



POLITECNICO
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Numerical simulations of nanostructured plasmas

Luca Fedeli



Chalmers University, 05/10/2016

The group at Politecnico di Milano



The group at Politecnico di Milano

Matteo Passoni
Associate professor



Numerical team

Luca Fedeli
Post-doc

Lorenzo Cialfi
PhD student

Arianna Formenti
PhD student



Material science/targetry team

Valeria Russo
Researcher

David Dellasega
Post-doc

Alessandro Maffini **Andrea Pazzaglia**
Post-doc PhD student

Margherita Zavelani Rossi
Associate professor



The group at Politecnico di Milano



Research interests

Laser-driven **ion acceleration**

Applications of laser-driven ions in **material science**

Secondary sources
(e.g. laser-driven **neutron sources**)

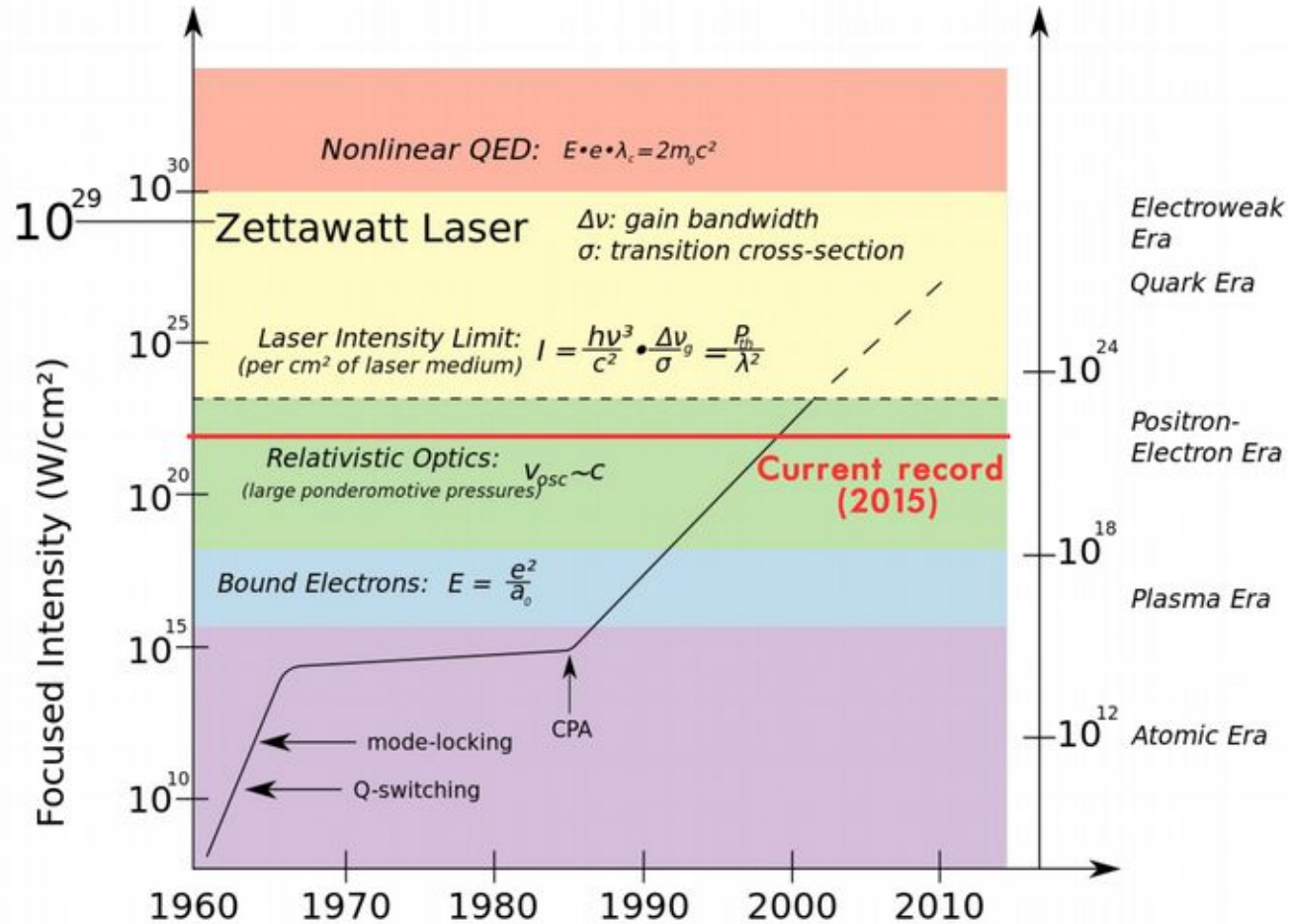
Advanced targets for laser-plasma experiments
(near-critical foams)



Nanostructured plasmas



Ultra-intense, ultra-short, ultra-high contrast lasers



**Ultra-short (10s fs),
ultra-intense (up to
 $\sim 10^{22}$ W/cm²) laser
systems**

**Ti:sapphire-based:
 $\lambda \sim 800$ nm**

**Very high temporal
contrast, even 10^{10}
@ps timescale**



Nanostructured plasmas

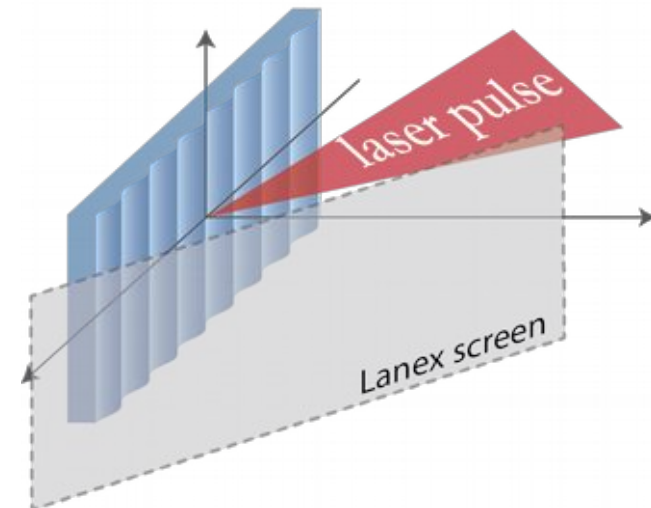
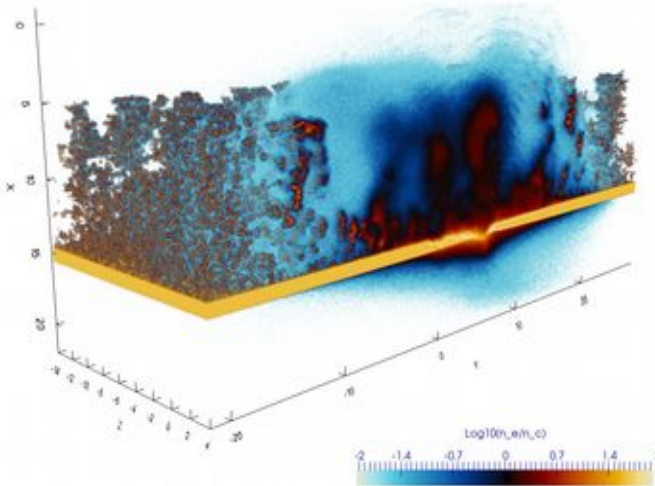


Nanostructured plasmas

If we irradiate a solid, nanostructured, target with these lasers, **the structures might survive**

In some cases this is **incidental**

In other cases it is **desirable**

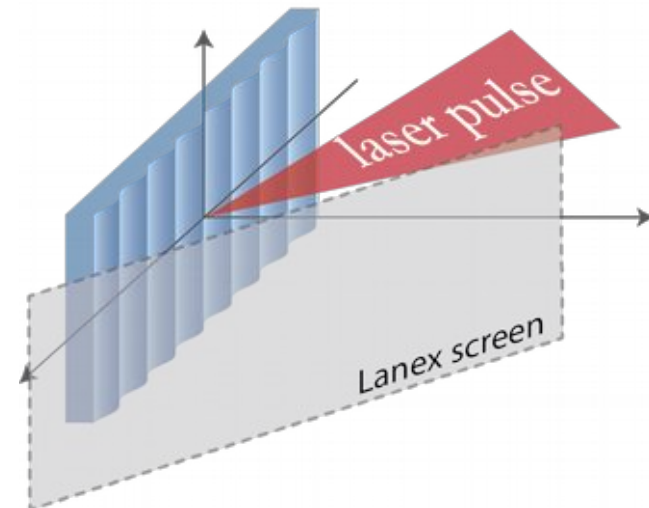
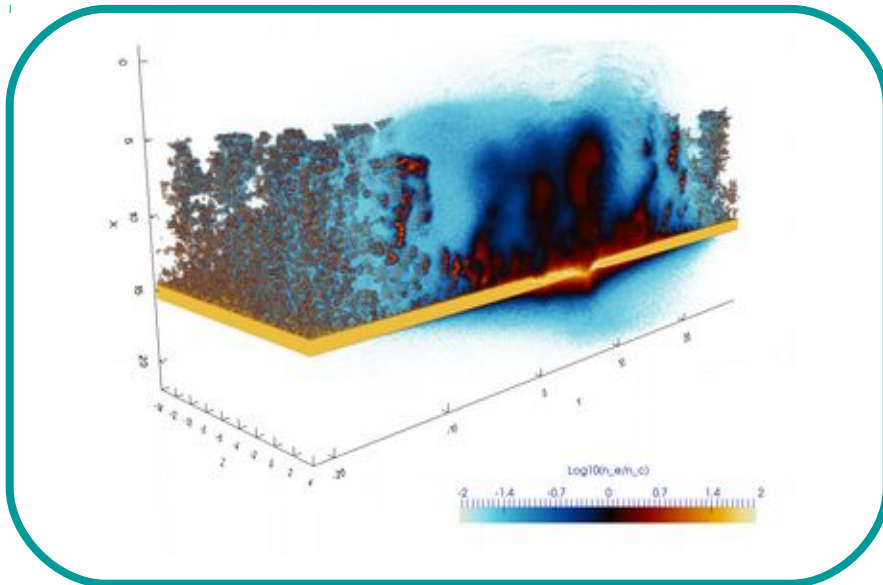


Nanostructured plasmas

If we irradiate a solid, nanostructured, target with these lasers, **the structures might survive**

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Nanostructured near-critical density plasmas

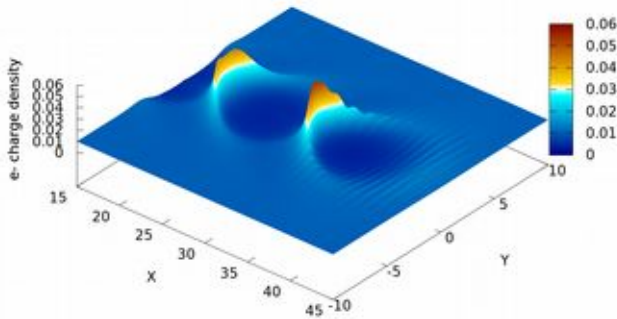
Why bother with low density porous materials?

Essentially because we care about laser-interaction with **near-critical plasmas**

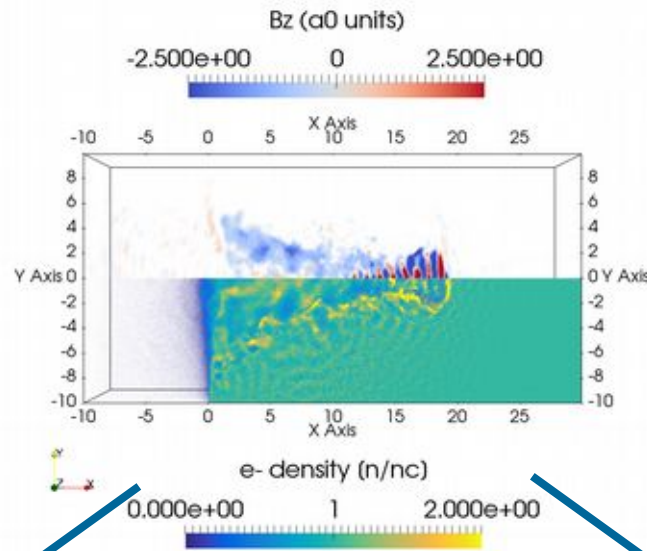


Near-critical plasmas

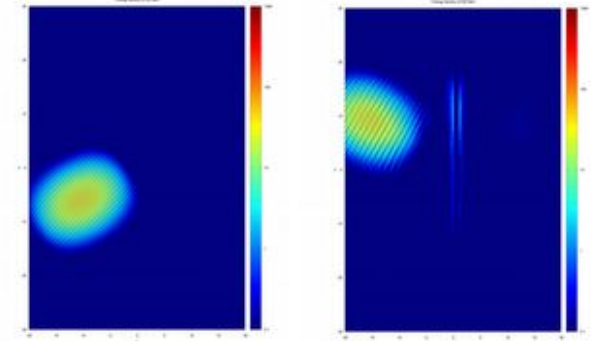
$$n \ll n_c / \langle \gamma \rangle$$



$$n \sim n_c / \langle \gamma \rangle$$



$$n \gg n_c / \langle \gamma \rangle$$



$$n_c = \frac{\pi m_e c^2}{e^2 \lambda^2}$$

$$\langle \gamma \rangle = \sqrt{1 + a_0^2 / 2}$$

$$a_0 = \frac{e E_0}{m_e \omega c}$$

**Near-critical
plasmas**

Collisionless
shocks

Synchrotron
emission

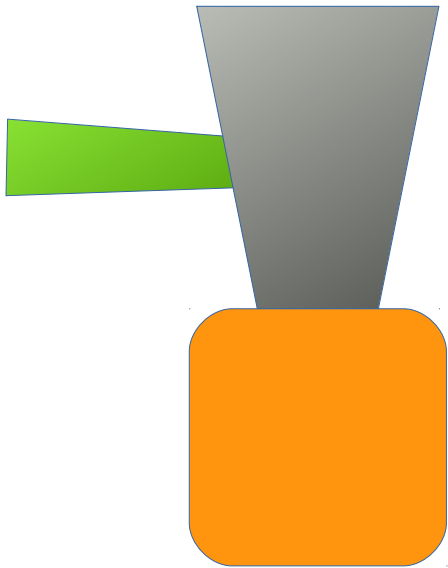
Laser-driven ion
acceleration



Near-critical plasmas

We don't really have many strategies
to explore that density range
 $1 n_c$ means few mg/cm^3 !

