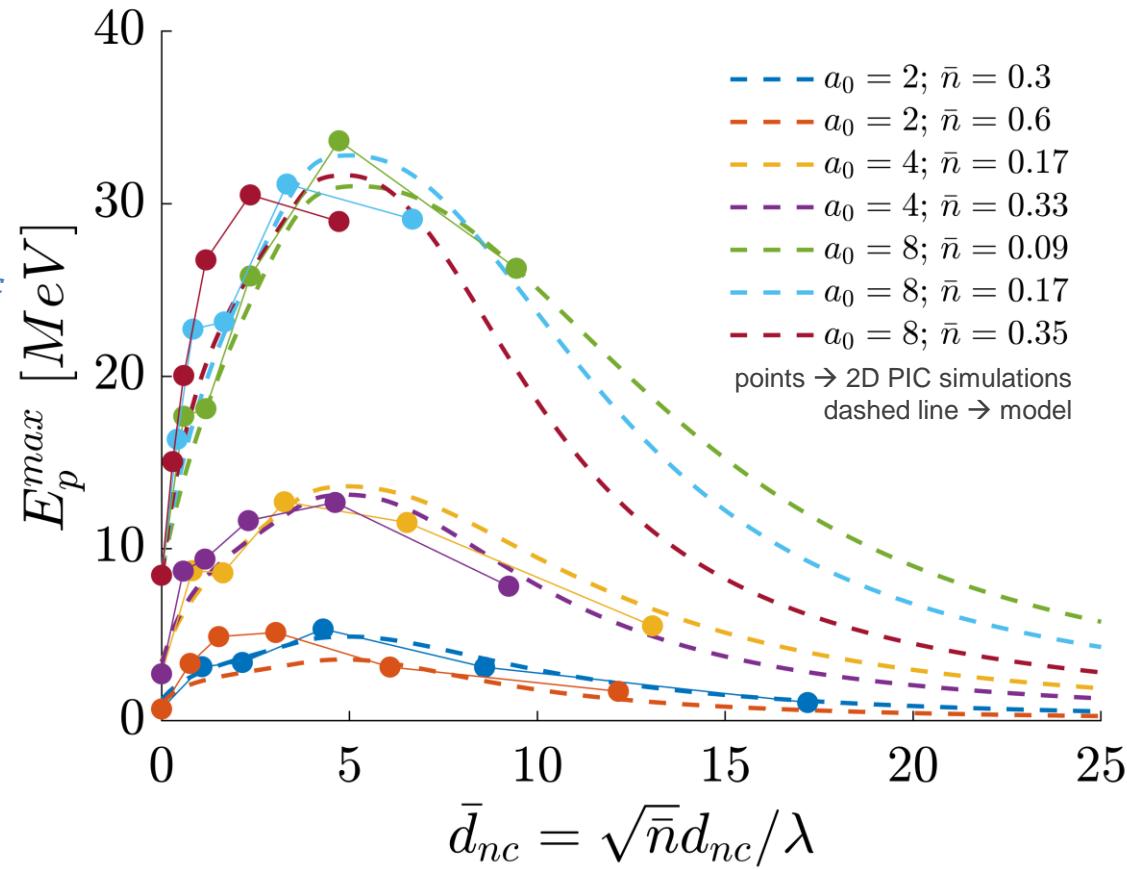
$$\epsilon_p^{max} = E_{DLT} \left[ \log \left( \frac{n_{h,DLT}}{\tilde{n}} \right) - 1 \right]$$

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last free parameter:  $\tilde{n} = 1.3 \cdot 10^{-3} n_c$

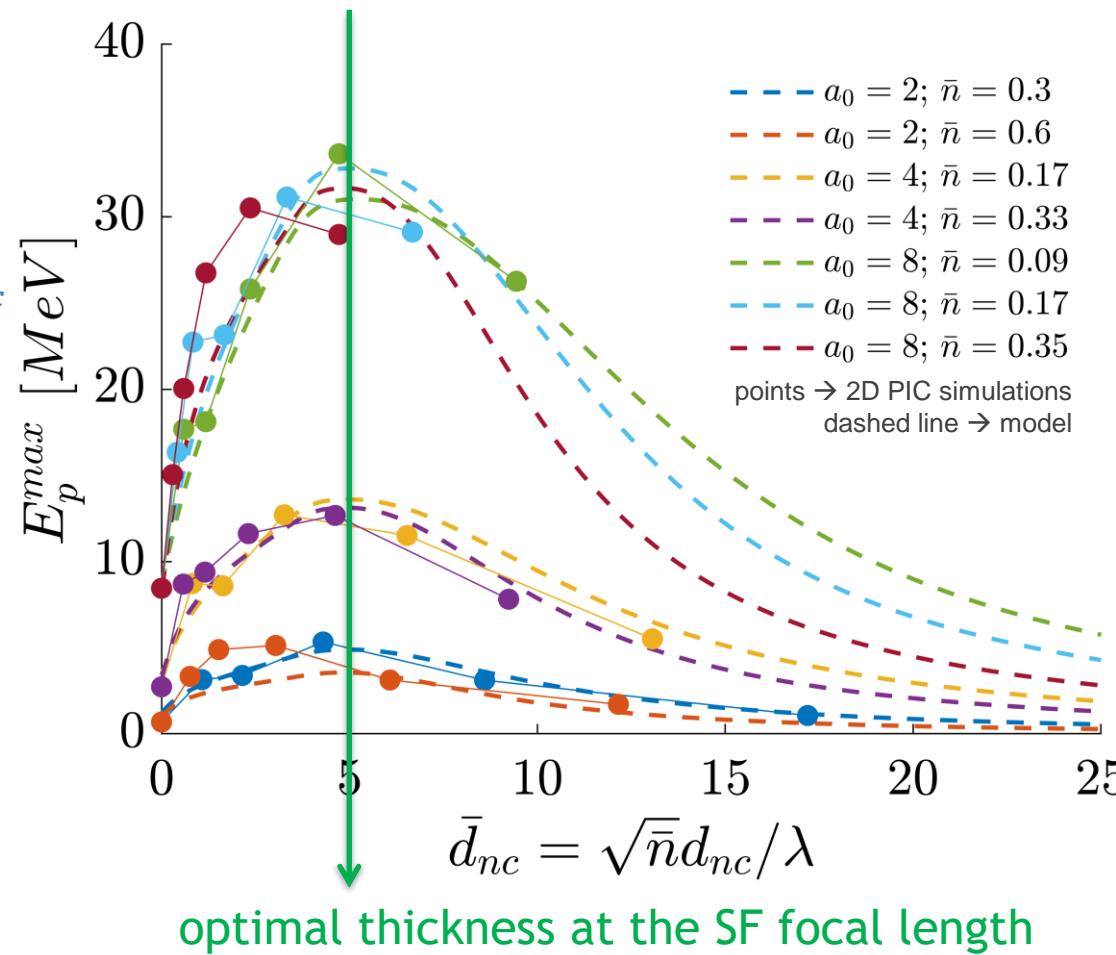


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$$\bar{d}_{nc} = \sqrt{\bar{n}} d_{nc} / \lambda$$

optimal thickness at the SF focal length

$$d_{nc}^{opt} \sim w_0 / \sqrt{\bar{n}}$$

# The same model is solved in 3D

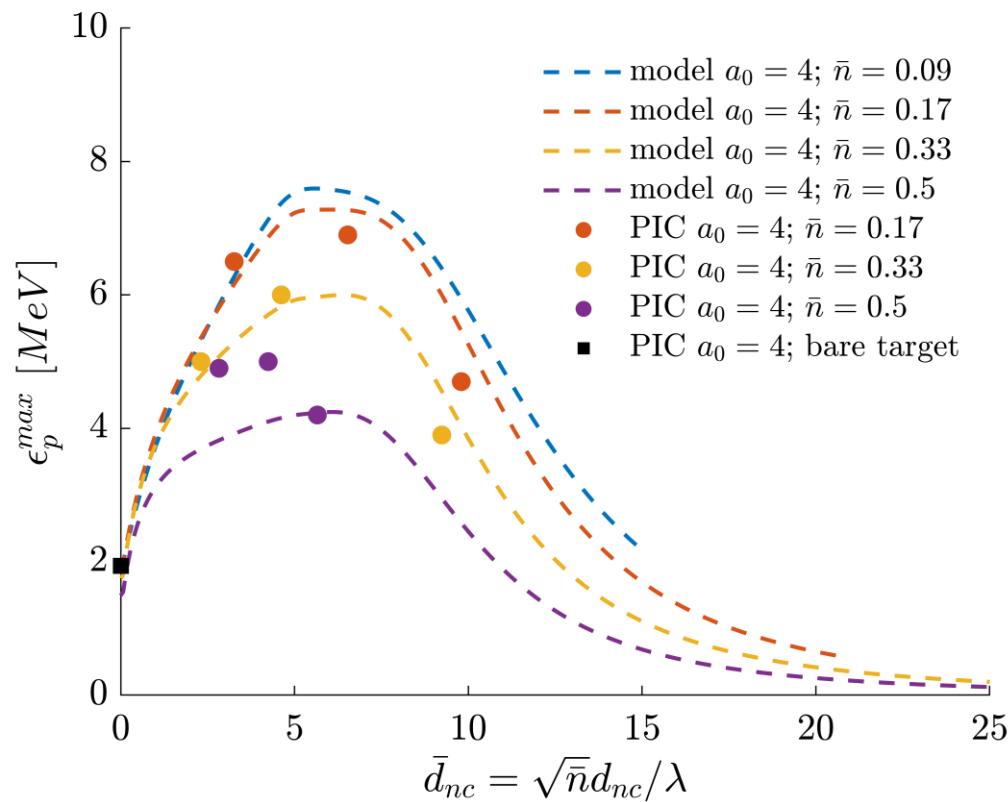
3D parameters:

$$C_{nc} = 1.1$$

$$r_c = 2.1$$

$$C_s = 0.18$$

$$\tilde{n} = 5 \cdot 10^{-2} n_c$$



# The same model is solved in 3D

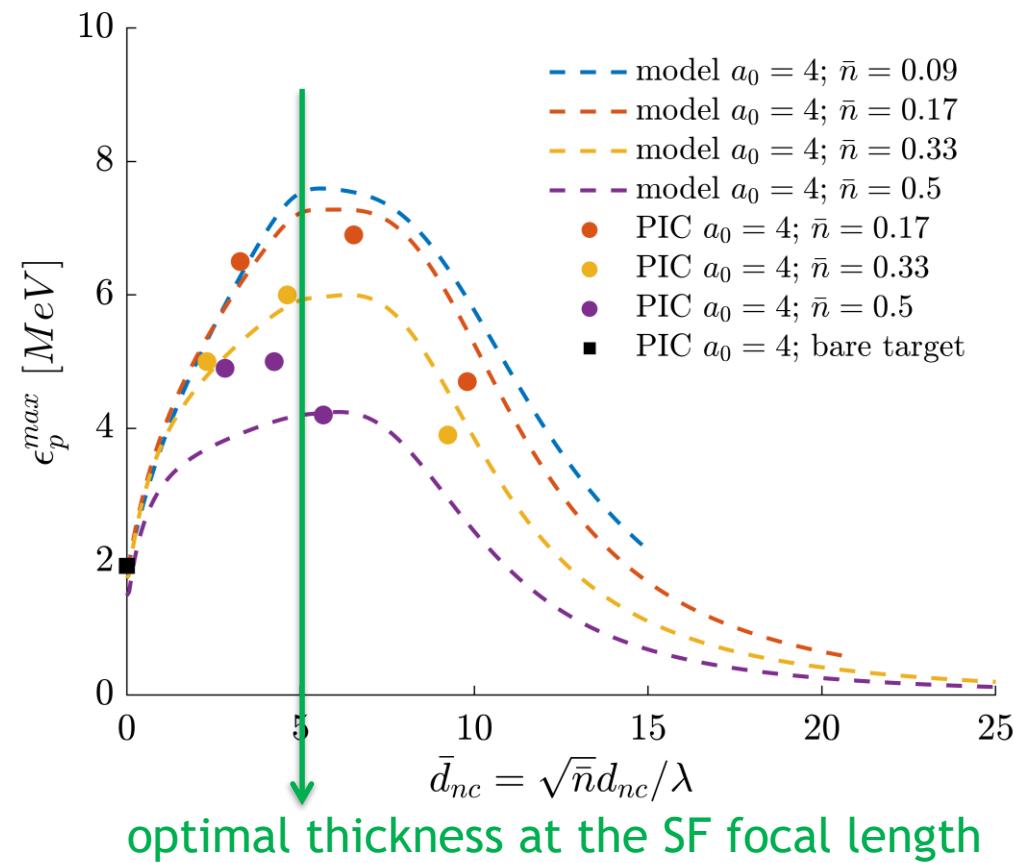
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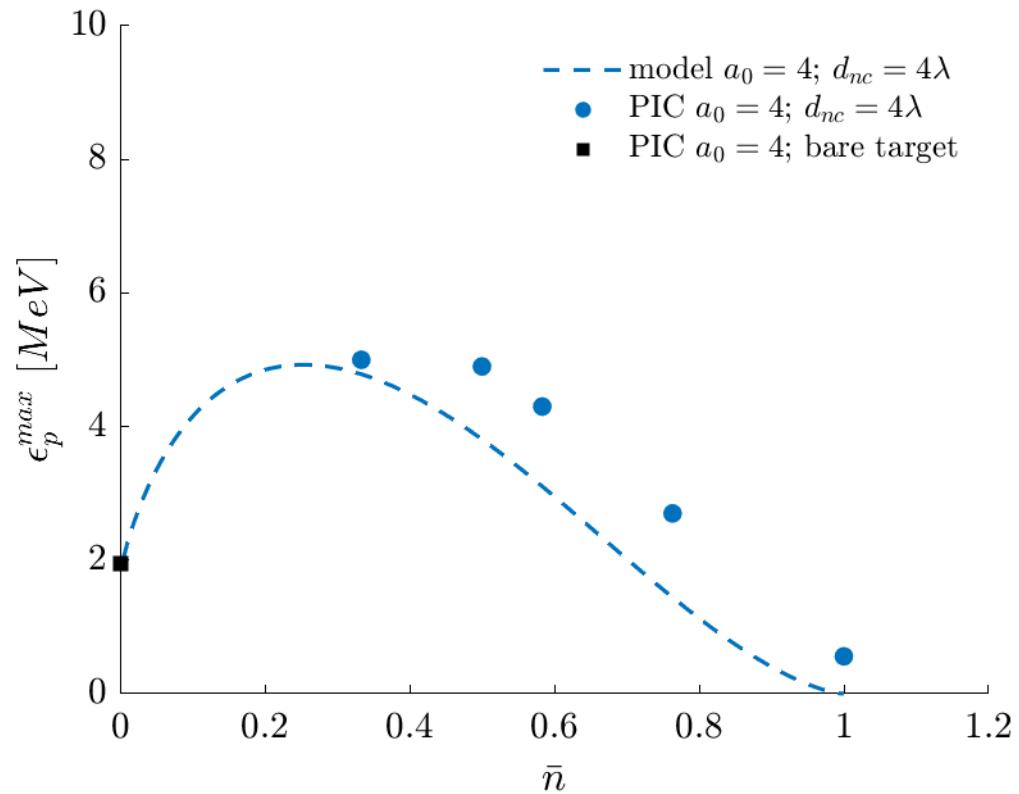
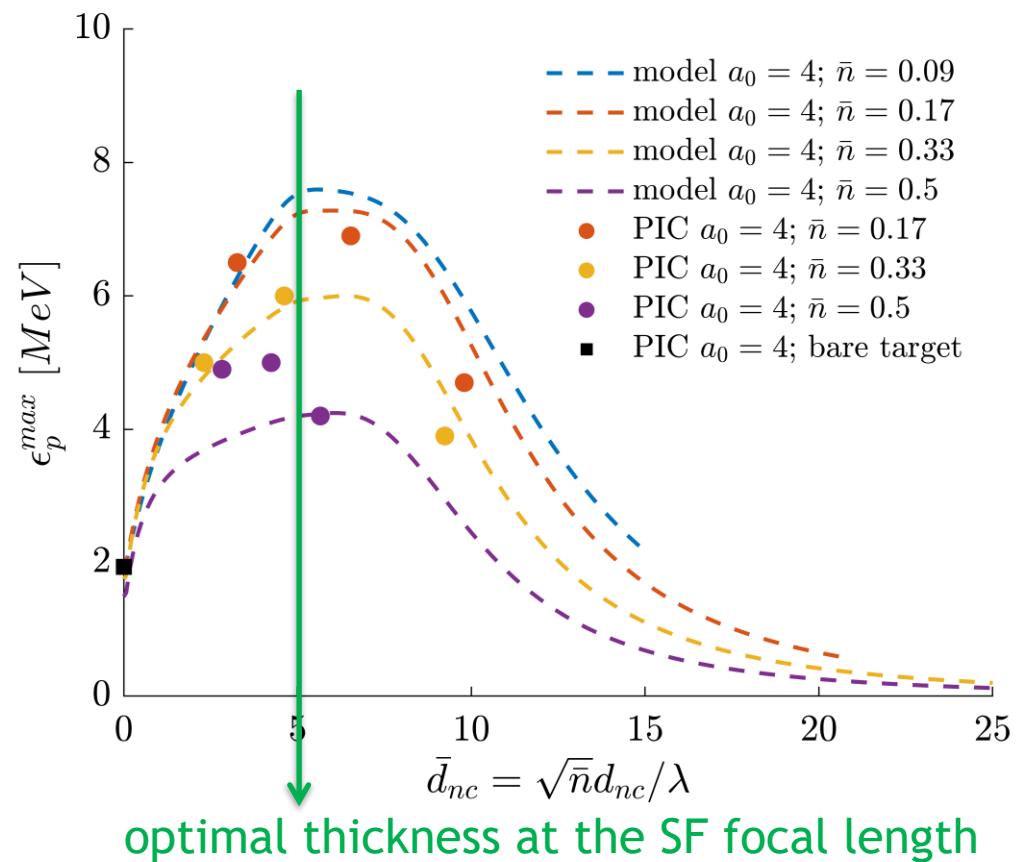
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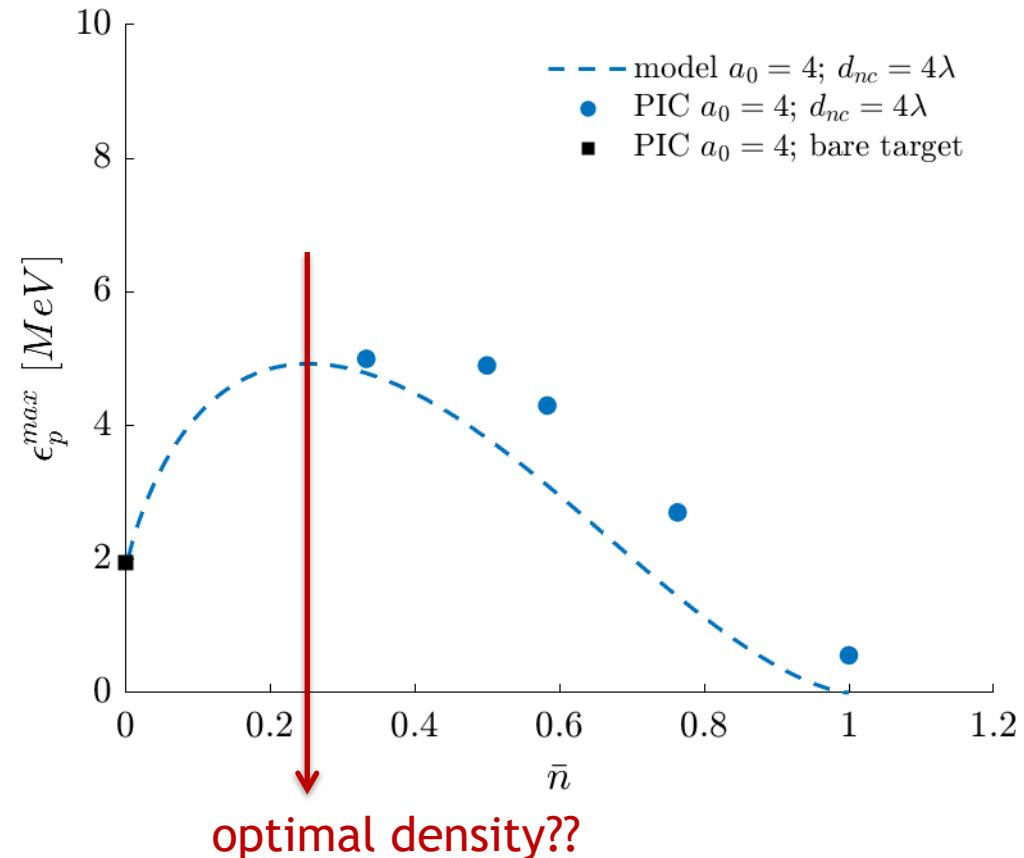
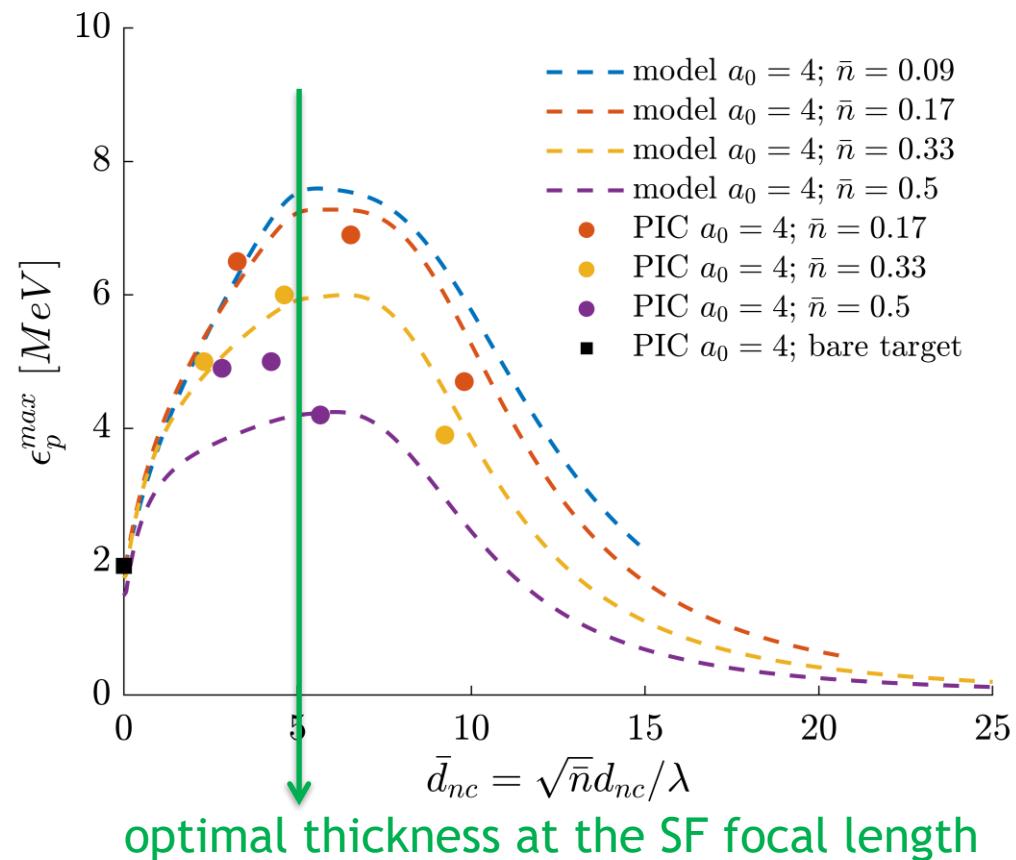
$$\begin{aligned}C_{nc} &= 1.1 \\r_c &= 2.1 \\C_s &= 0.18 \\\tilde{n} &= 5 \cdot 10^{-2} n_c\end{aligned}$$