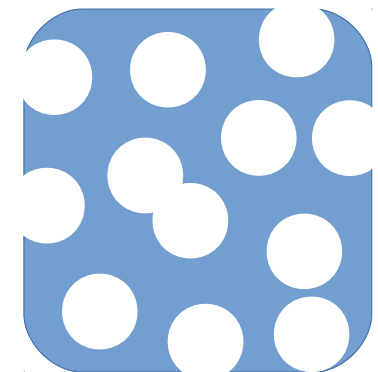
High-density
gas-jets



Pre-heating



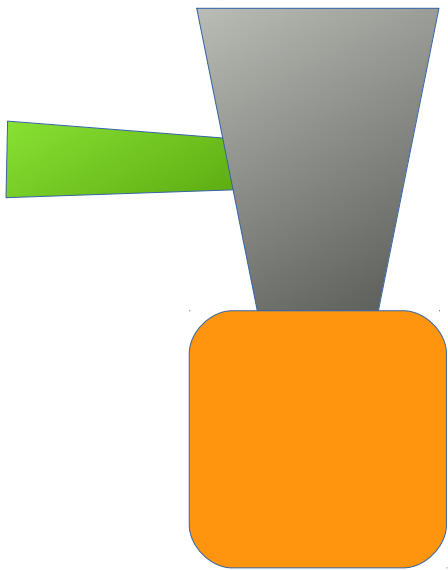
Low-density
porous
materials



Near-critical plasmas

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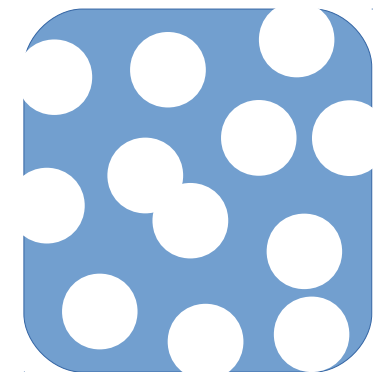
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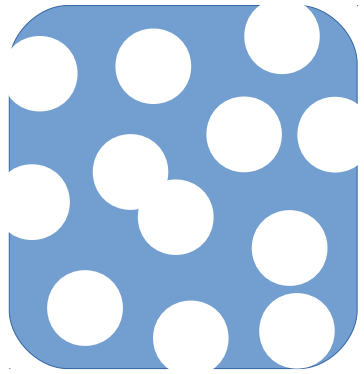
Pre-heating



Low-density
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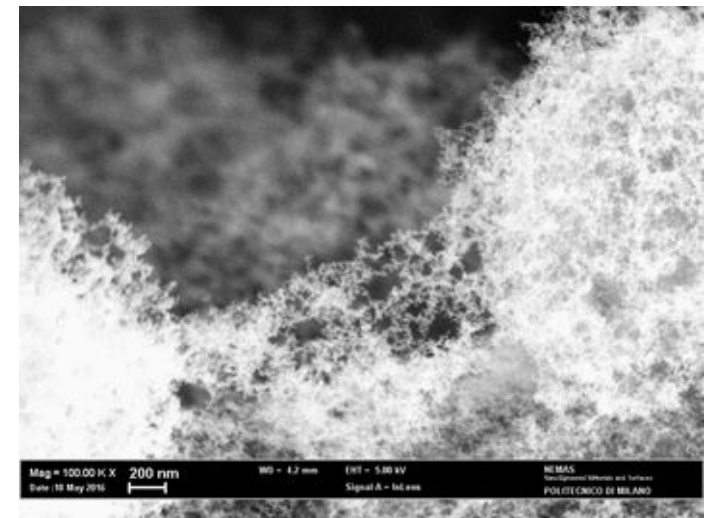
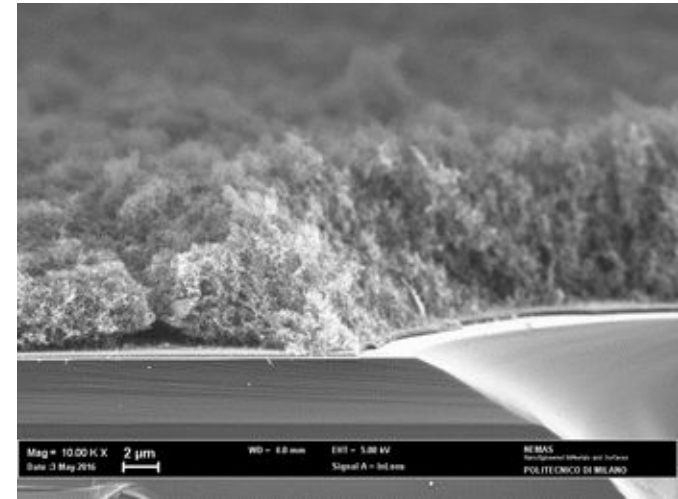
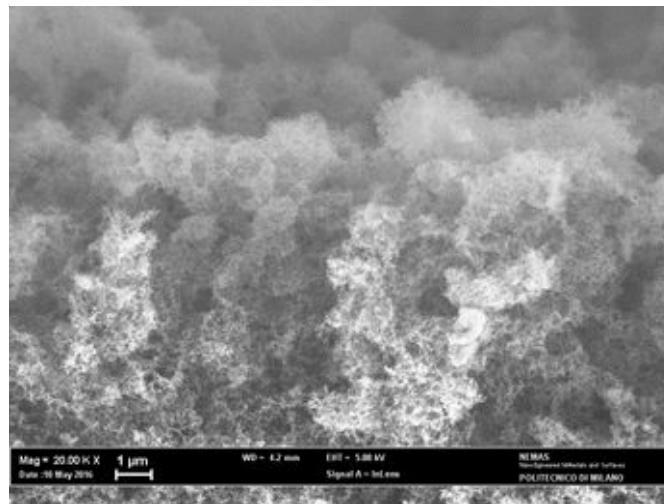
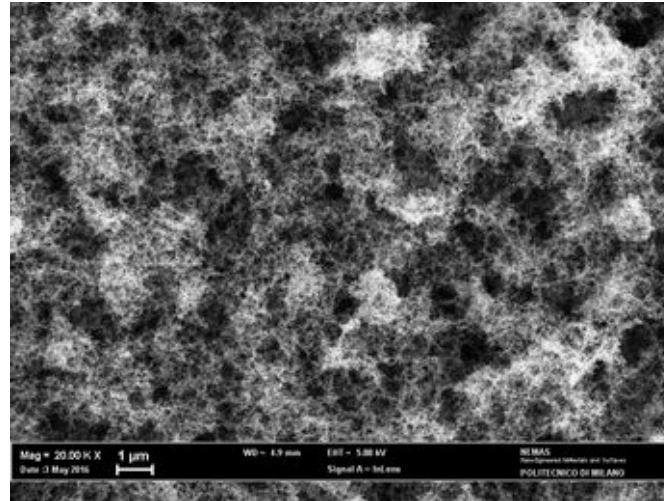


Near-critical plasmas



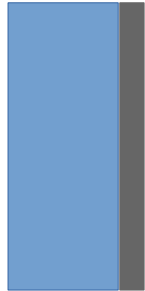
Low-density
carbon
foam

Tunable
density,
down to \sim
 $1n_c$ (fully
ionized)



Zani et al. Carbon 56 (2013)

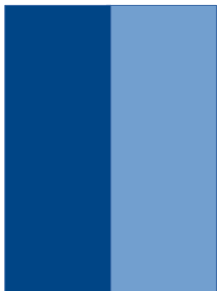
Near-critical plasmas



Can be
attached onto a
solid foil



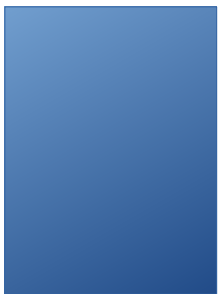
Proven.
Thickness range:
 $\sim 4\text{-}60\ \mu\text{m}$



Abrupt density
change (but still
low density)



Proven.
But, better control
is needed



Density
gradient



Proven.
But, challenging to
control



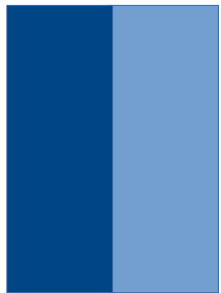
Near-critical plasmas



Can be
attached onto a
solid foil



A lot of “freedom” in
target design
(e.g. density tailored for
Magnetic Vortex
acceleration, Collisionless
Shocks generation...)



Abrupt density
change (but still
low density)



Density
gradient



Experiments with foam-attached targets



I.Prencipe et al., PPCF 58 (2016)
M.Passoni et al., PRAB 19(2016)



Experiments with foam-attached targets



In 2014/2015 we performed experiments with foam-attached targets

Gwangju PW-class laser facility

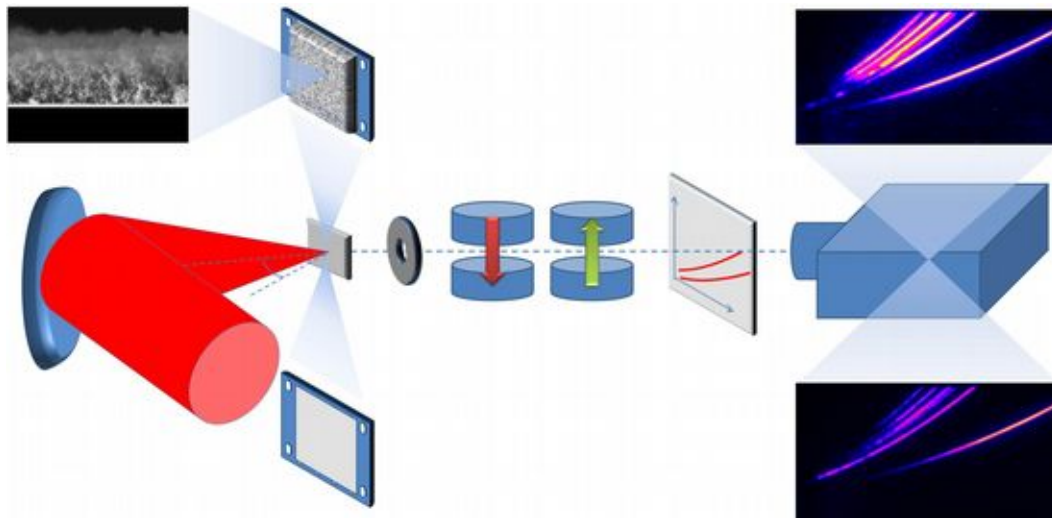
Aim: enhancing laser-driven ion acceleration with better laser-target coupling



I.Prencipe et al., PPCF 58 (2016)
M.Passoni et al., PRAB 19(2016)



Experiments with foam-attached targets



Up to 5×10^{20} W/cm²
 30 fs, 30° pulse incidence
 C-, P-, S- polarization

Thomson Parabole to look
 at ion spectra



Targets made of **0.75 μm Al +**
0-36 μm Carb. foam (~ 1 n_c)

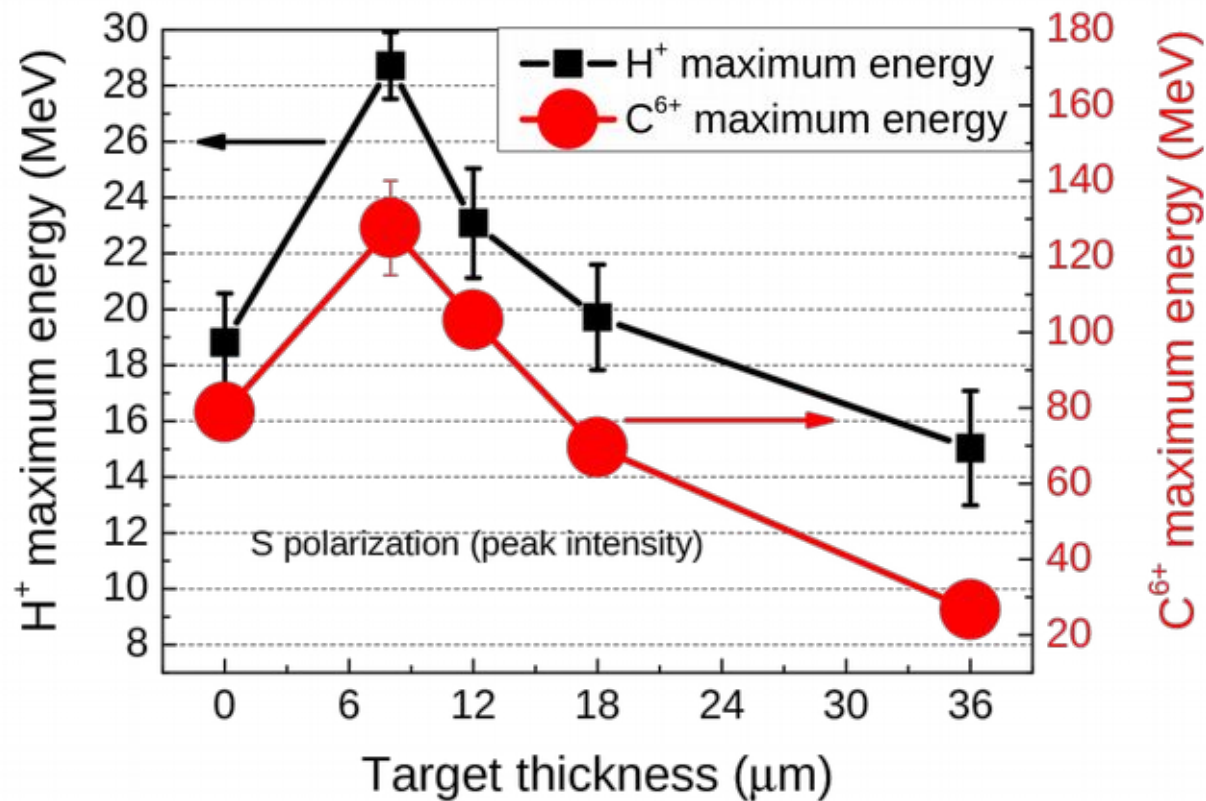


I. Prencipe et al., PPCF 58 (2016)

M. Passoni et al., PRAB 19(2016)

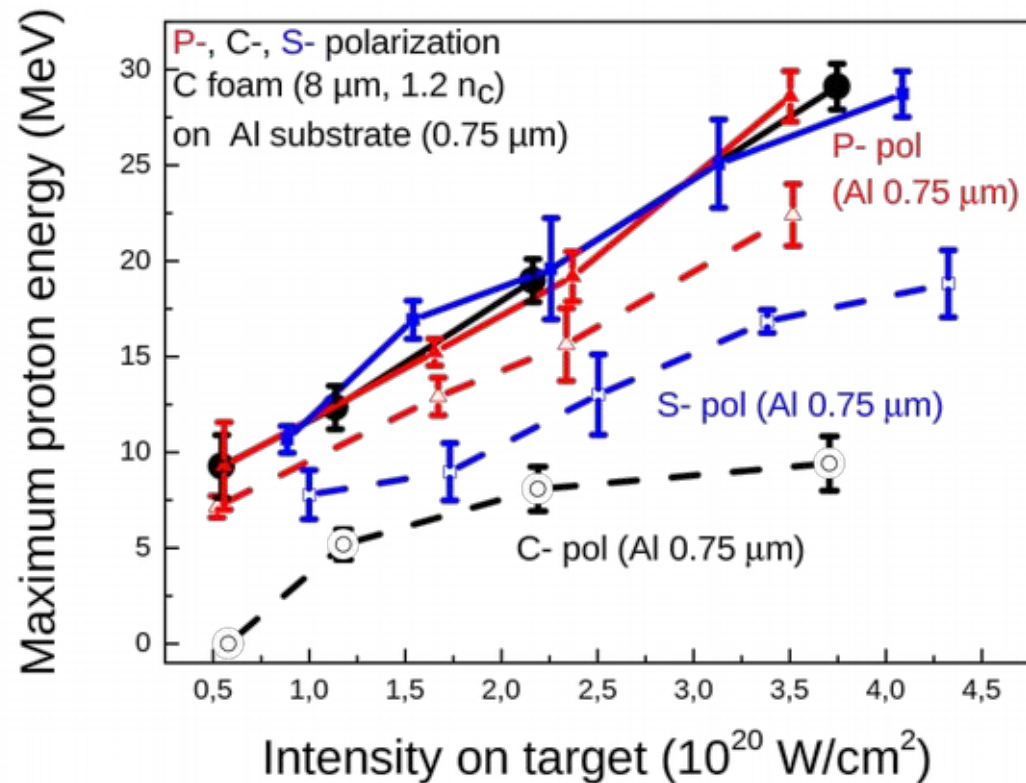


Experiments with foam-attached targets



Optimal foam thickness

Experiments with foam-attached targets



With foam no effects of pulse polarization

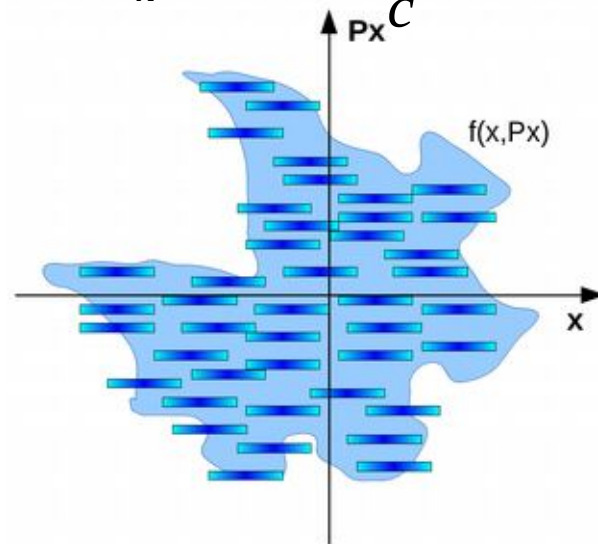
How do we simulate these plasmas?



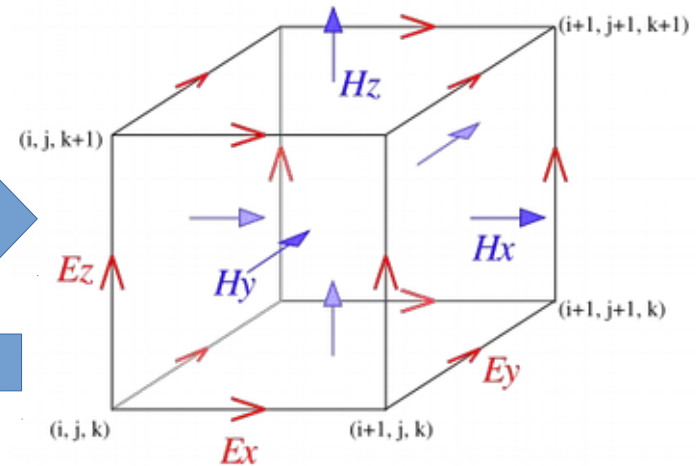
How do we simulate these plasmas?

Particle-In-Cell codes

$$\partial_t f + \mathbf{v} \cdot \nabla_x f + q \left(\vec{E} + \frac{\mathbf{v}}{c} \times \mathbf{B} \right) \cdot \nabla_p f = 0$$



Maxwell's equations



$$f(\mathbf{x}, \mathbf{p}, t) \approx \sum_i S(\mathbf{x} - \mathbf{x}_i(t)) \delta(\mathbf{p} - \mathbf{p}_i(t))$$

We need to simulate these **complex structures** in Particle-In-Cell (**PIC**) codes



How do we simulate these plasmas?

We've used and we'll use foam-attached targets in forthcoming experiments

We need **numerical support**

How do we model these structures?

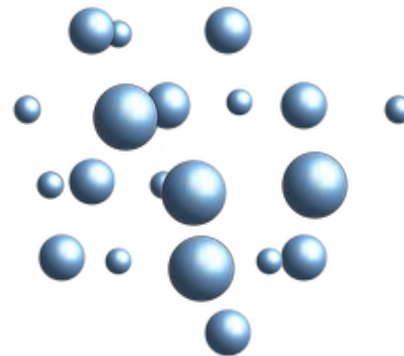


Models

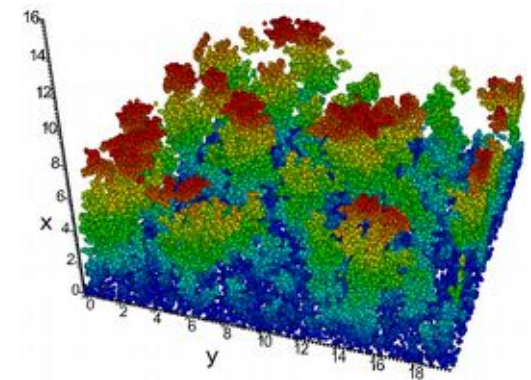
Uniform plasmas



Idealized model



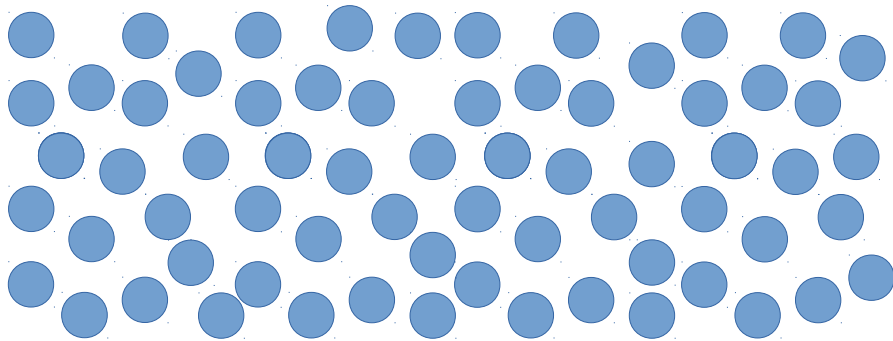
More realistic model



Simplified models



Instead of using a **uniform plasma** (as typically done in the literature)

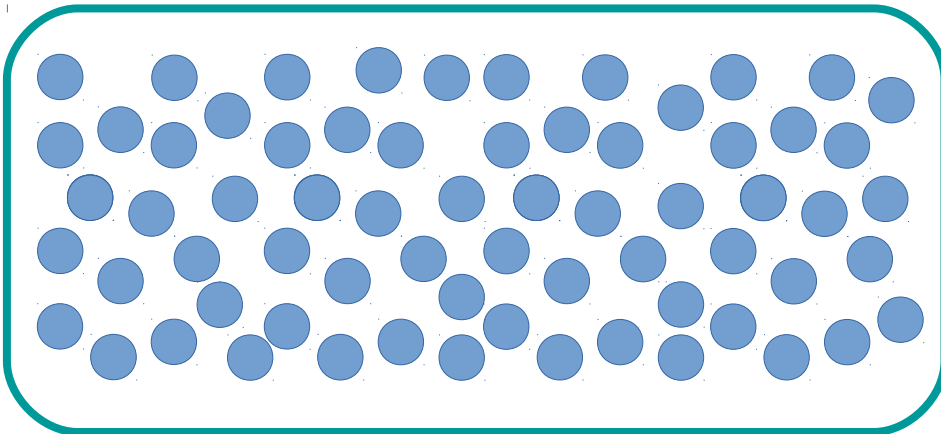


We can try to use a “**random balls**” model

A.Sgattoni et al. PRE 85 (2012) S.Okihara et al. PRE 69 (2004)



Simplified models



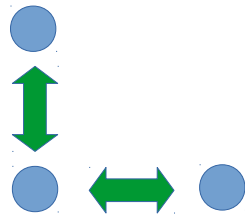
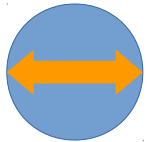
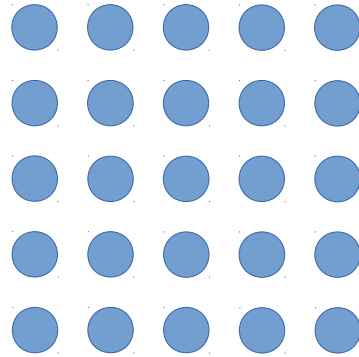
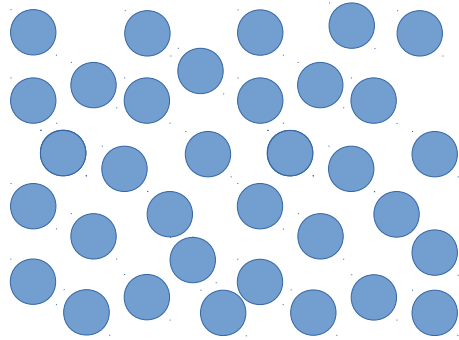
Very crude model

No μm -scale
structure

Spheres are not
connected



Simplified models



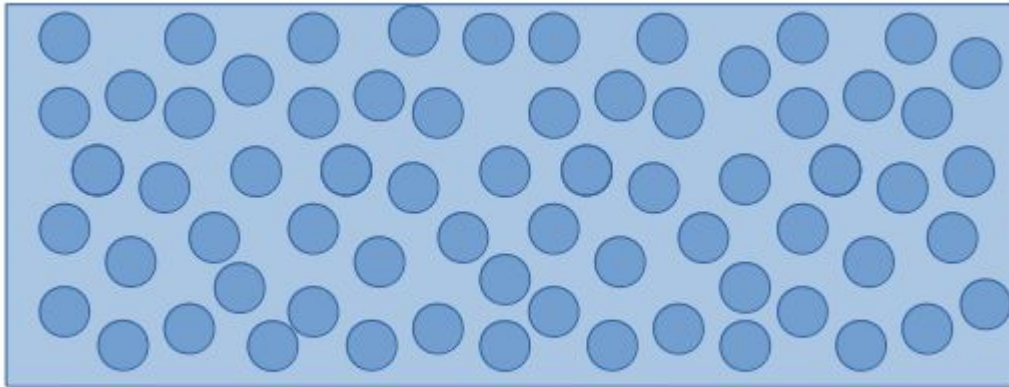
Few parameters to play with

Ordered vs Disordered

Radius and average distance



Simplified models



We can even mix a uniform plasma with a random balls plasma

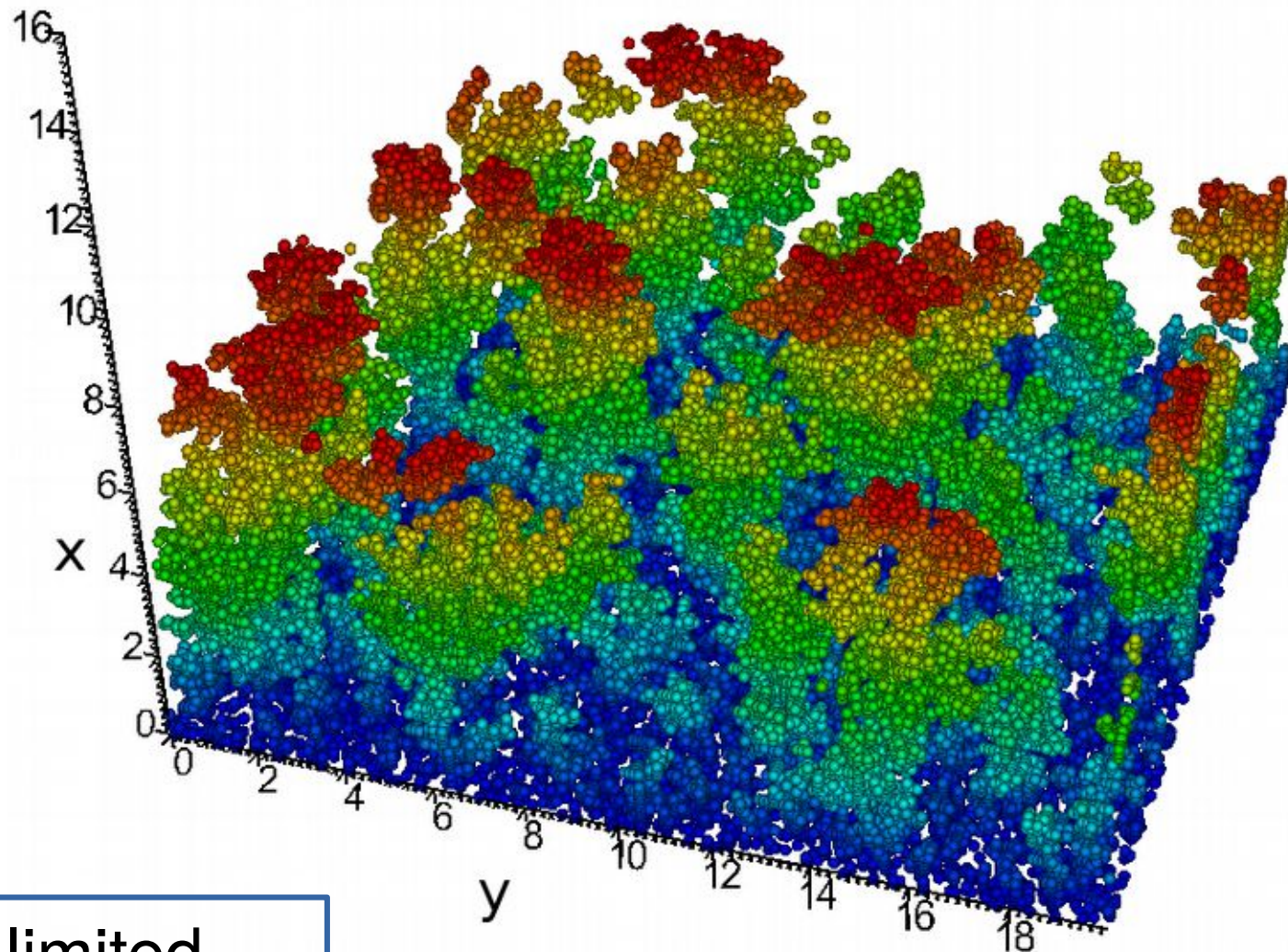
Might simulate partial pre-heating



More realistic models



More realistic models



Diffusion limited
aggregation model

T.A. Witten & L.M. Sanders PRL 47 (1981)

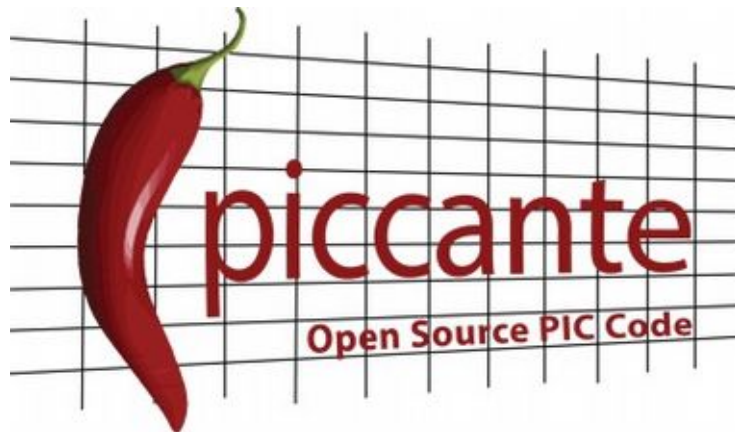
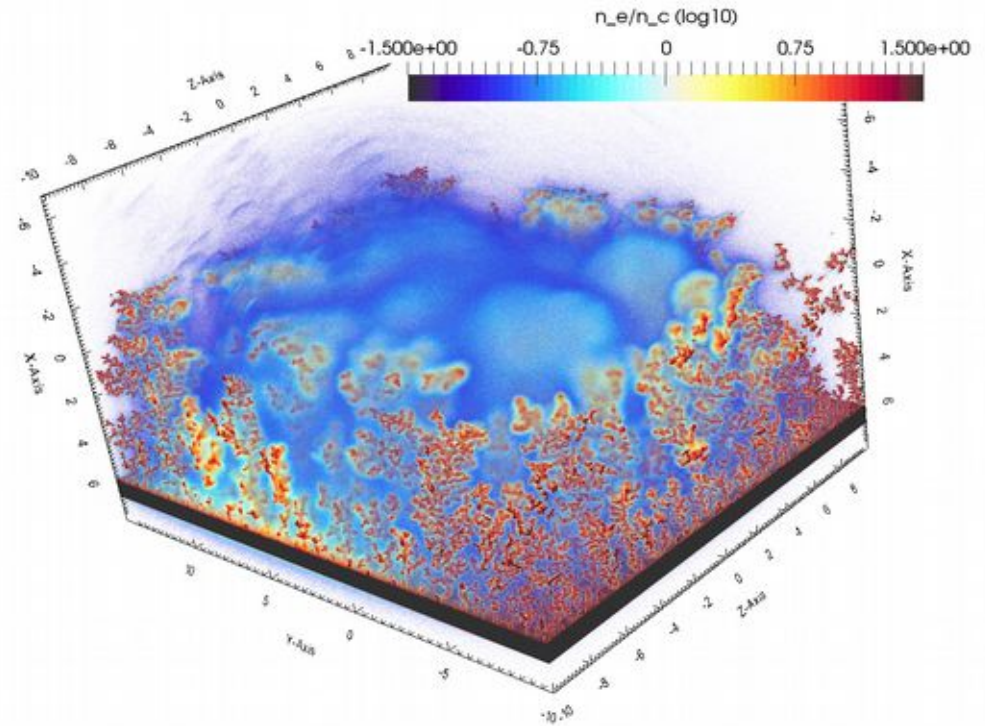


Experiments with foam-attached targets



Experiments with foam-attached targets

We used a realistic model to support our experimental activity on foam-attached targets

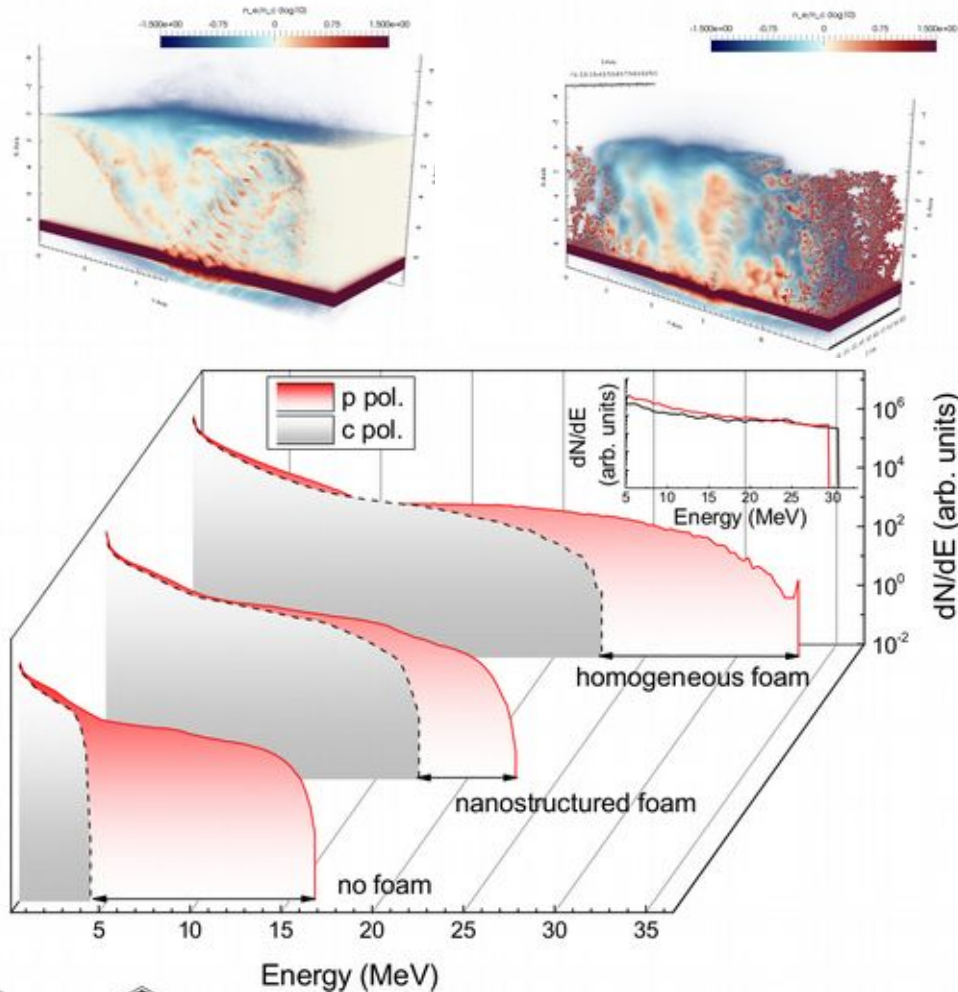


I.Prencipe et al., PPCF 58 (2016)
M.Passoni et al., PRAB 19(2016)

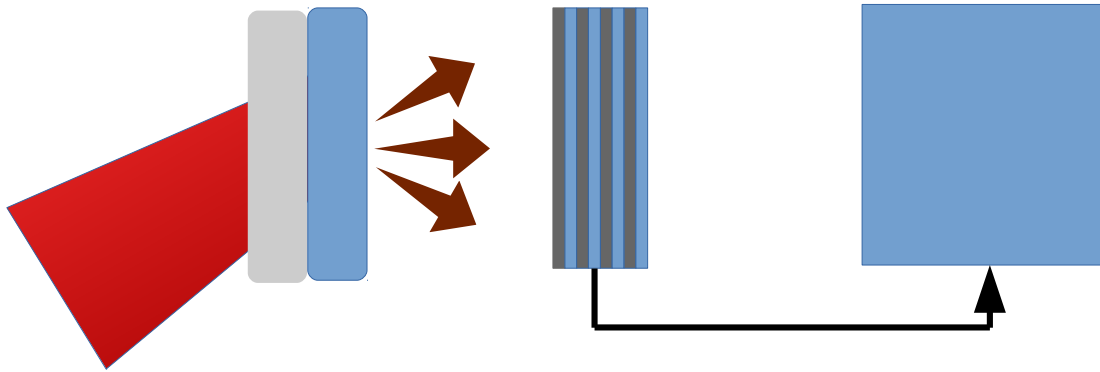


How do we simulate these plasmas?