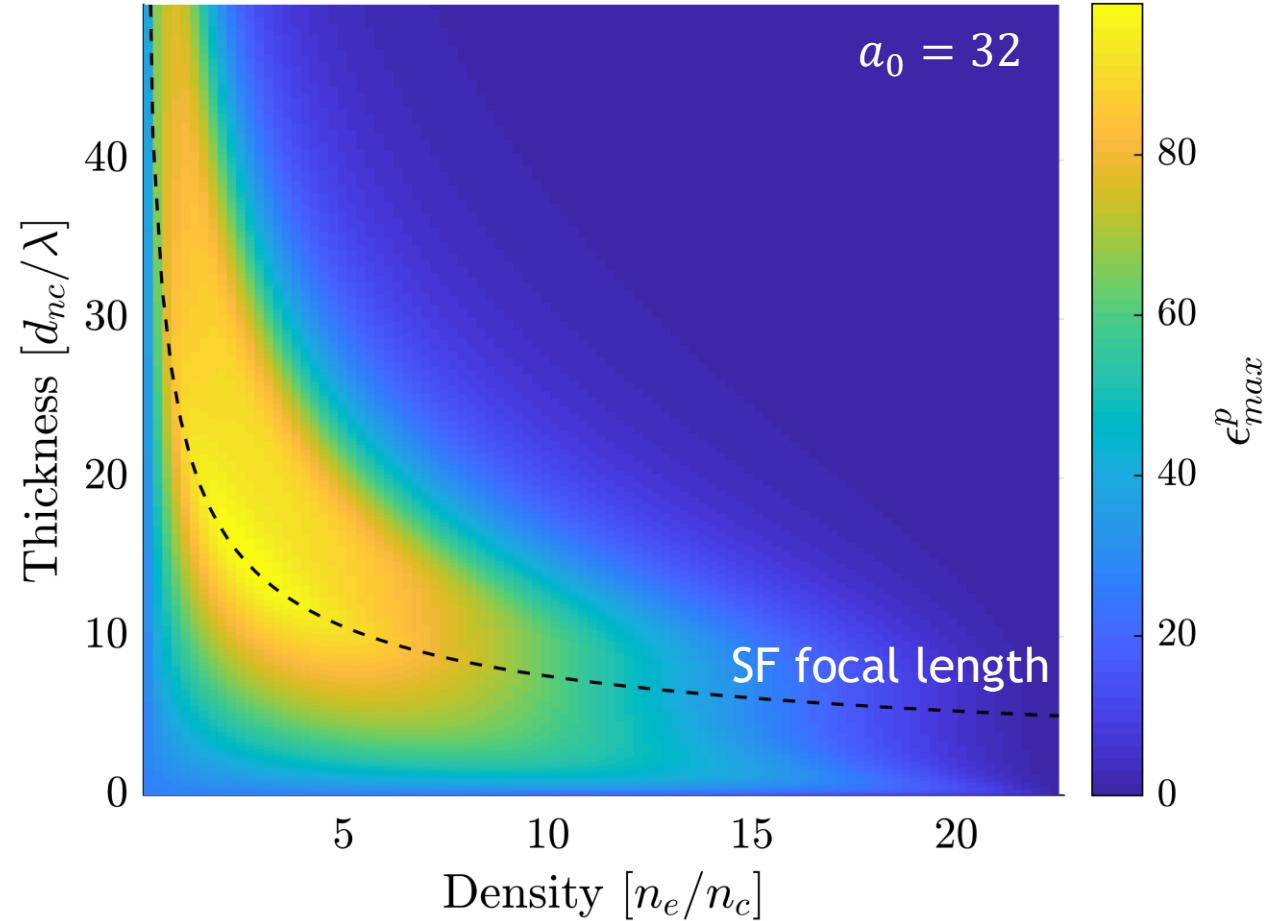
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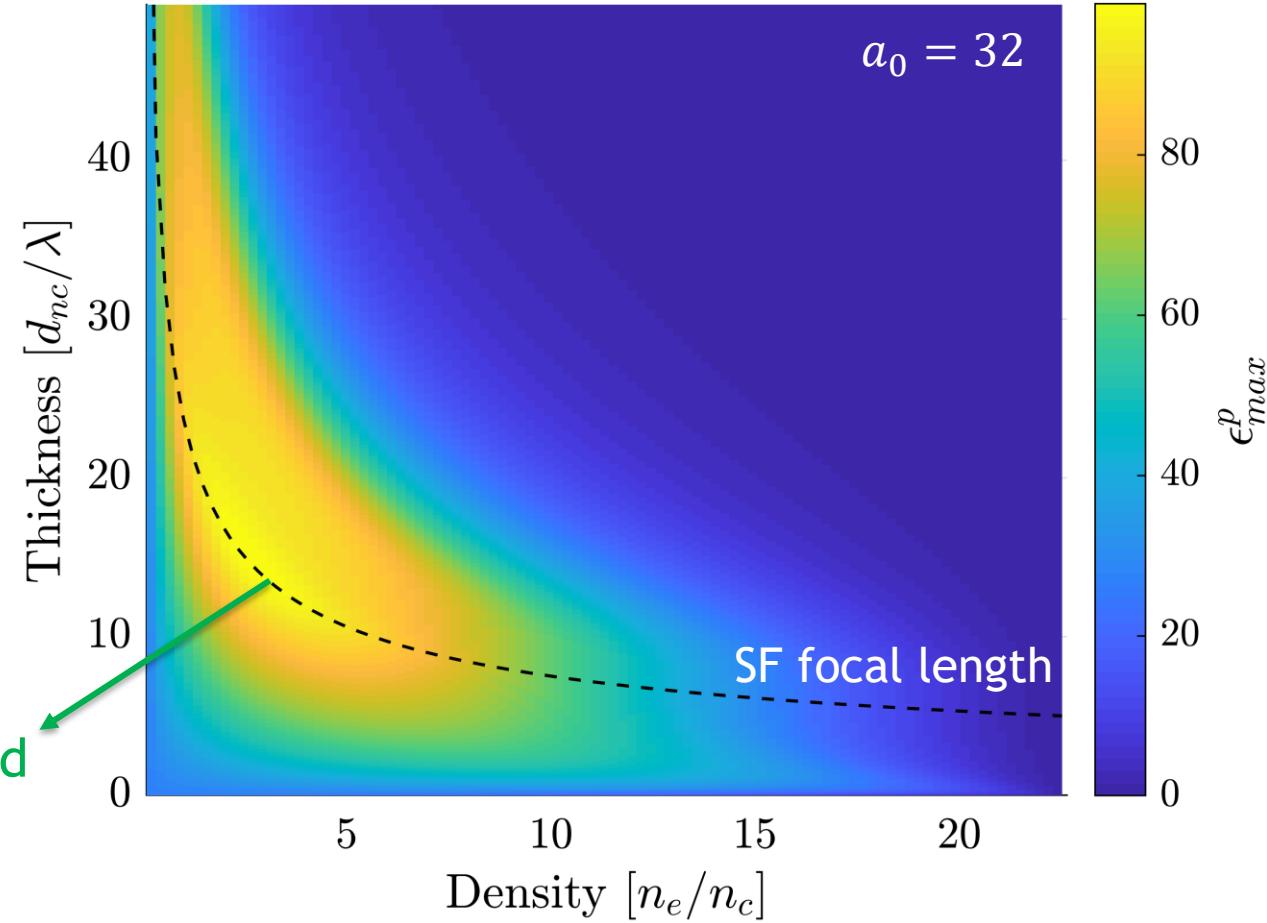
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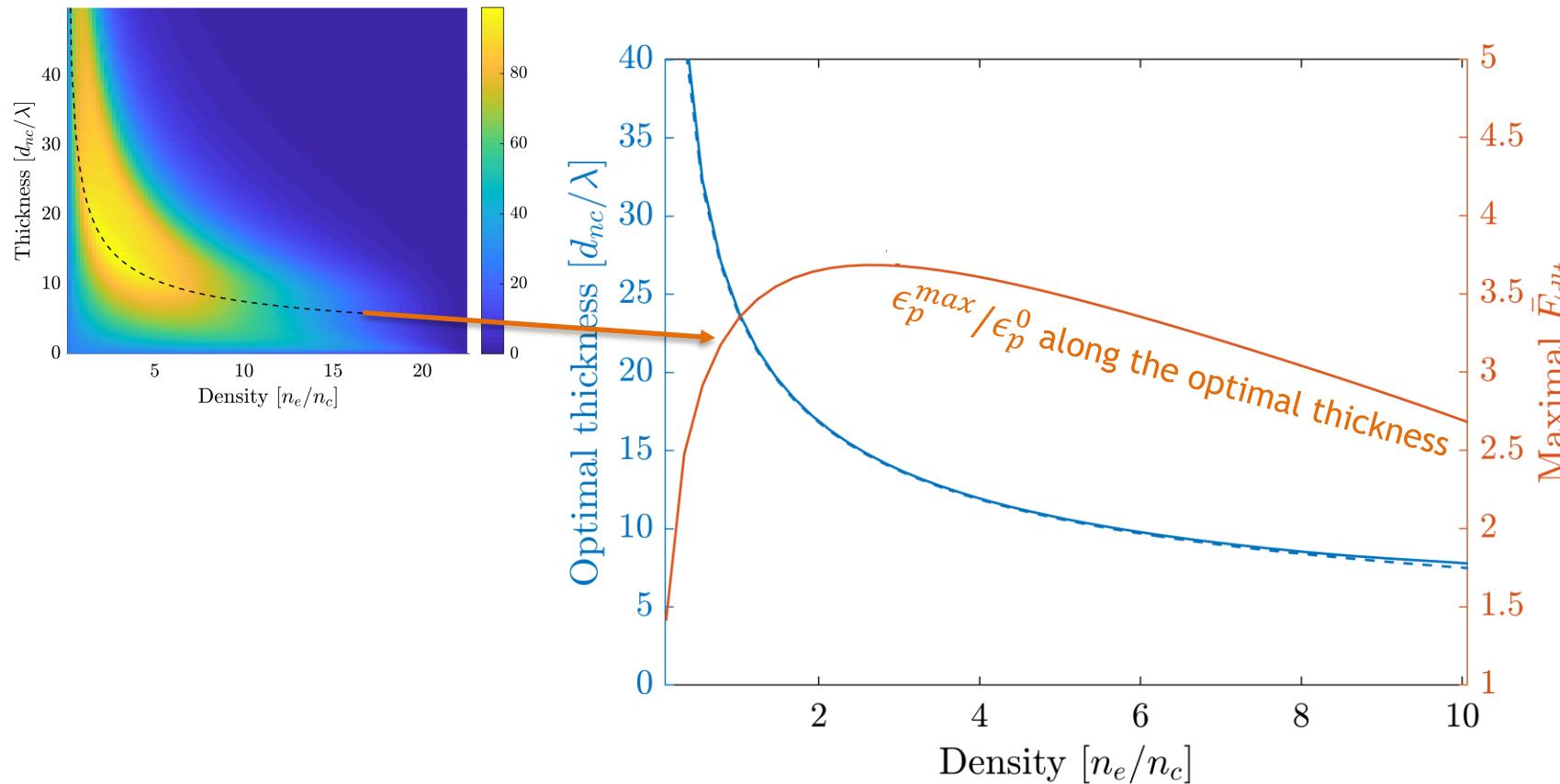
# Maximum proton energy heat map