Simulations with realistic foams allowed to reproduce essential features observed in the experiments



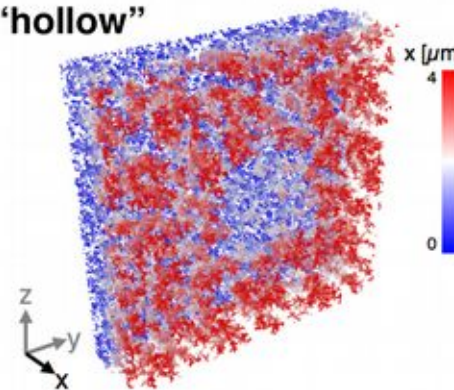
Some recent developments



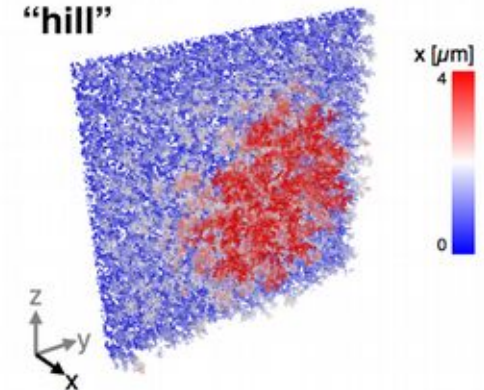
Synthetic RadioChromic Films for direct comparison with experimental results.

Also to understand the effect of foam inhomogeneities

“hollow”



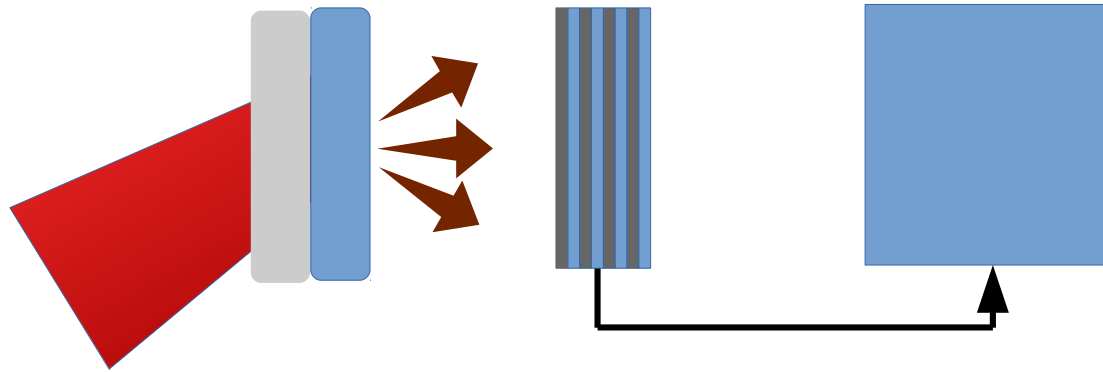
“hill”



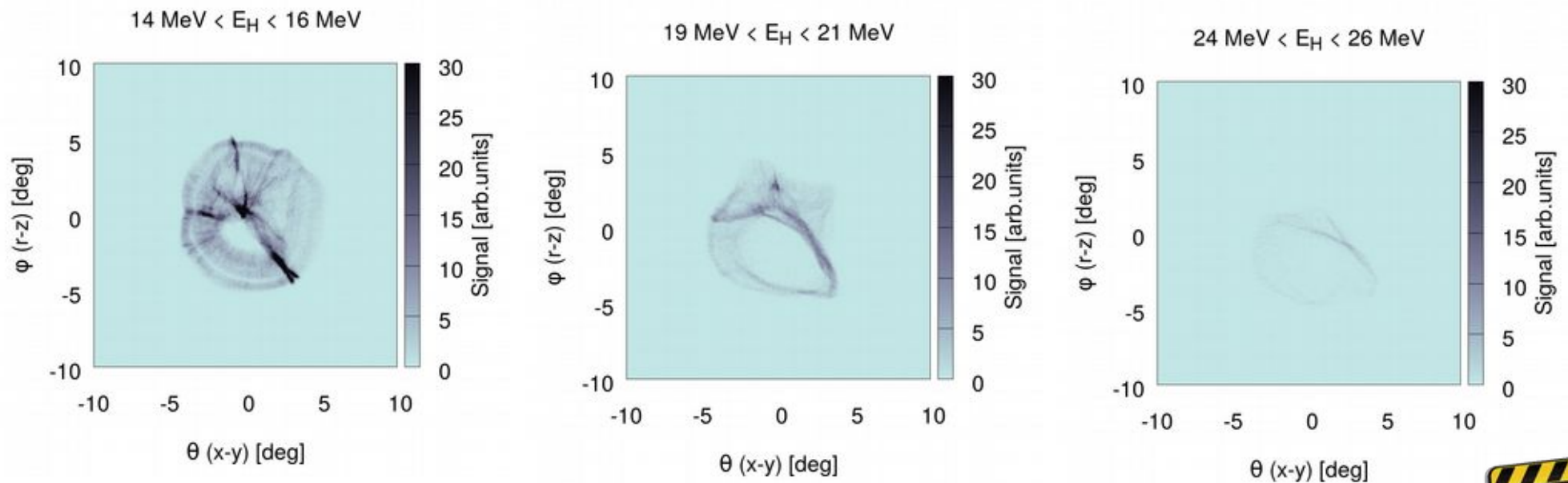
Simulations done by A. Formenti



Some recent developments



Synthetic RadioChromic Films for direct comparison with experimental results.



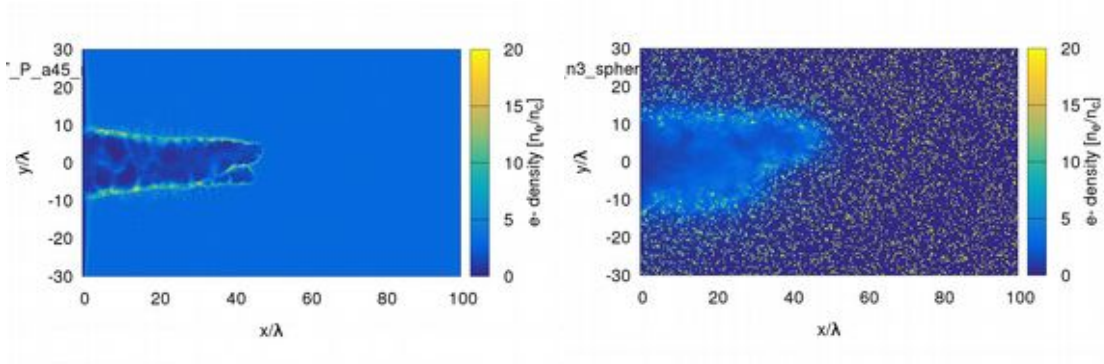
Simulations done by A. Formenti



Simulations of nanostructured plasmas: some examples with simplified models



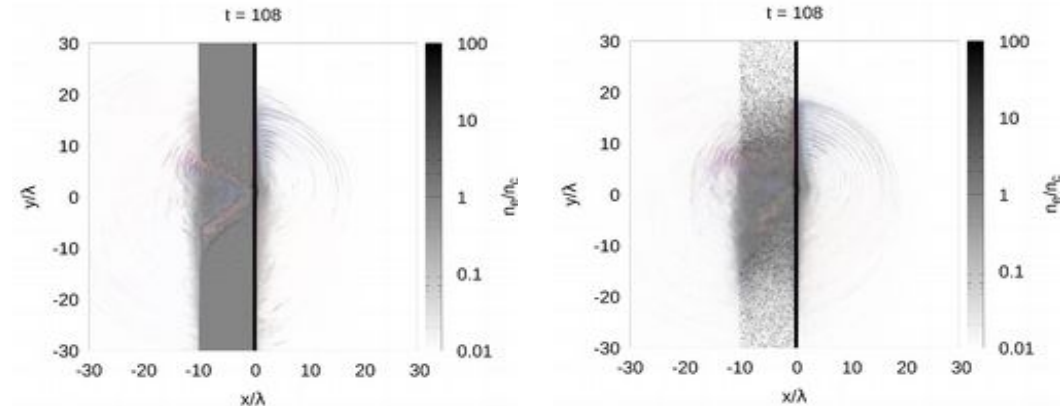
Simulations of nanostructured plasmas: some examples with simplified models



Laser propagation
in near-critical
foams



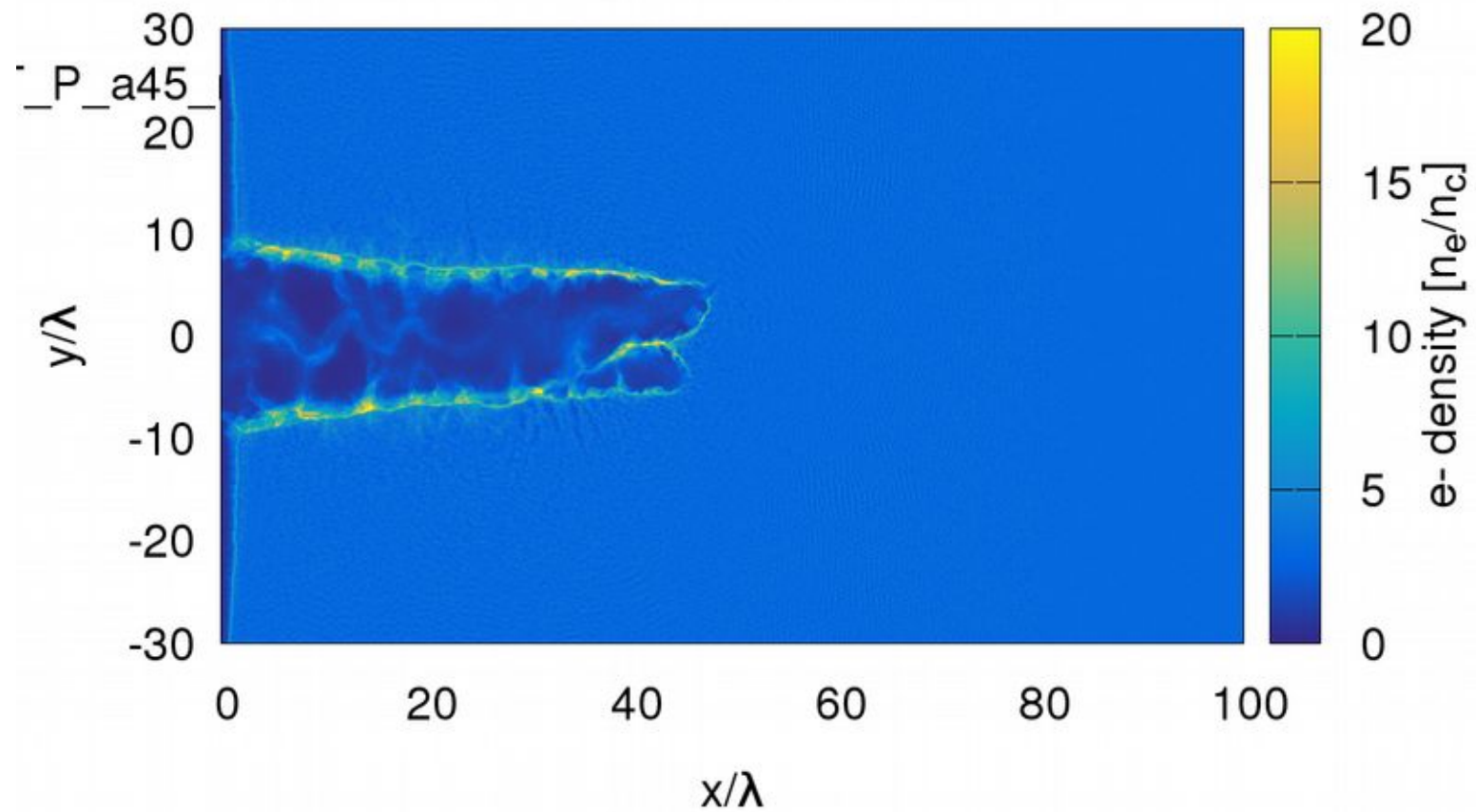
Enhanced electron
heating with foam-
attached targets



Laser propagation in near-critical plasmas

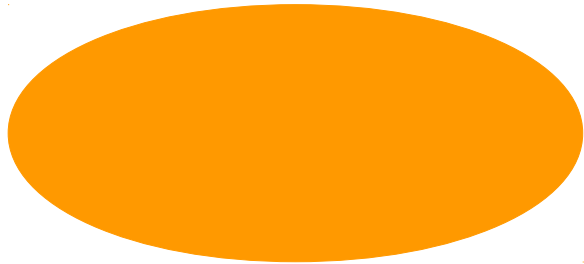


Laser propagation in near-critical plasmas



Laser propagation in near-critical plasmas

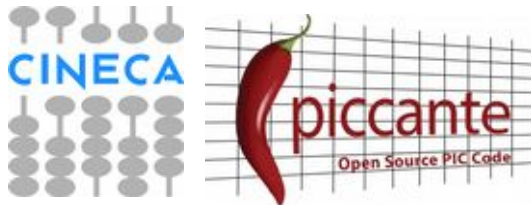
The numerical setup



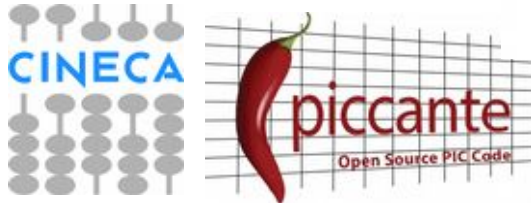
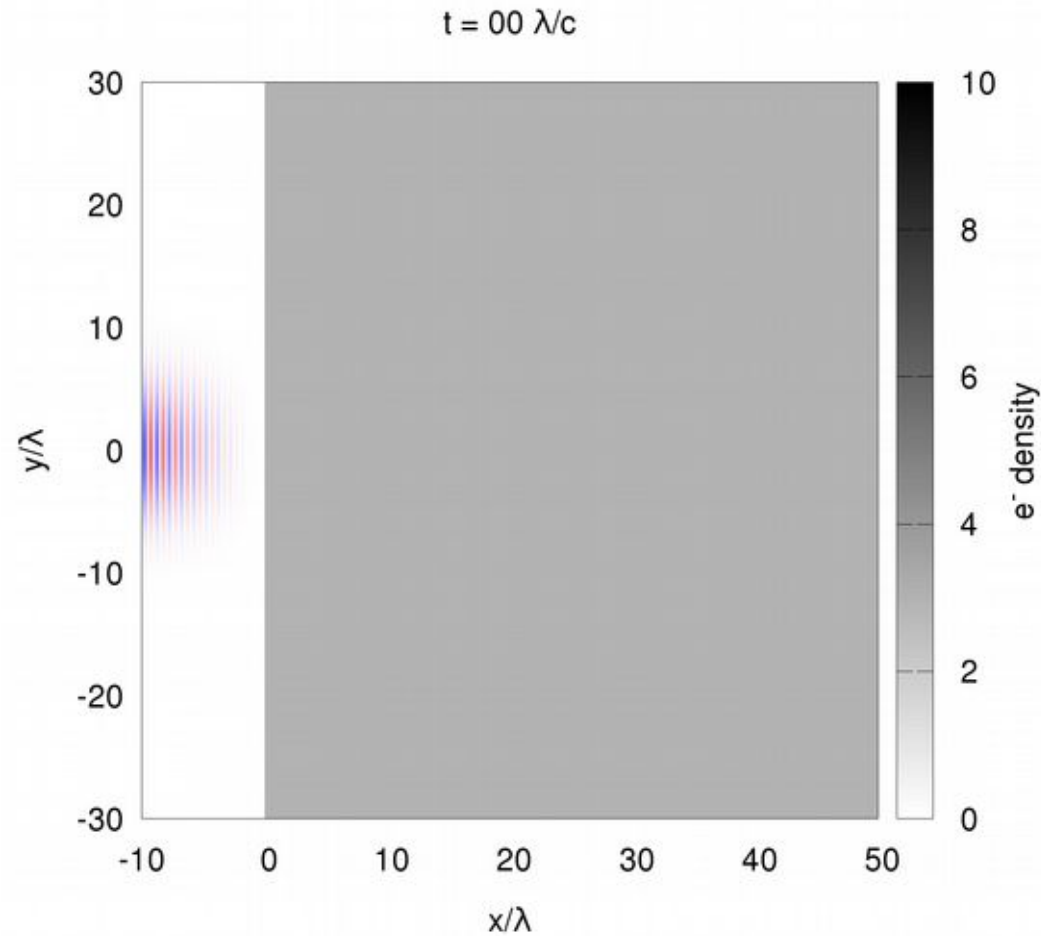
P-polarized, gaussian
 $a_0=45$, $w=5\lambda$, $\tau_{FWHM}=15\lambda/c$