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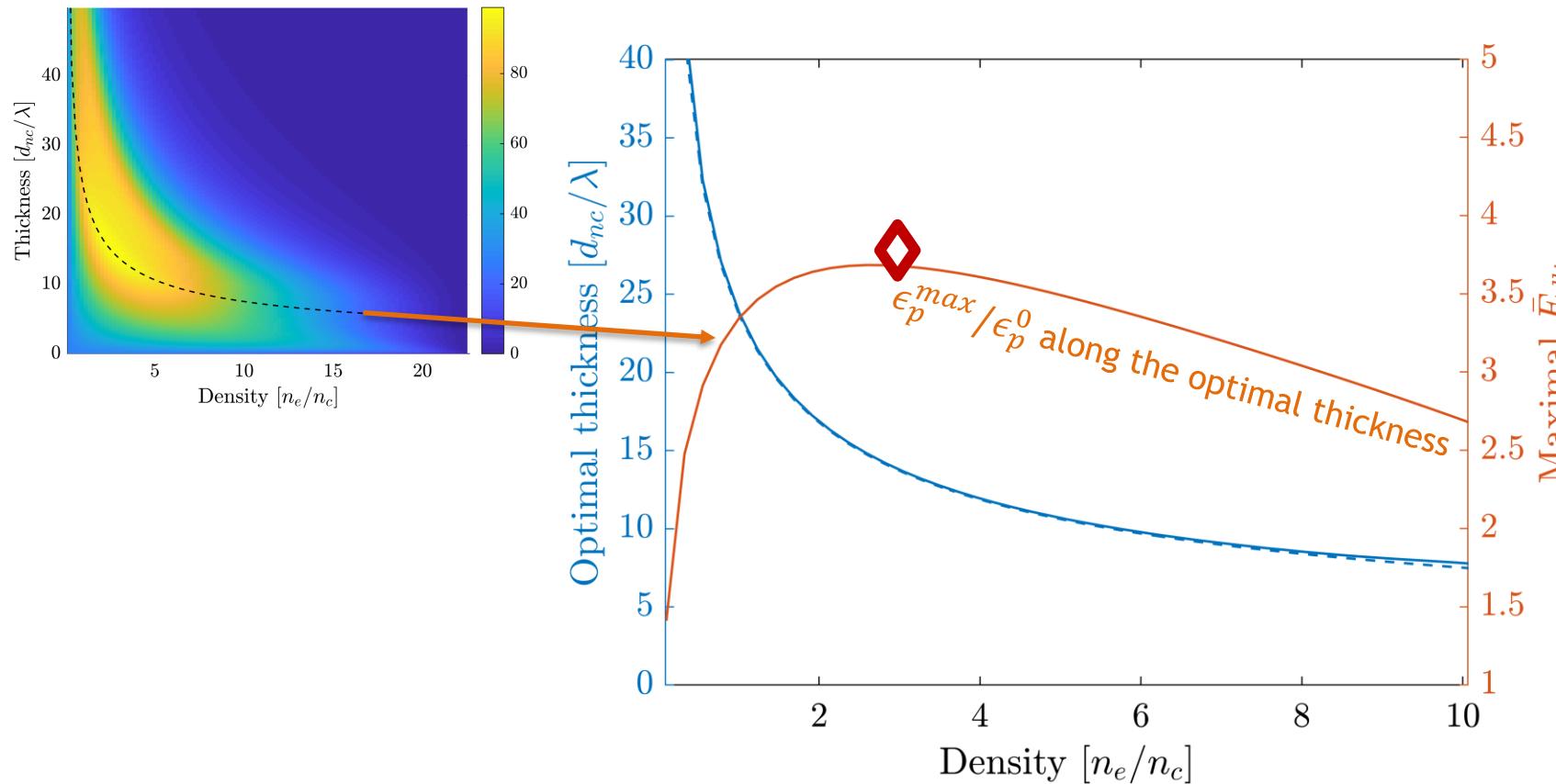


# Analytical solution in the ultra-relativistic case



Ultra-relativistic case  $\rightarrow a_0 \gg 1$

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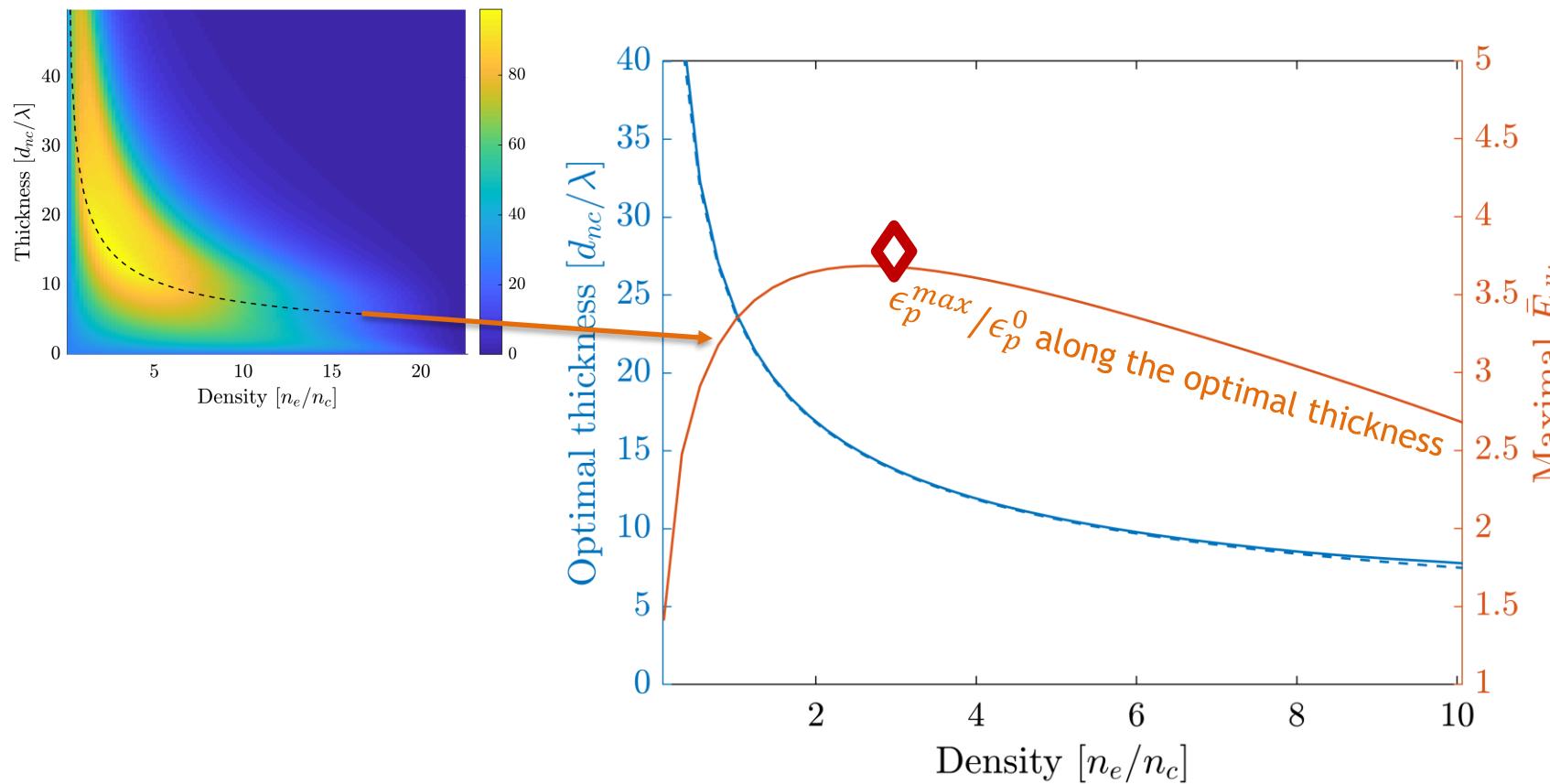
optimal density:

$$\bar{n}^{opt} = \frac{\lambda^2}{\pi w_0^2} \left( \frac{12\sqrt{2}\tau c/\lambda}{r_c^2 C_{nc}} \right)^{2/3}$$

Enhancement factor:

$$\bar{E}_{DLT}^{opt} = \frac{3C_{nc}}{4C_s} \left[ 1 - \frac{1}{\pi} \left( \frac{\sqrt{3}C_{nc}r_c^2}{2\tau c/\lambda} \right)^{2/3} \right]$$

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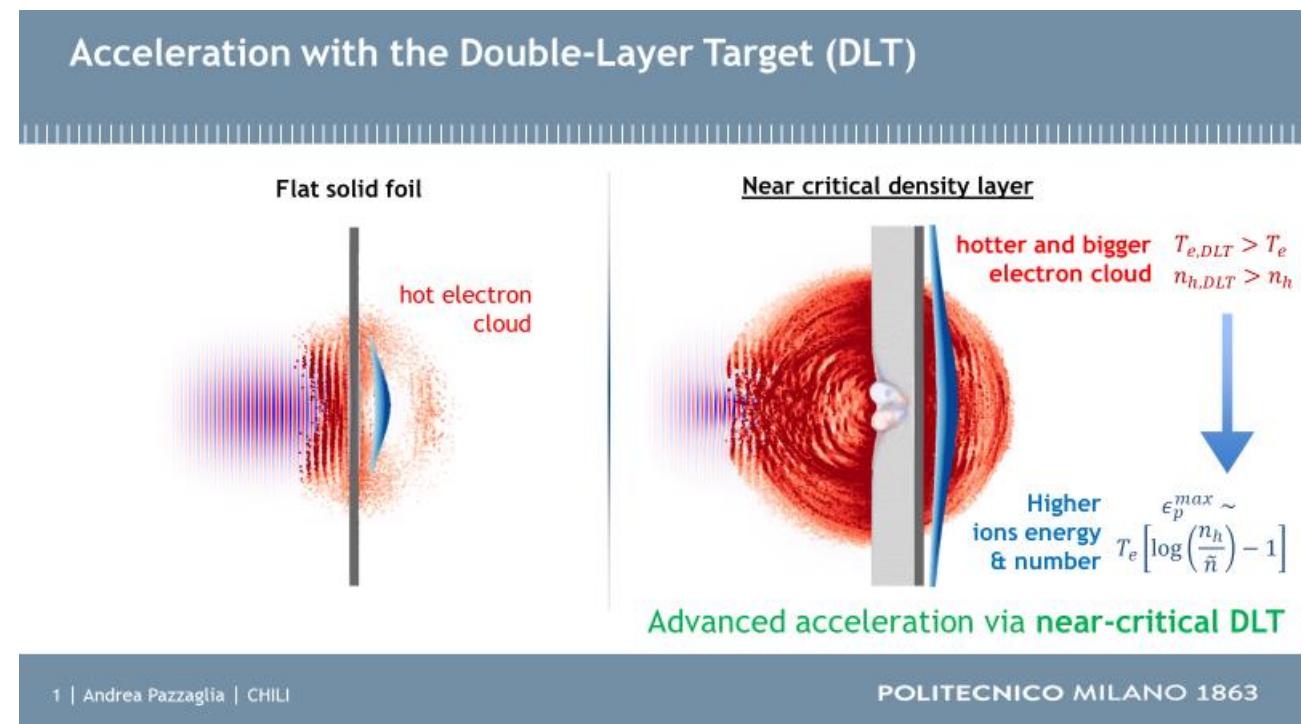
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enhancement factors higher than ones reported in the literature

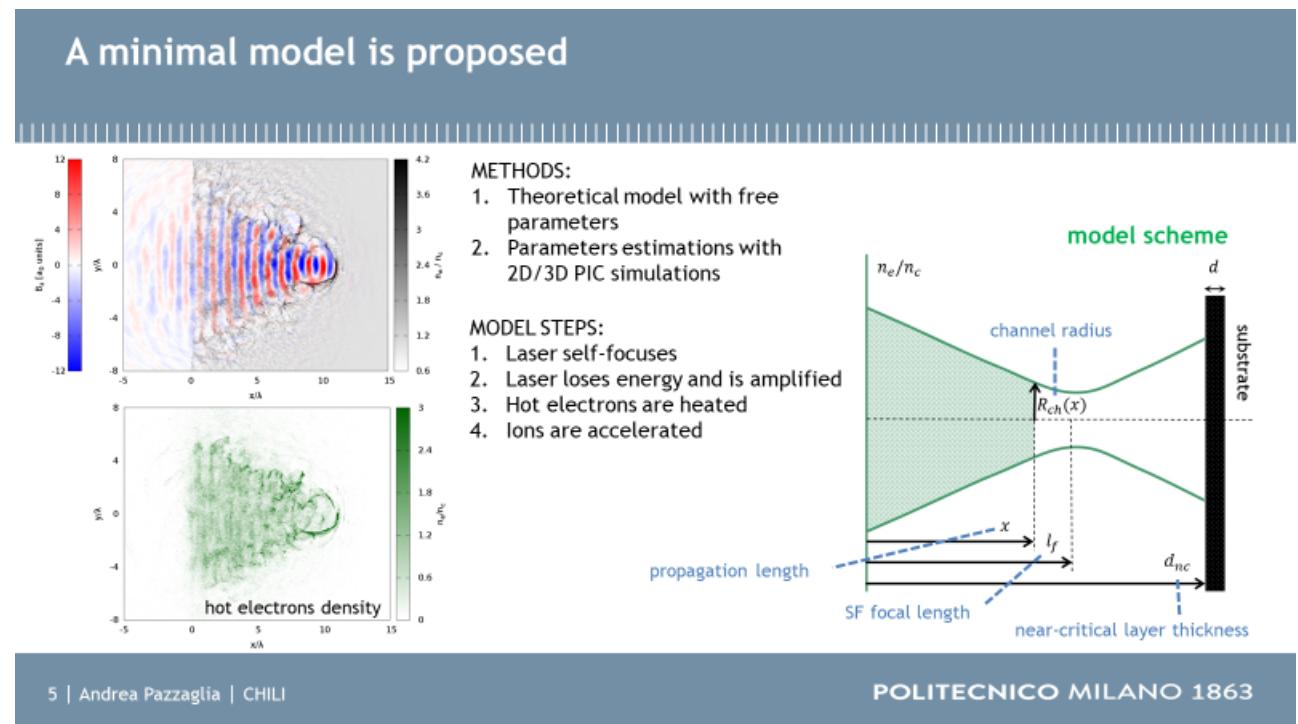
# Conclusions

- Advanced TNSA via near-critical double-layer target



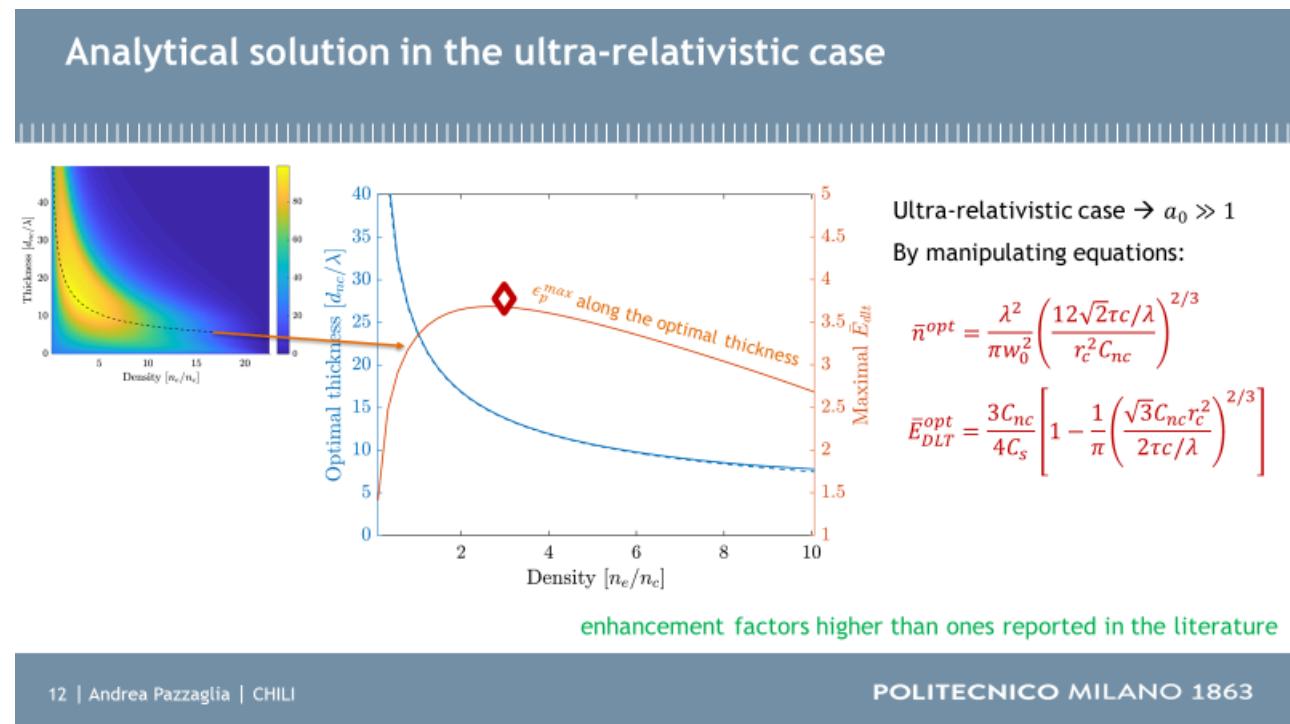
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- Modelization of proton acceleration with DLT