Uniform, $n = 3 n_c$
30 part.p.cell (for e^-)

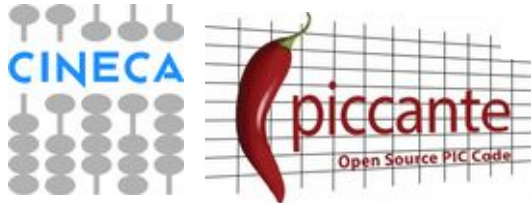
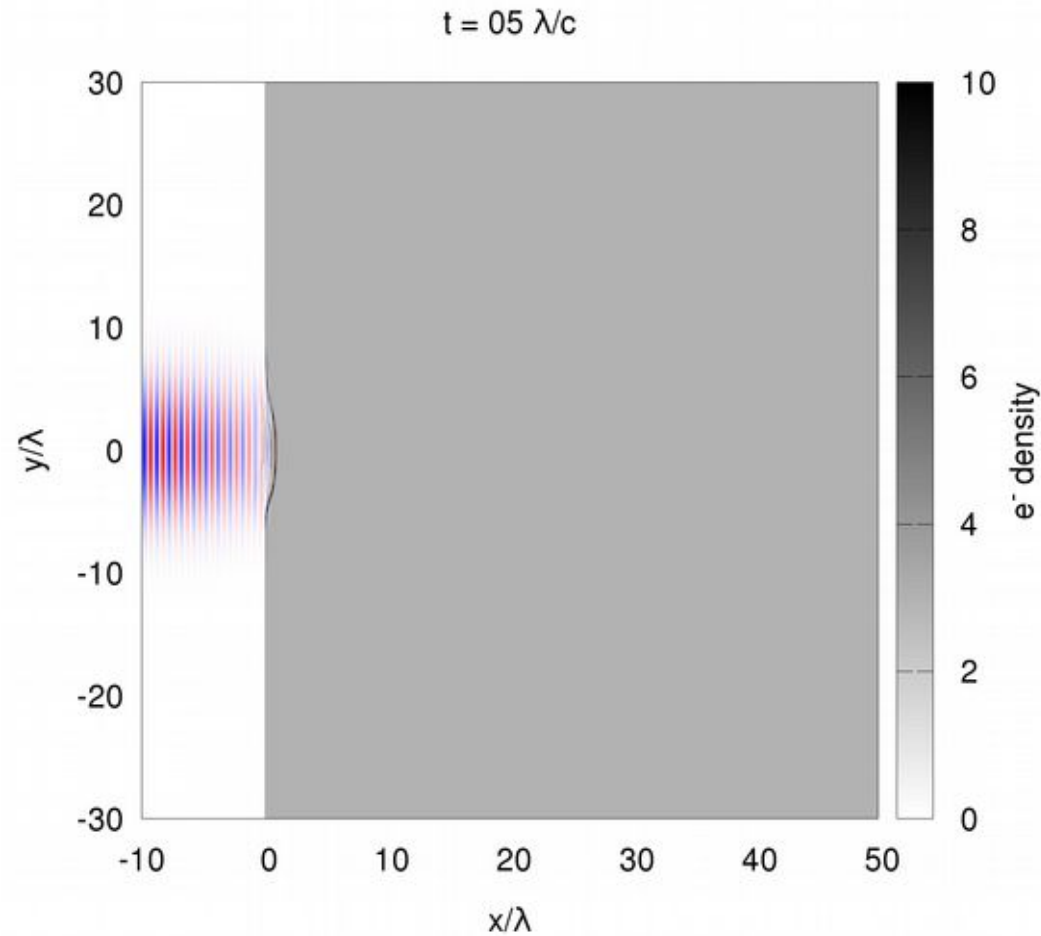
Box: $220\lambda \times 60\lambda$
Resolution: 30 pp λ



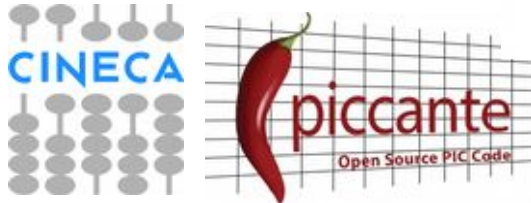
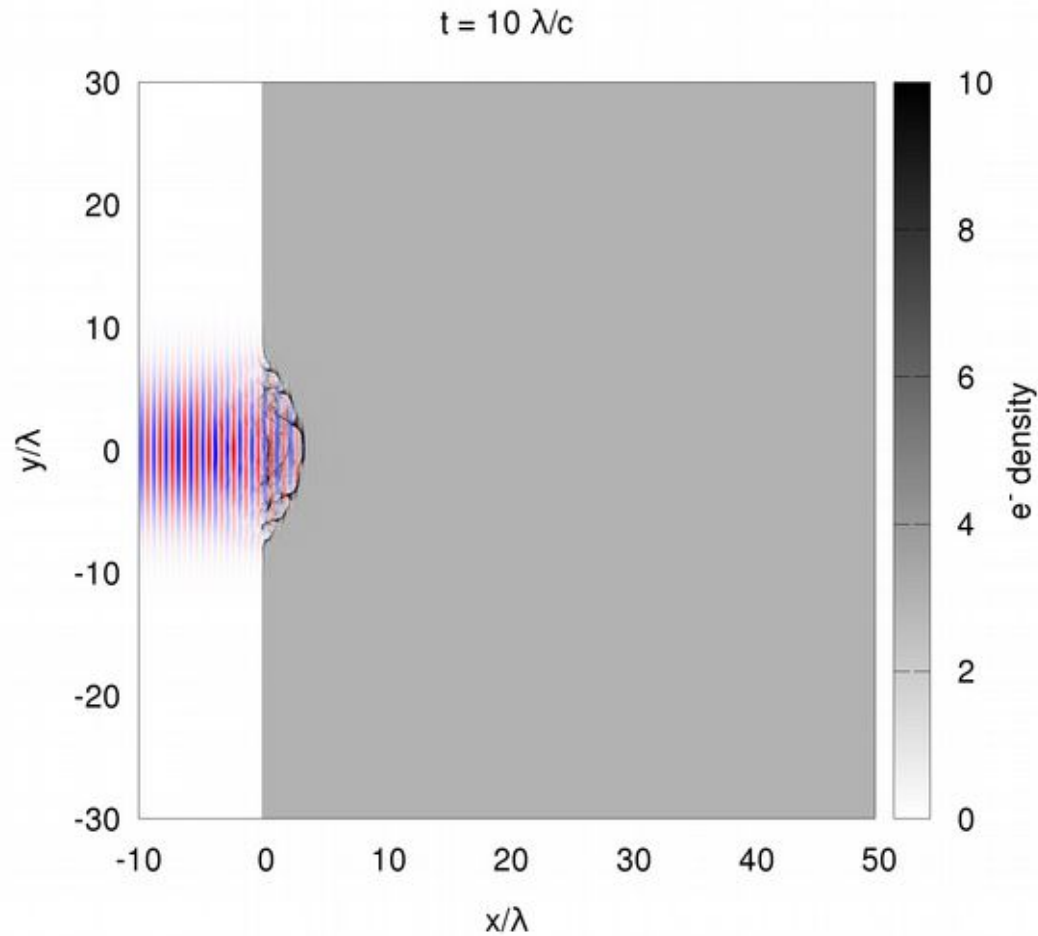
Laser propagation in near-critical plasmas



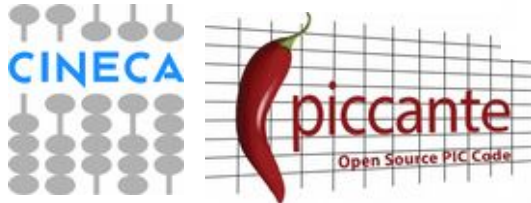
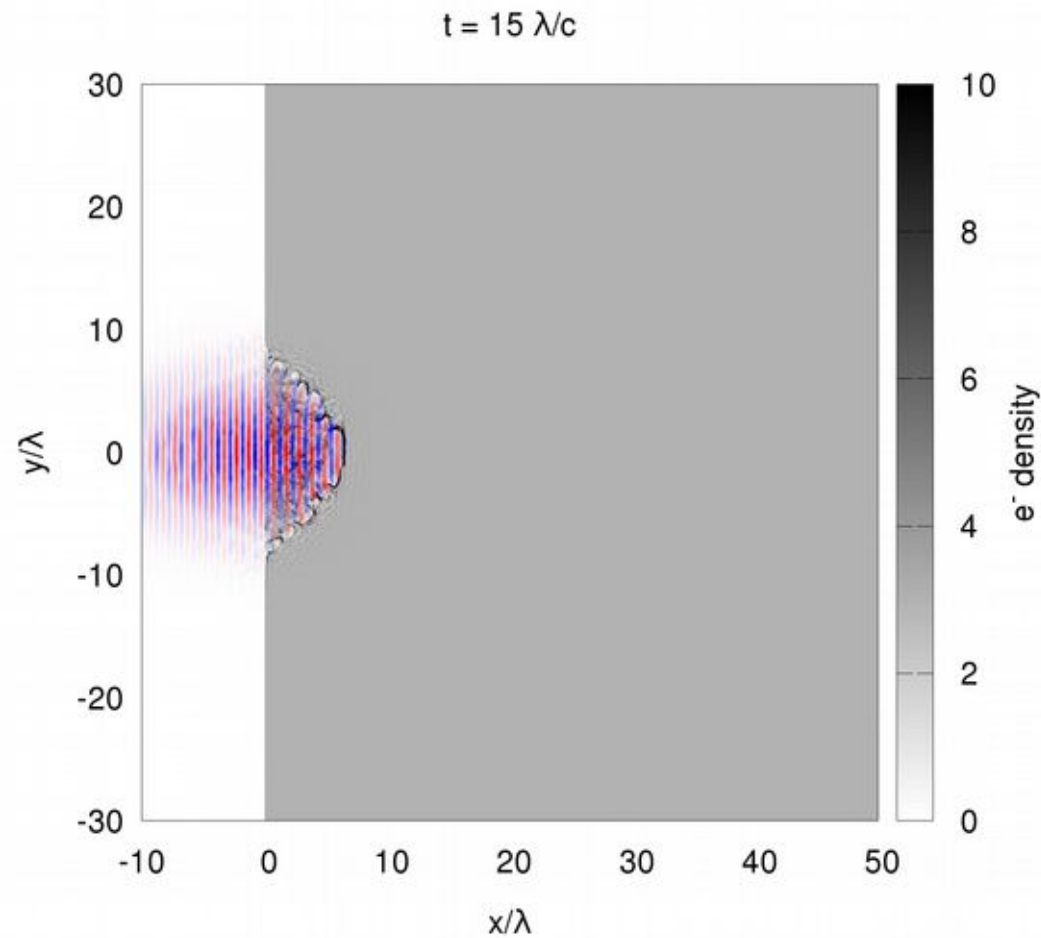
Laser propagation in near-critical plasmas