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- Advanced TNSA via near-critical double-layer target
- Modelization of proton acceleration with DLT
- Optimal DLT parameters



# Future perspectives

- Optimal DLT realization

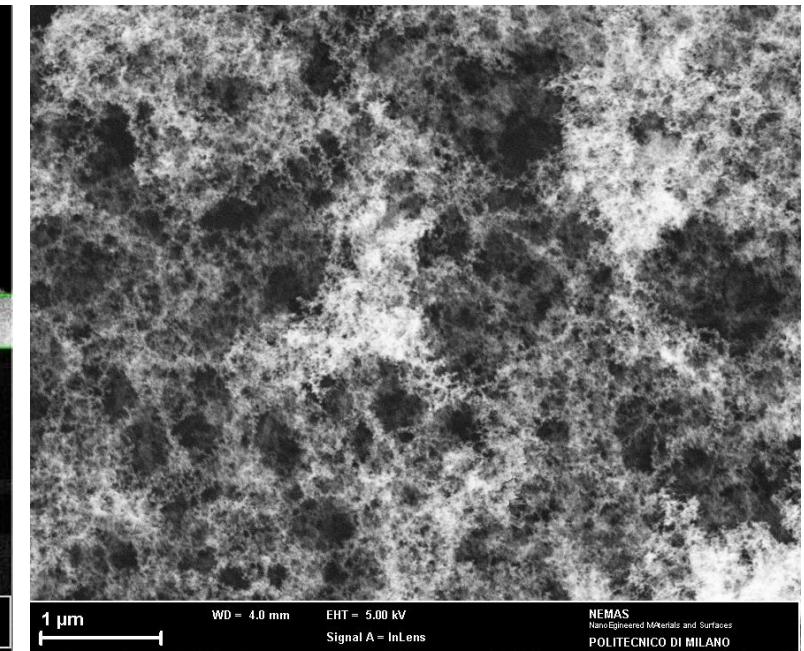
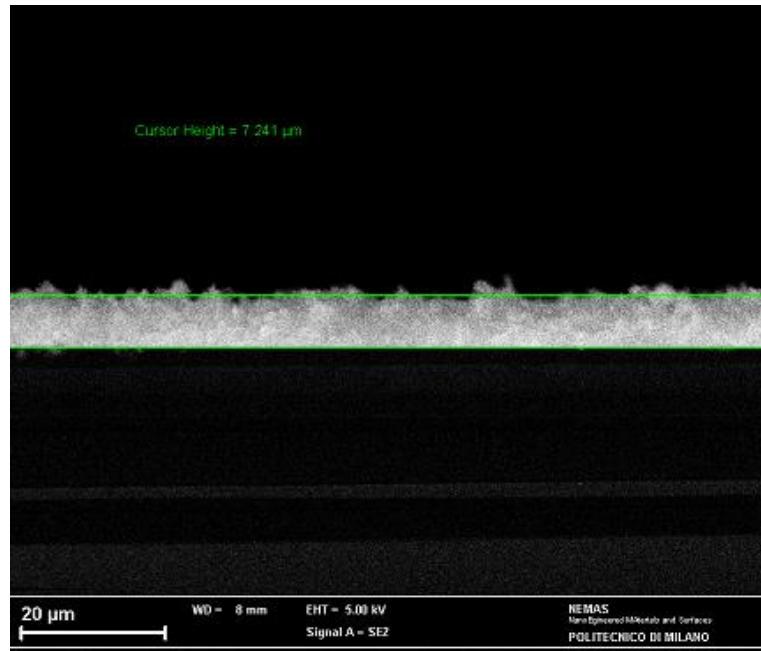
❖ Nanostructured near-critical layer

Zani, Alessandro, et al. *Carbon* 56 (2013): 358-365.

Maffini, A., et al. *Physical Review Materials* 3.8 (2019): 083404.

Passoni, Matteo, et al. *Plasma Physics and Controlled Fusion* (2019).

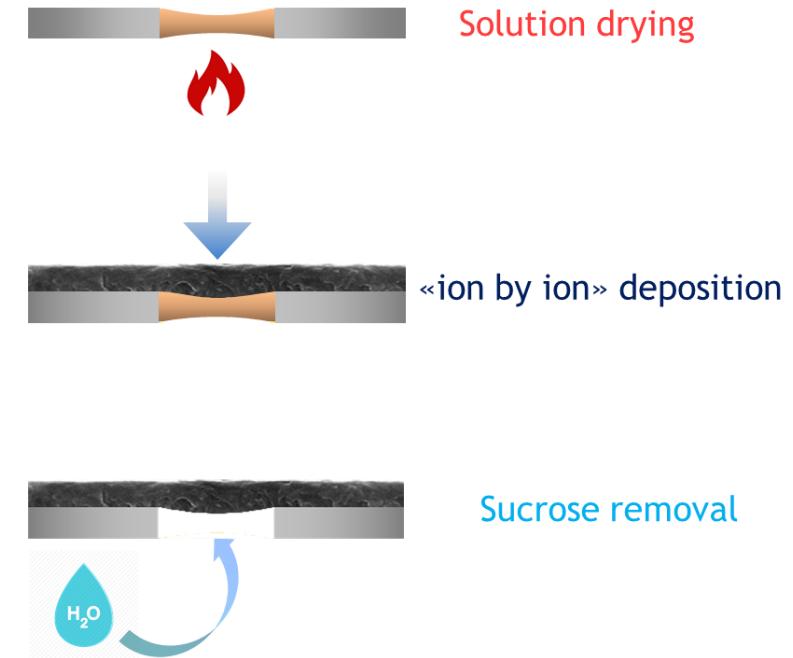
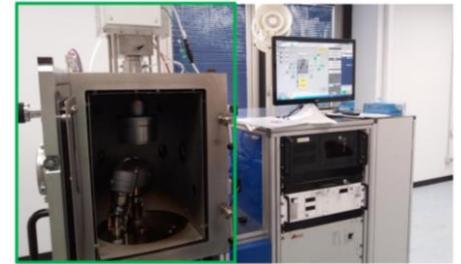
Produced by ns-PLD and fs-PLD



# Future perspectives

- Optimal DLT realization
  - ❖ Nanostructured near-critical layer
  - ❖ Substrate production

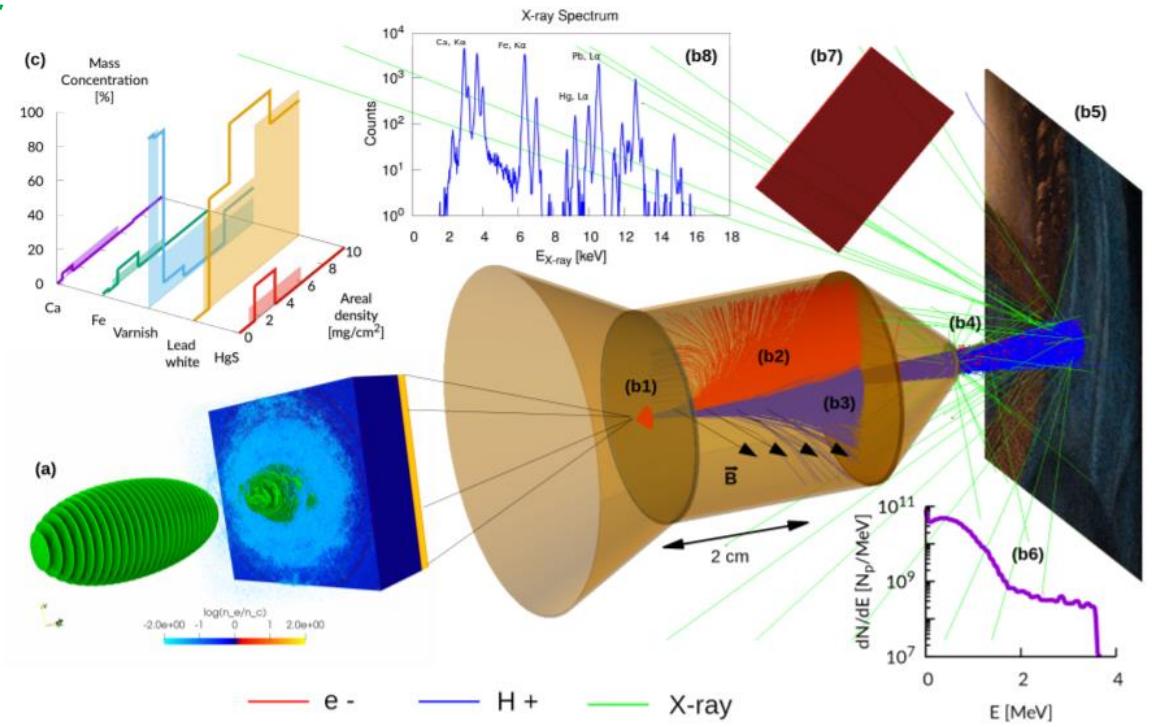
High Power Impulse  
Magnetron Sputtering  
(HiPIMS)



# Future perspectives

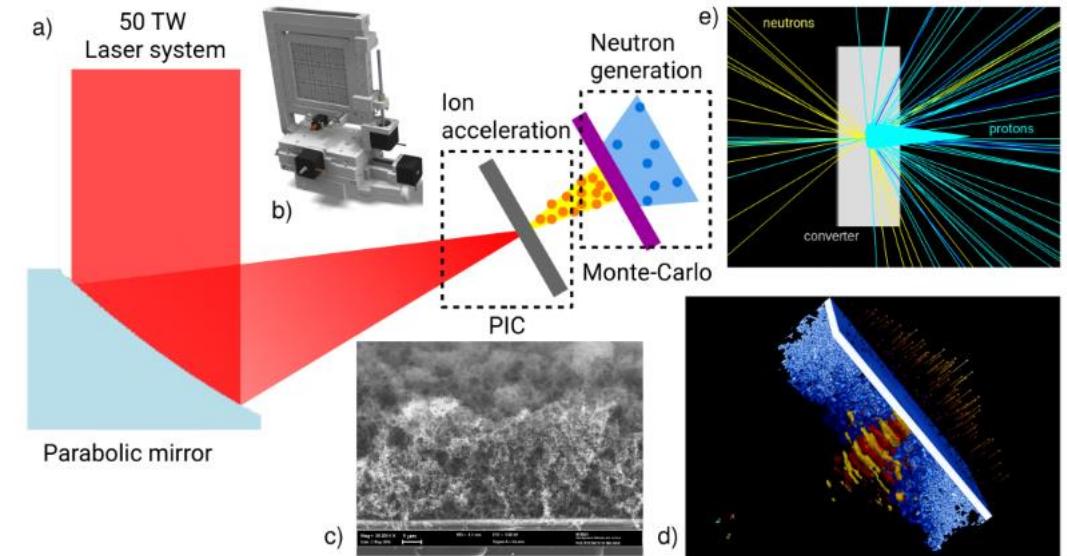
- Optimal DLT realization
  - ❖ Nanostructured near-critical layer
  - ❖ Substrate production
- Applications
  - ❖ Ion Beam Analysis

Passoni M., Fedeli L and Mirani F. Superintense Laser-driven Ion Beam Analysis (2019). *Scientific Reports*



# Future perspectives

- Optimal DLT realization
  - ❖ Nanostructured near-critical layer
  - ❖ Substrate production
- Applications
  - ❖ Ion Beam Analysis
  - ❖ Neutron & Radioisotopes production



Fedeli L. et al. *New Journal of Physics* Under review

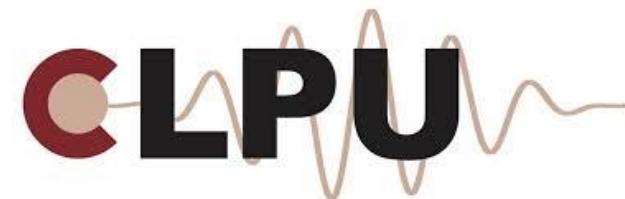
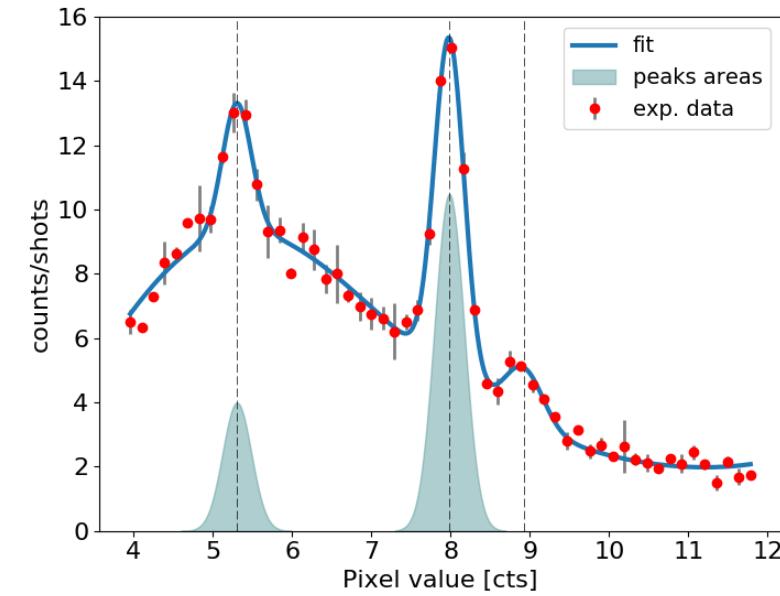
A. Tentori Master's thesis, Politecnico di Milano, Italy (2018)

F. Arioli Master's thesis, Politecnico di Milano, Italy (2019)

A. Giovannelli Master's thesis, Politecnico di Milano, Italy (2019)

# Future perspectives

- Optimal DLT realization
  - ❖ Nanostructured near-critical layer
  - ❖ Substrate production
- Applications
  - ❖ Ion Beam Analysis
  - ❖ Neutron & Radioisotopes production
  - ❖ Dedicated experiments