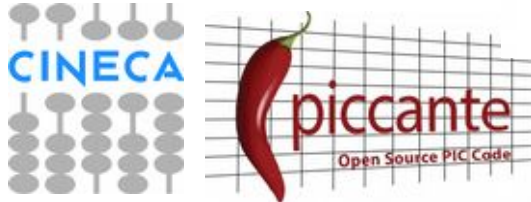
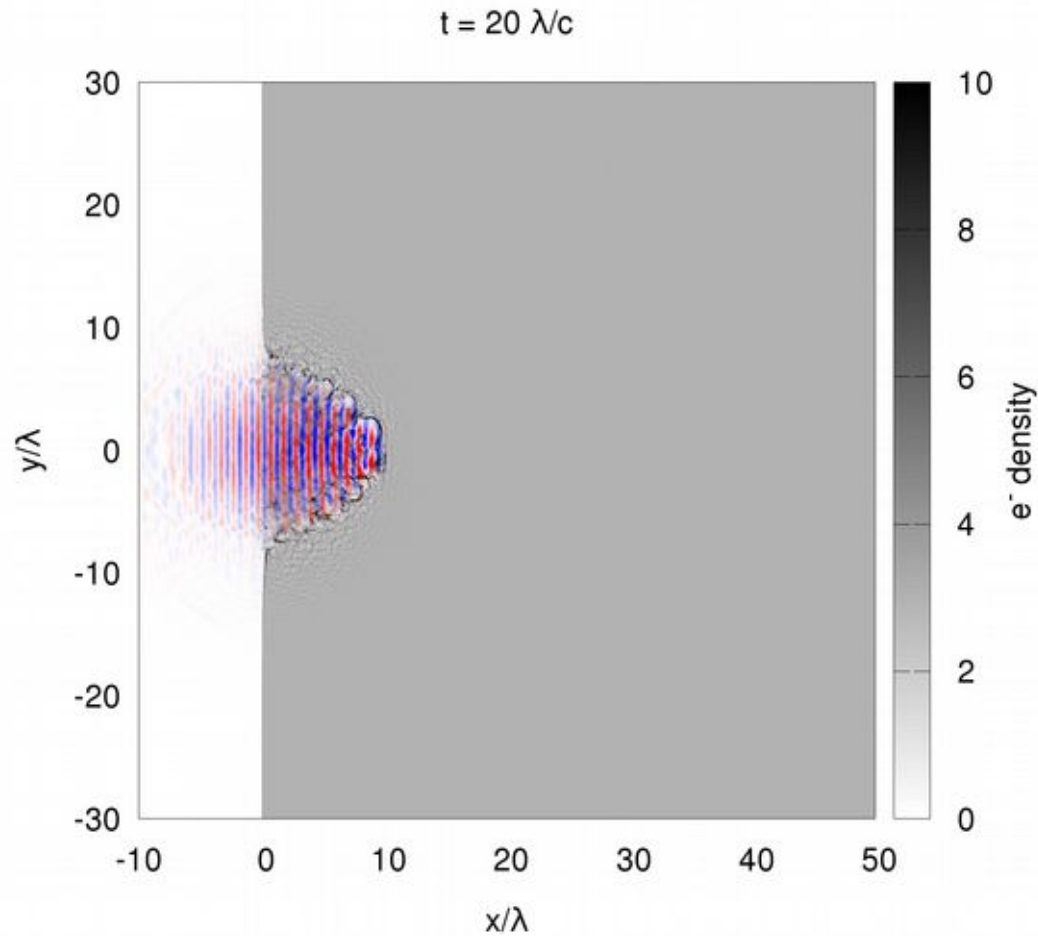
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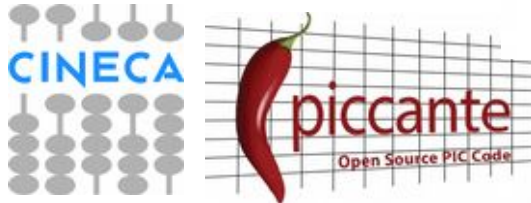
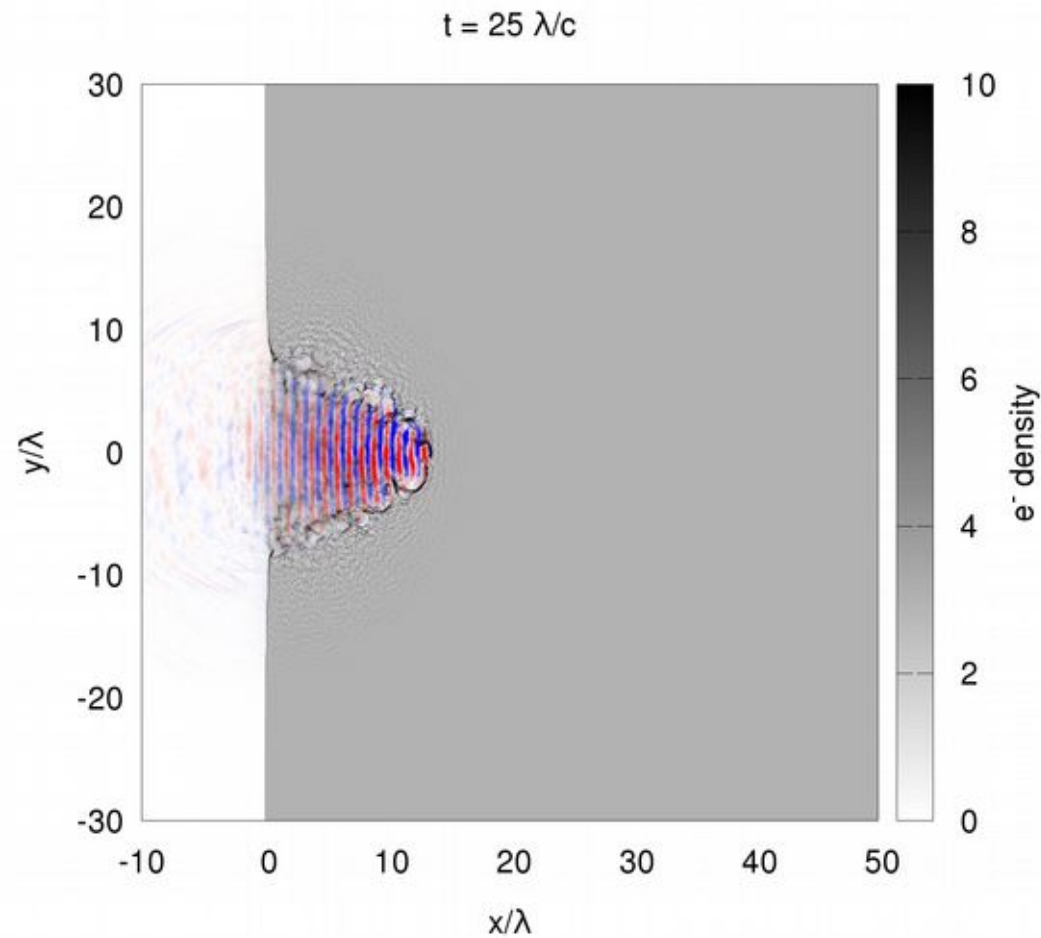
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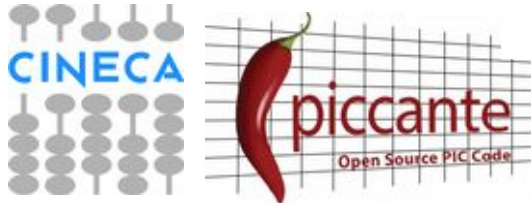
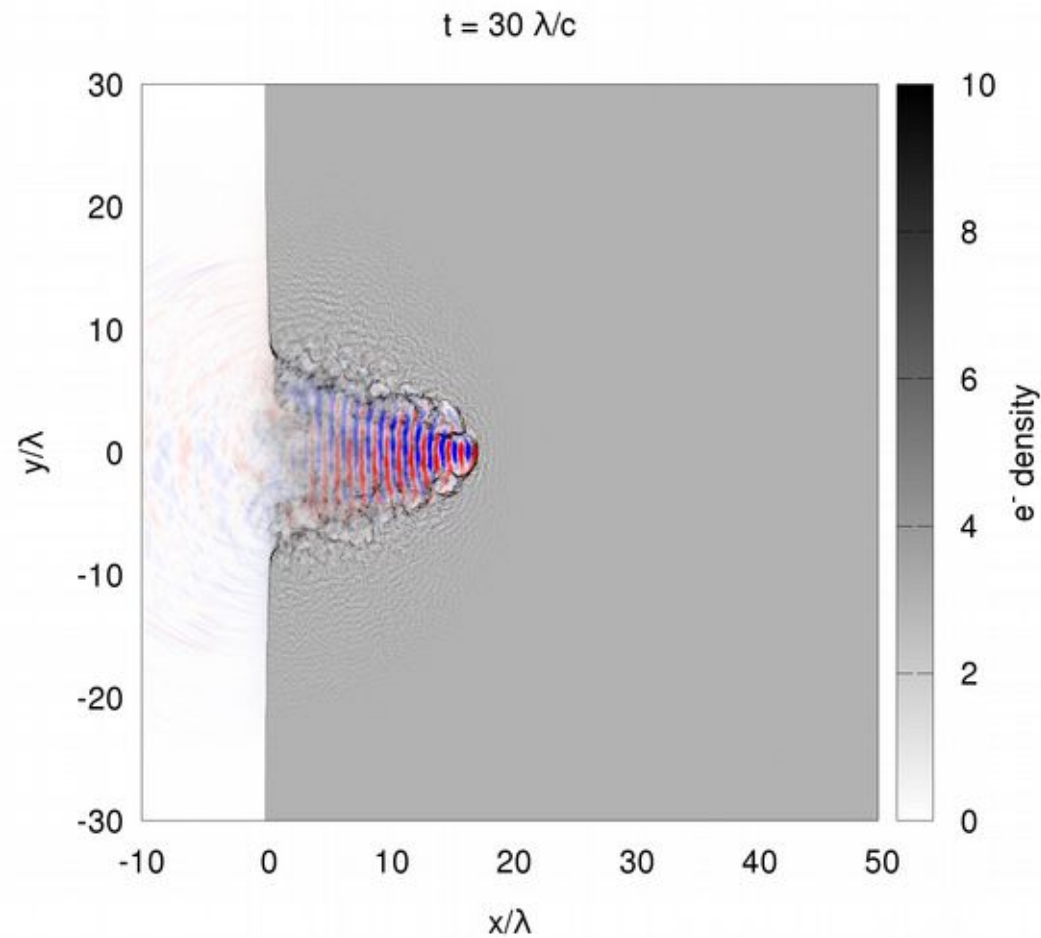
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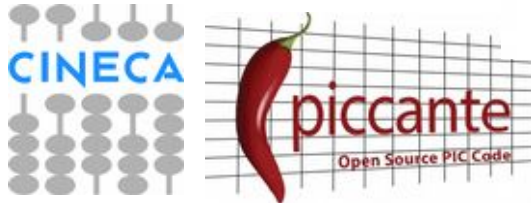
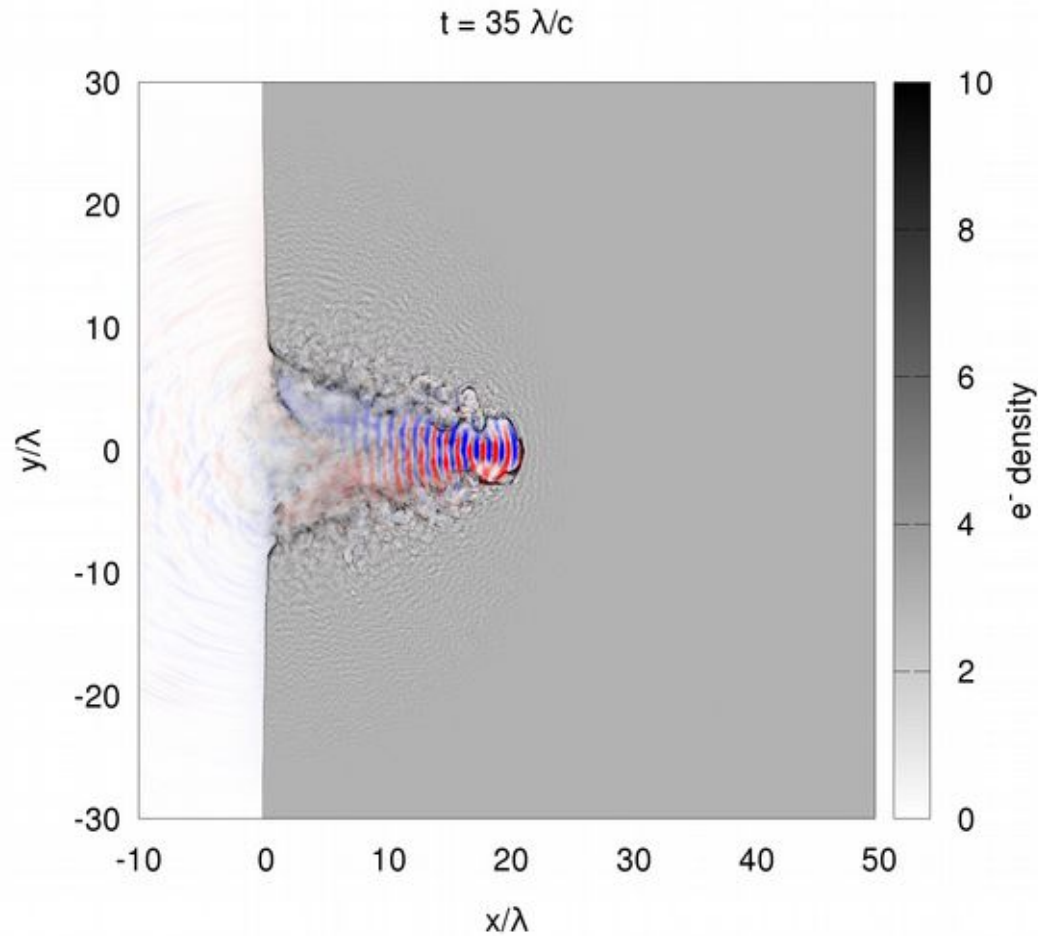
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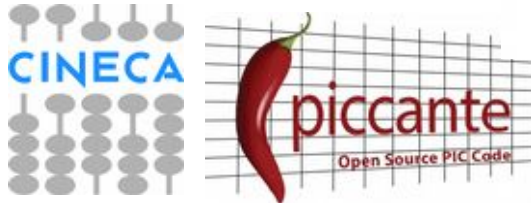
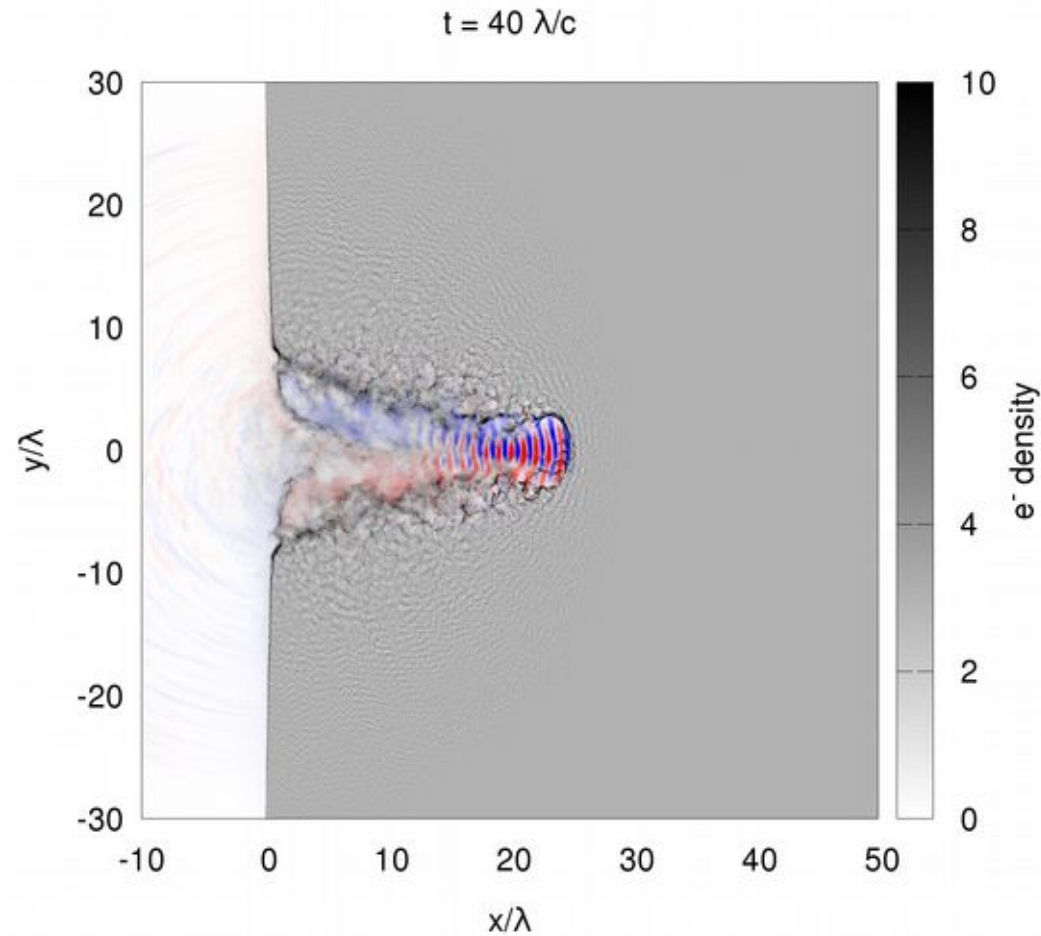
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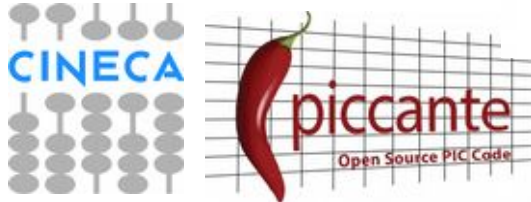
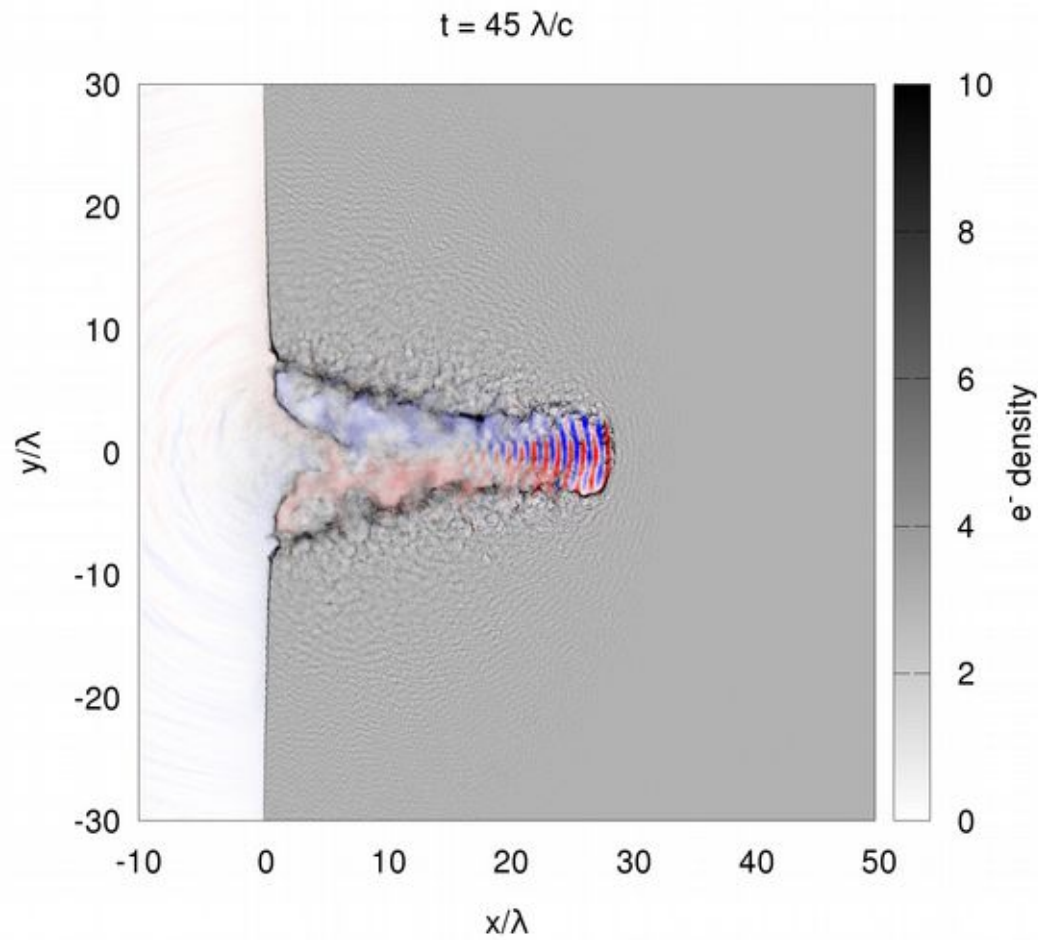
Laser propagation in near-critical plasmas