# Acknowledgments



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MILANO 1863



M. Passoni



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A. Maffini



L. Fedeli



A. Pola



A. Formenti

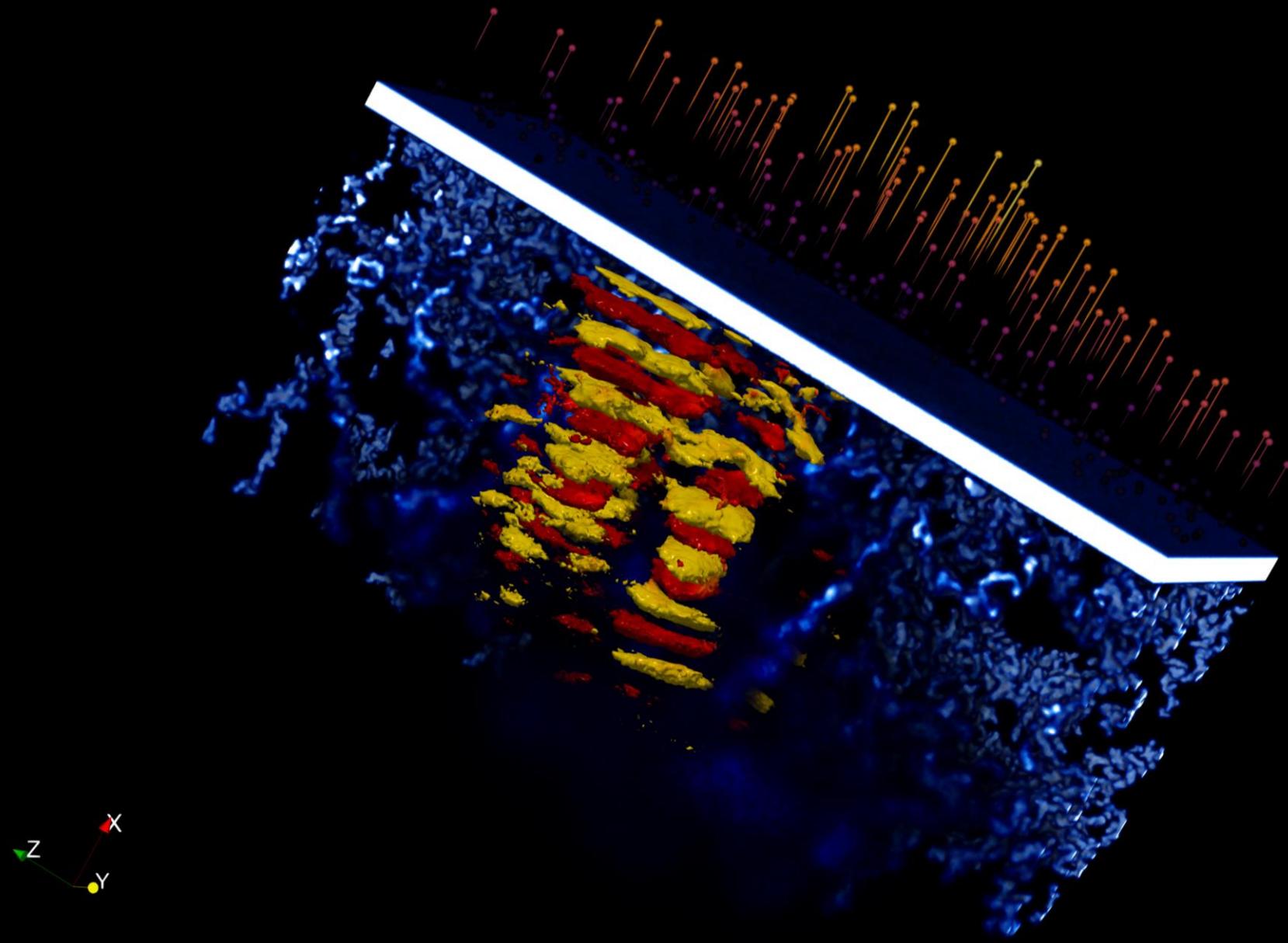


A. Pazzaglia



F. Mirani

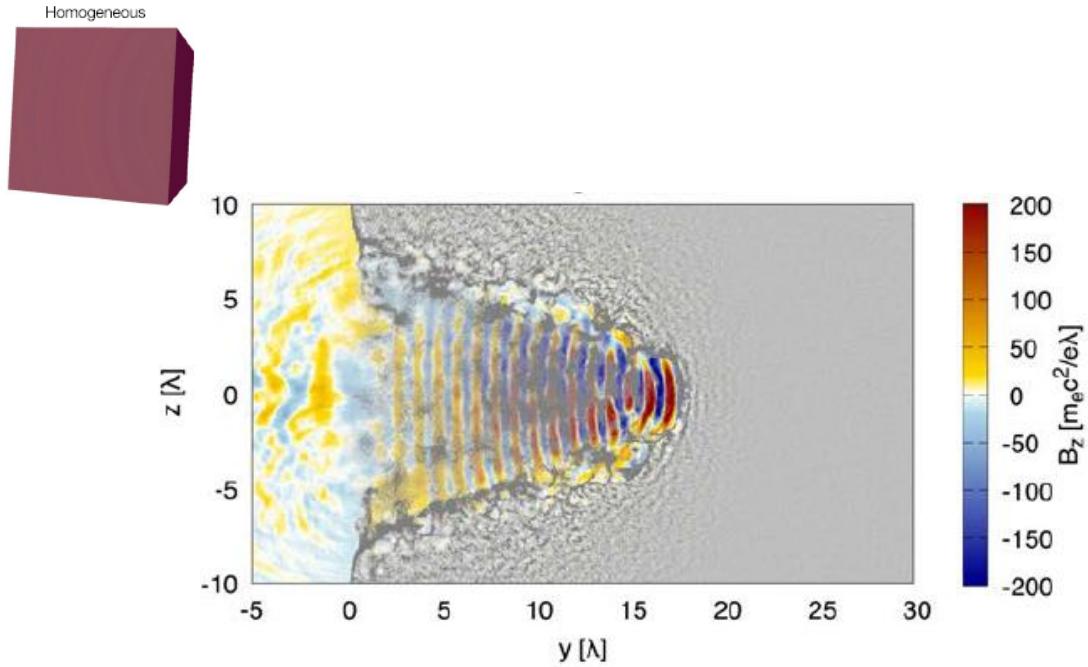




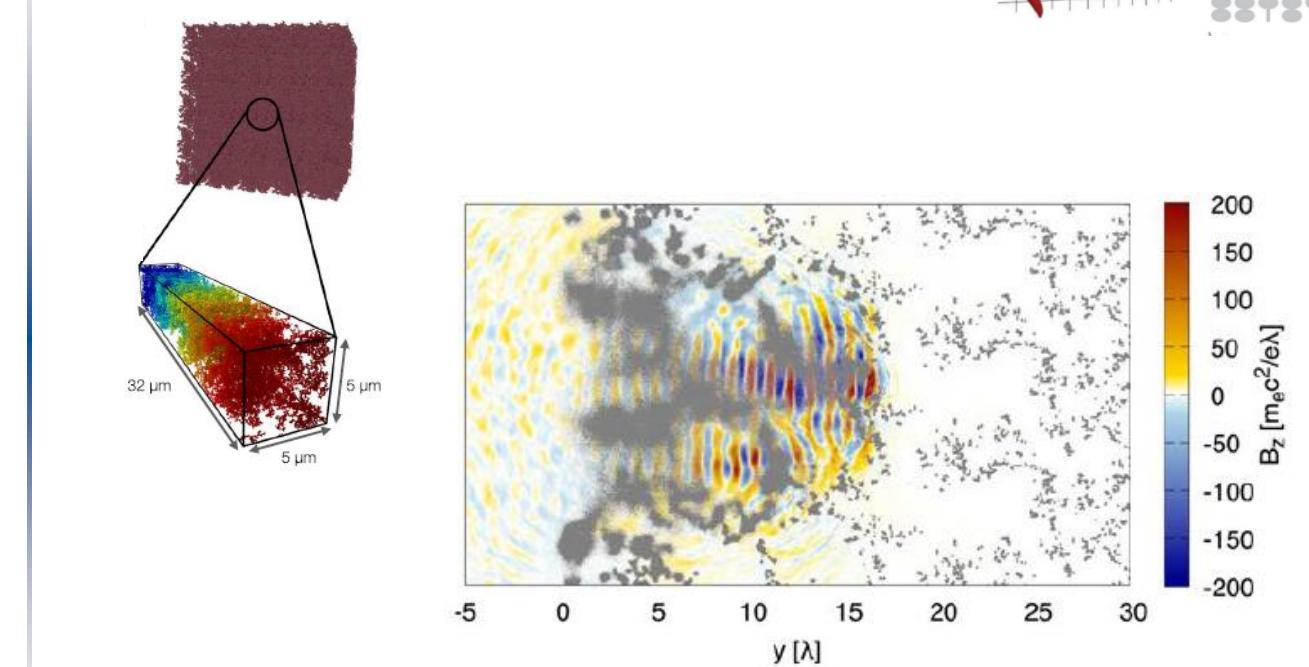
*...and thank you for your attention!!*

# Realistic near-critical layer effects

## Homogeneous near-critical plasma



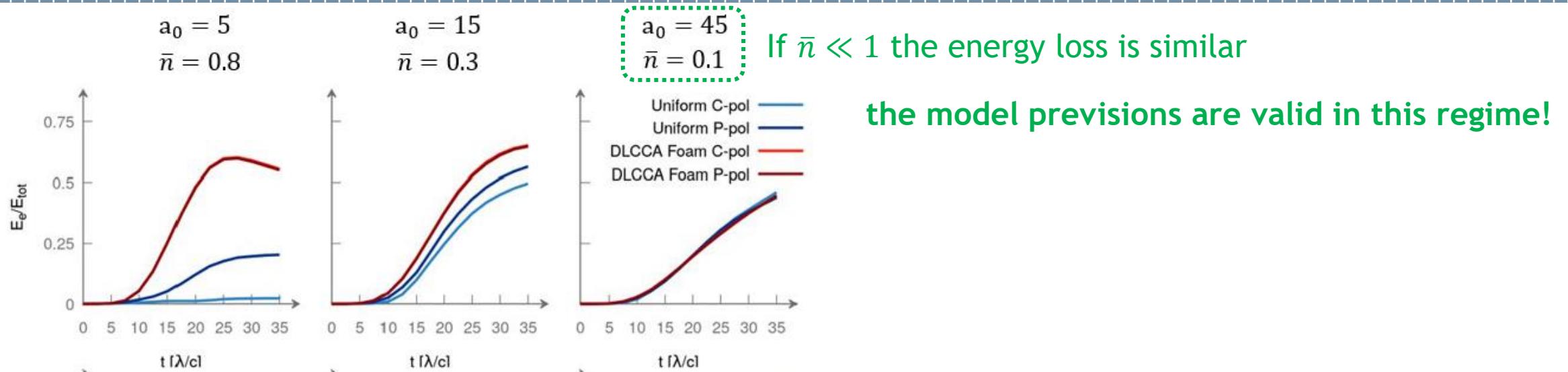
## Nanostructured near-critical plasma



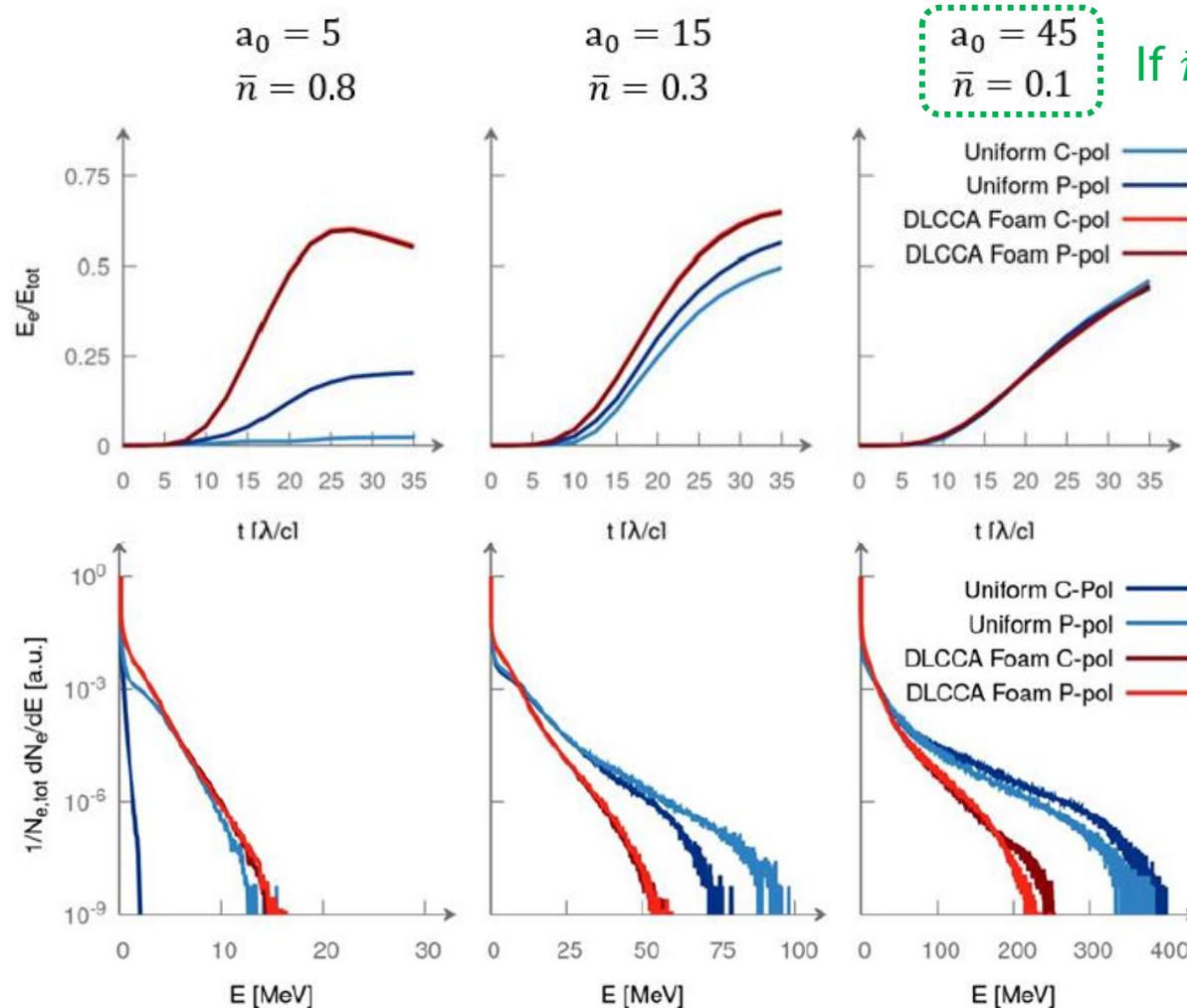
Fedeli, L., Formenti, A., Cialfi, L., Pazzaglia, A., & Passoni, M. (2018). Ultra-intense laser interaction with nanostructured near-critical plasmas. *Scientific reports*, 8(1), 3834.

3D PIC simulations show evident differences

# Differences in pulse energy loss and electron heating



# Differences in pulse energy loss and electron heating



If  $\bar{n} \ll 1$  the energy loss is similar

the model previsions are valid in this regime!

Nanostructured plasma:

- Electrons temperature ↓
- Electrons number ↑

$$\epsilon_p^{max} = T_{DLT} \left[ \log \left( \frac{n_{h,DLT}}{\tilde{n}} \right) - 1 \right]$$

lower energy expected  
uniform near-critical plasma are optimal