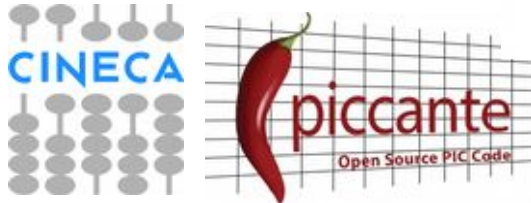
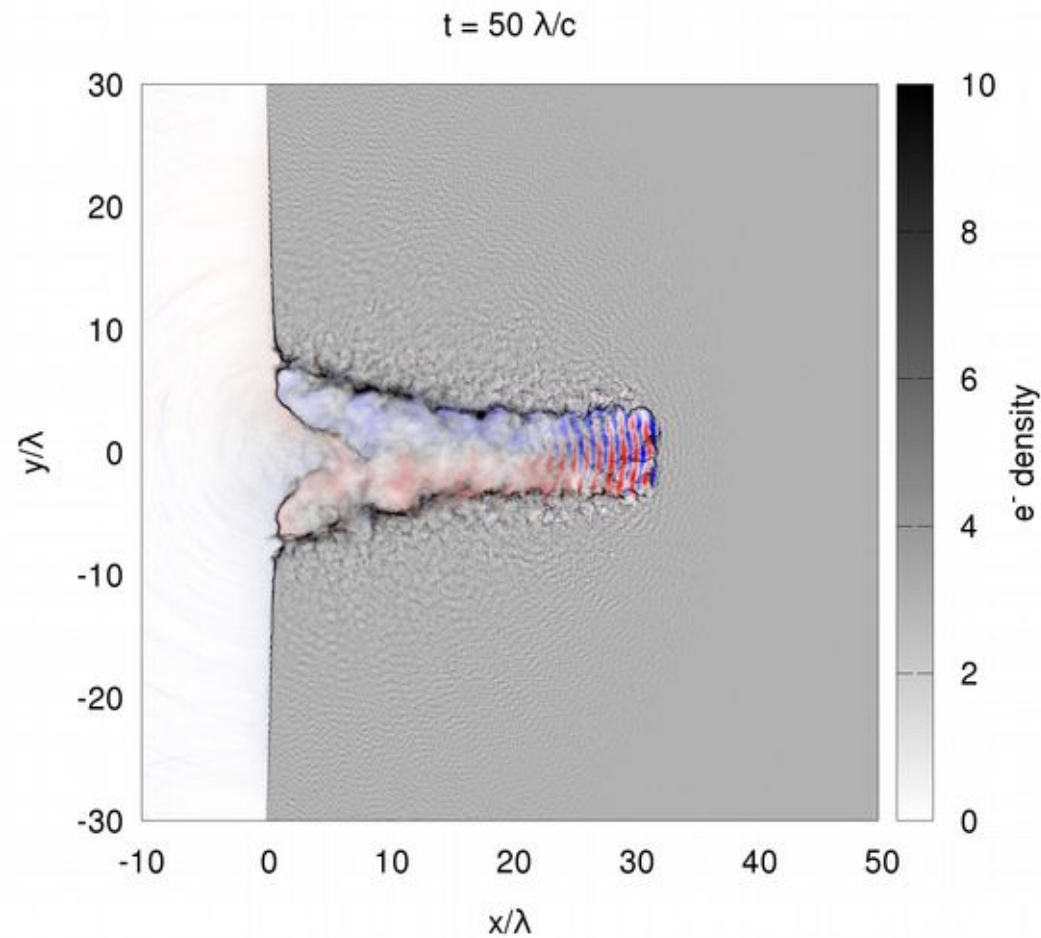
Laser propagation in near-critical plasmas



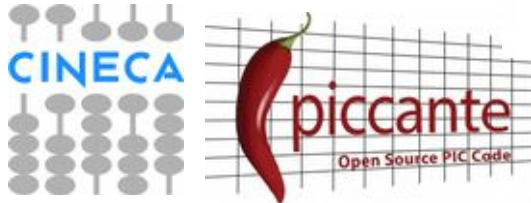
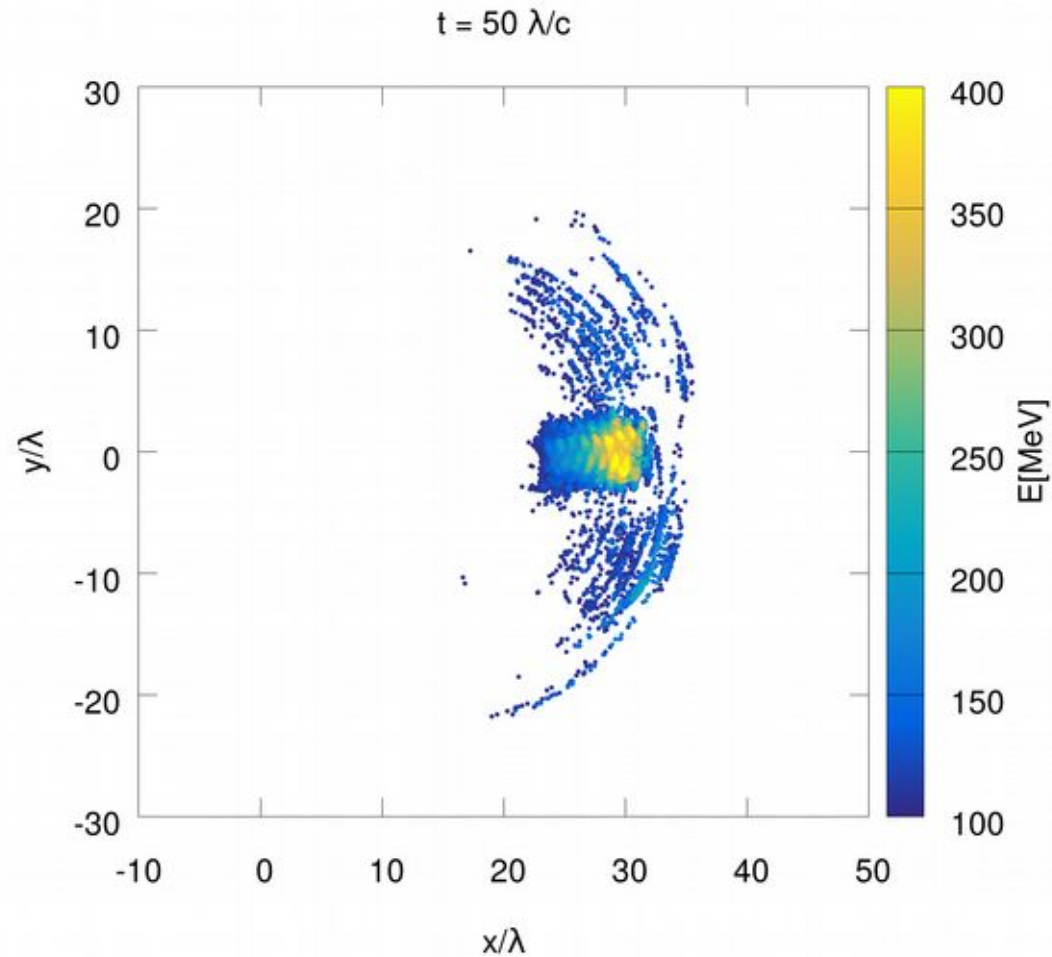
Laser propagation in near-critical plasmas



Laser propagation in near-critical plasmas



Laser propagation in near-critical plasmas

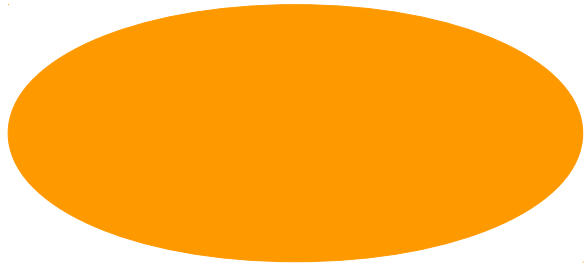


H.Wang et al. PoP 22 (2015)
D.J. Stark et al. PRL 116 (2016)

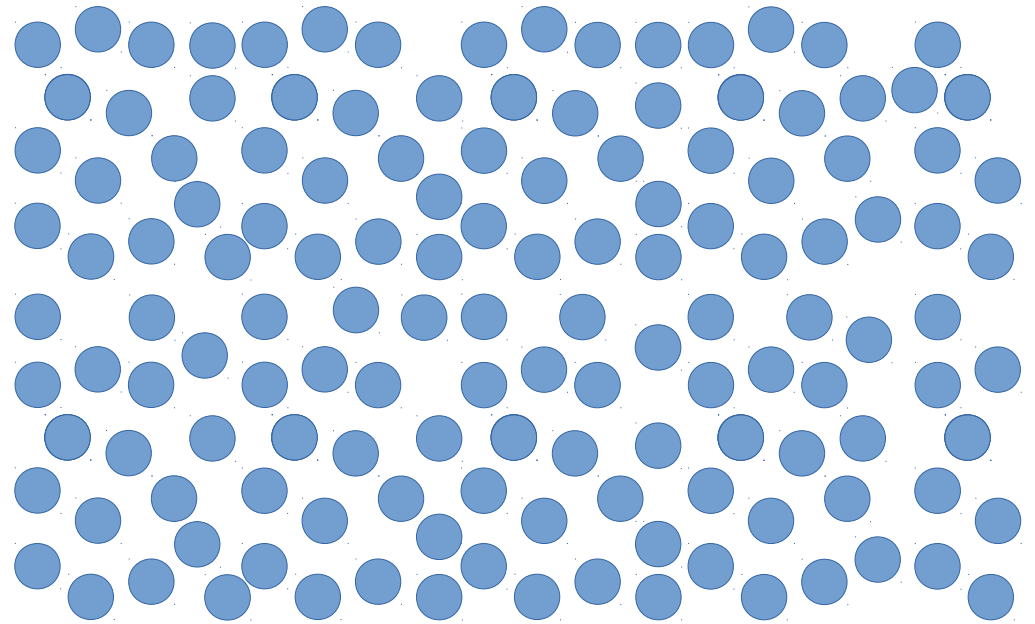


Laser propagation in near-critical plasmas

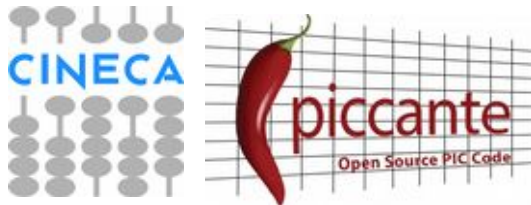
The numerical setup



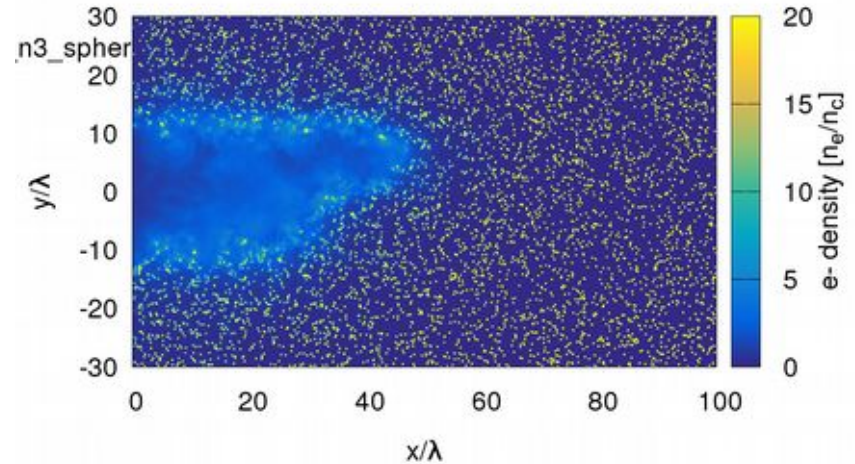
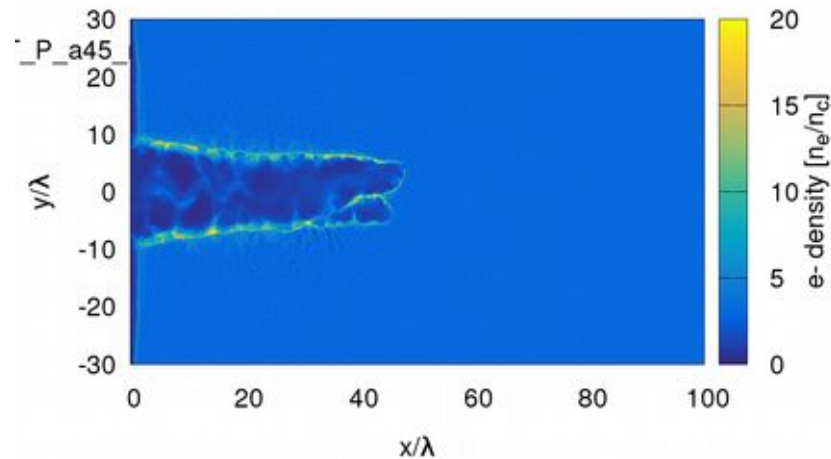
P-polarized, gaussian
 $a_0 = 45$, $w = 5\lambda$, $\tau_{\text{FWHM}} = 15\lambda/c$



Rnd. spheres, $\langle n \rangle = 3 n_c$
 $r = 0.178 \lambda$, filling = 0.1
 270 part.p.cell (for e^-)



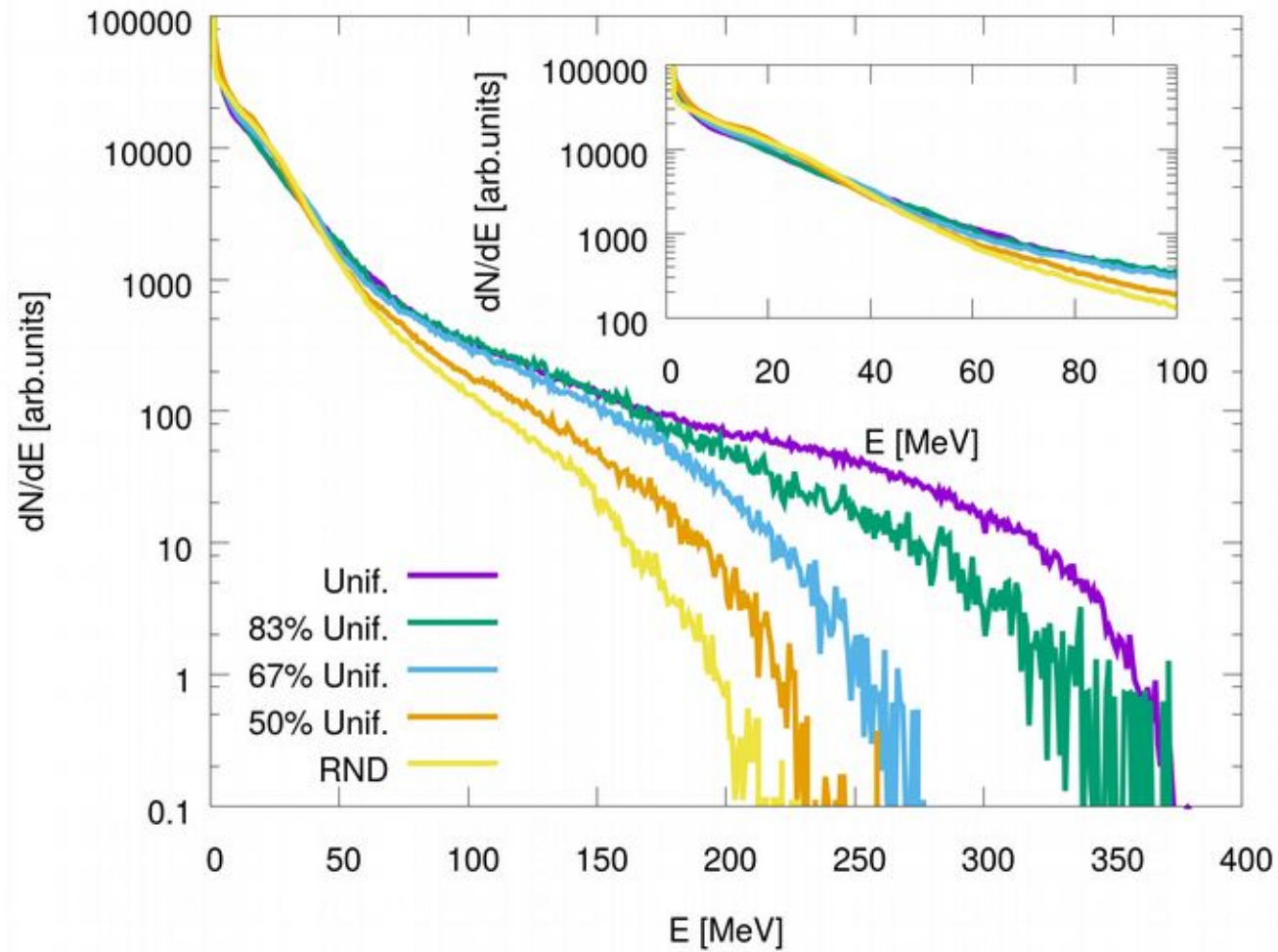
Numerical simulations



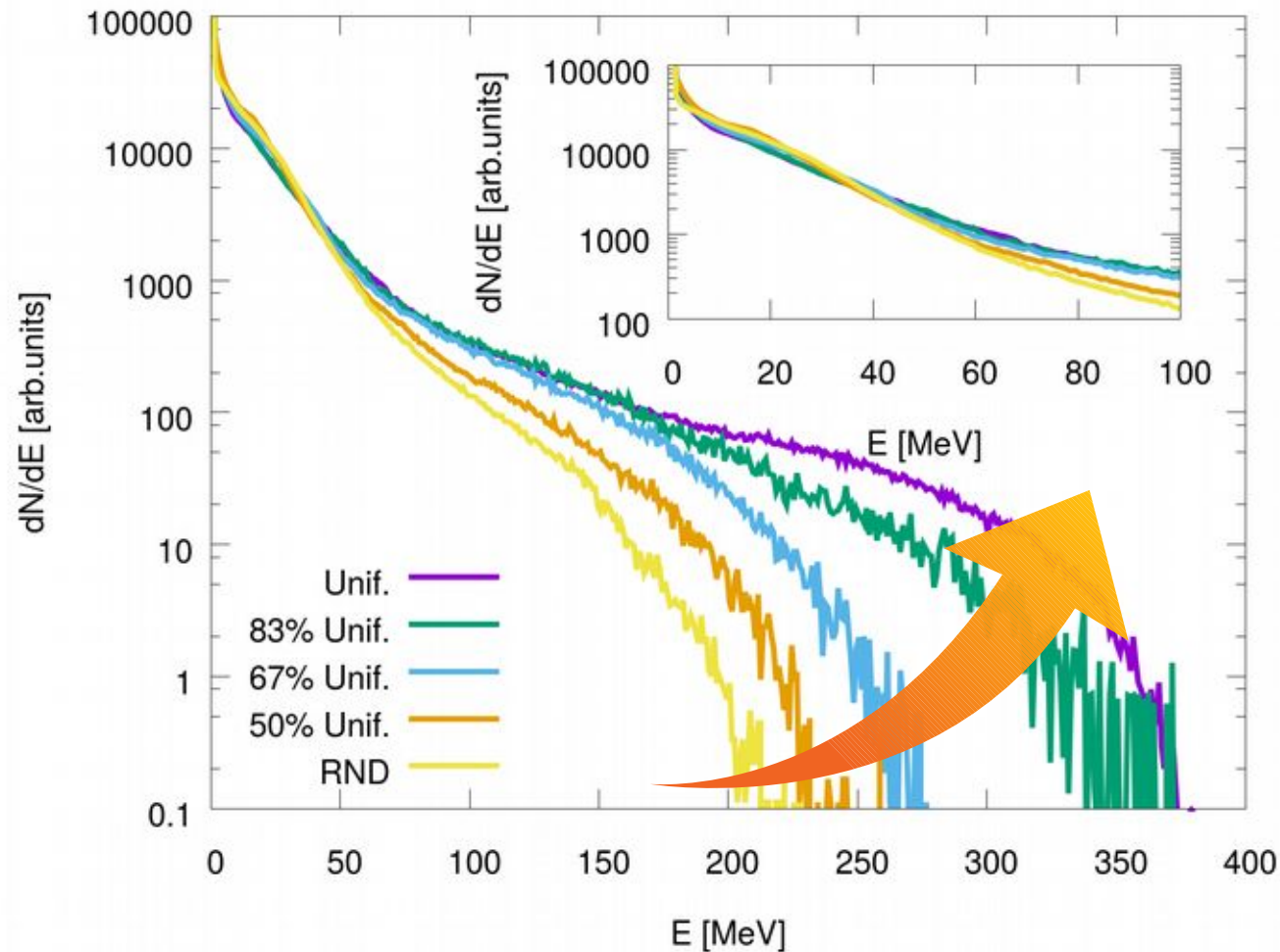
$$67\% \quad \square + 33\% \quad \bullet \bullet \bullet \bullet \bullet = 3 n_c \text{ on avg.}$$

I can mix the two plasmas, going from a fully uniform plasma to a fully disconnected random spheres - plasma

Numerical simulations



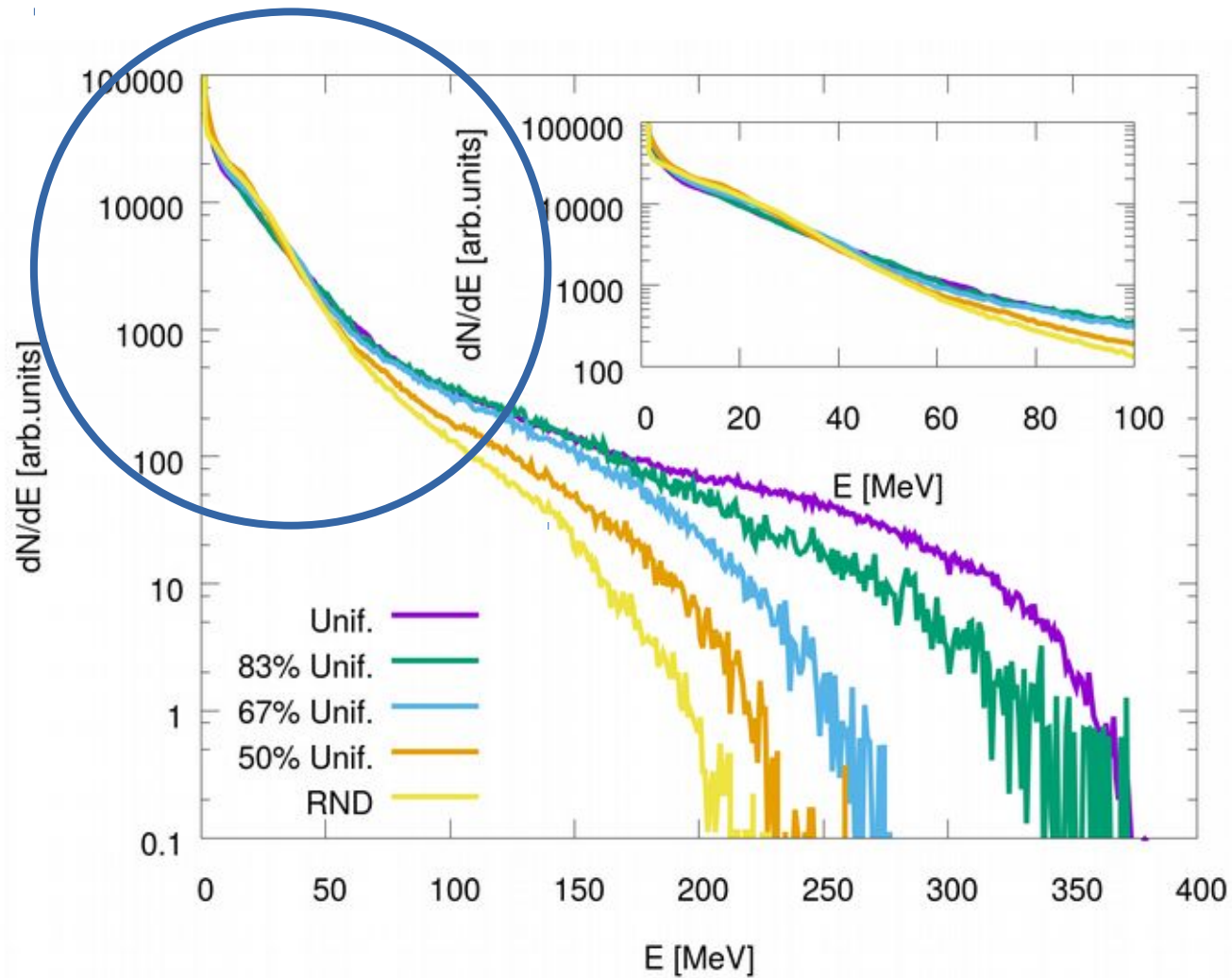
Numerical simulations



From “completely random spheres”
to completely uniform



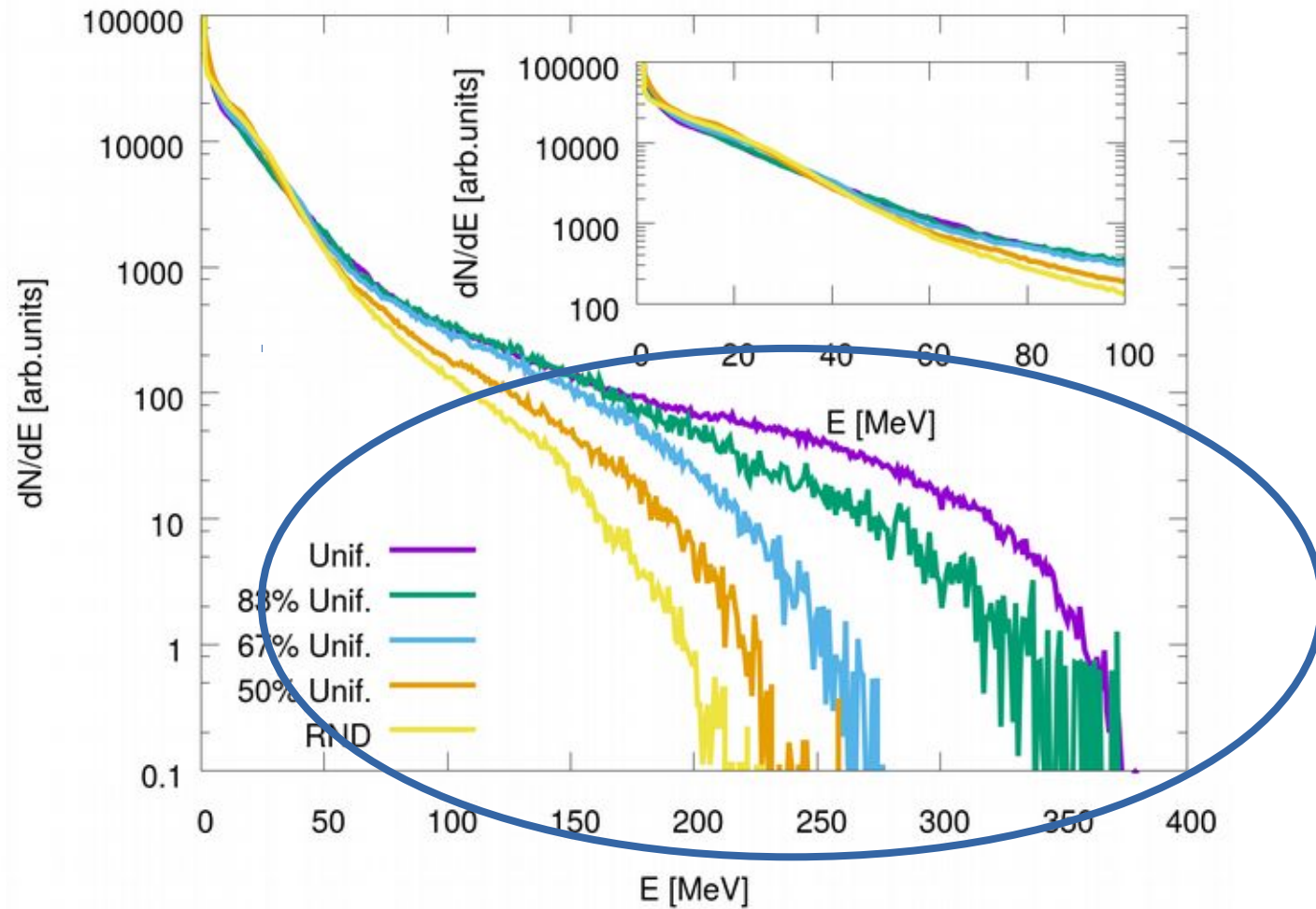
Numerical simulations



“Some” temperature difference here



Numerical simulations



Significant cut-off energy difference

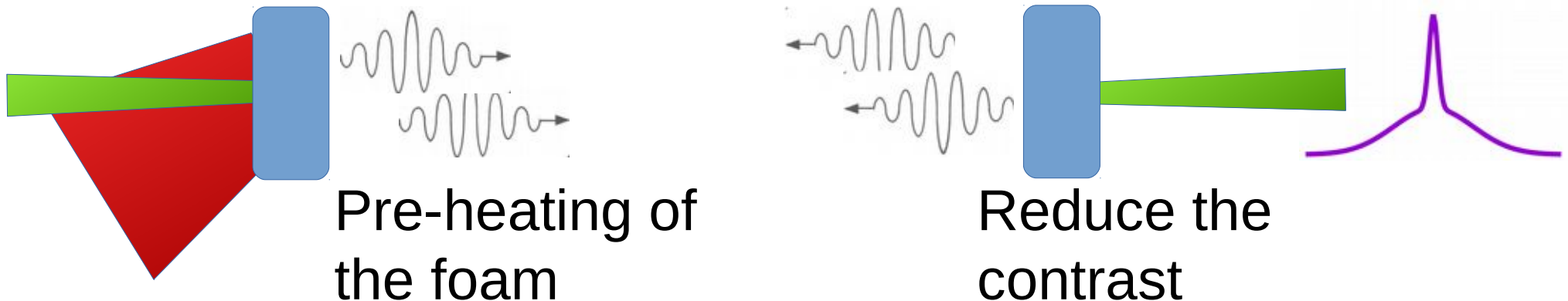


Numerical simulations

This is observable if we look at the spectrum of synchrotron emission. Peak scales as $\sim \gamma^3 \omega_c$

According to the model, “uniform is probably better” for synchrotron emission

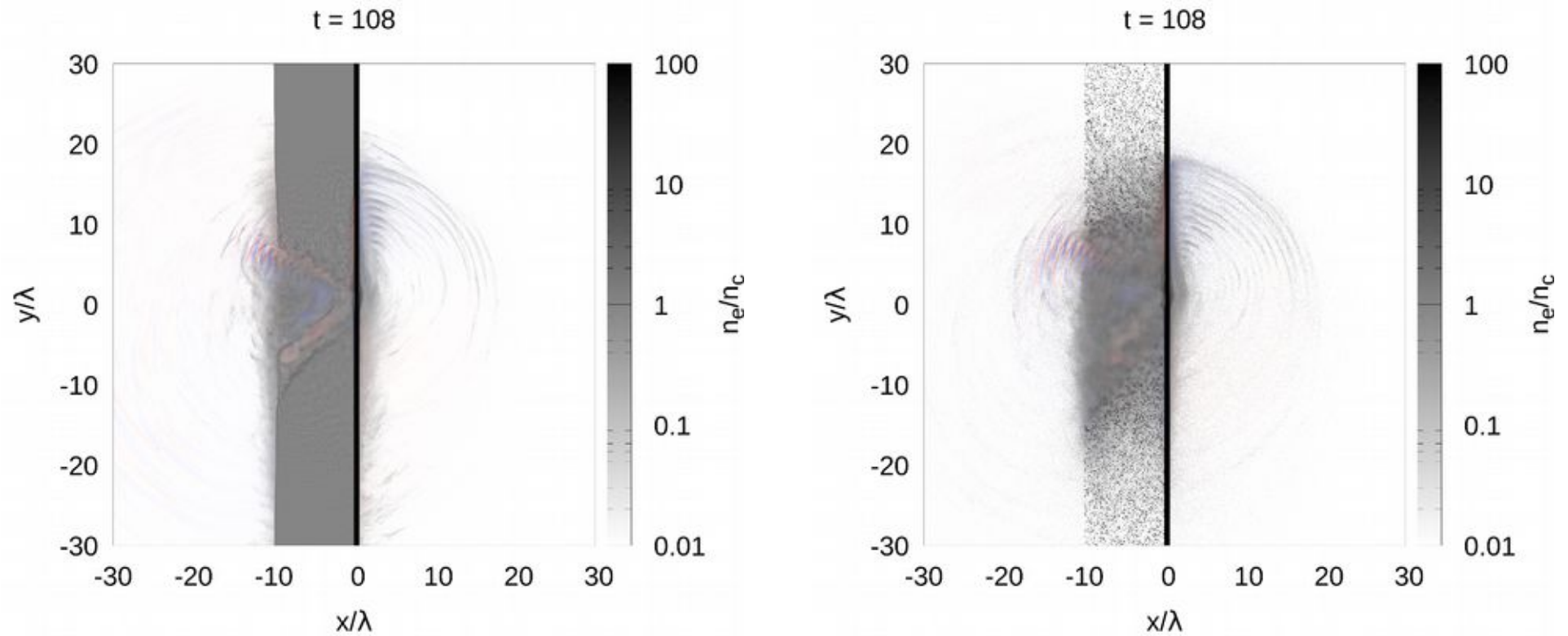
In principle we could see if the model makes any sense with a simple experiment



Electron heating in foam-attached targets



Electron heating in foam-attached targets




Electron-heating in foam-attached targets



A lot of existing literature!

Interesting for several reasons:
ion acceleration, electron/positron beams,
electron transport...

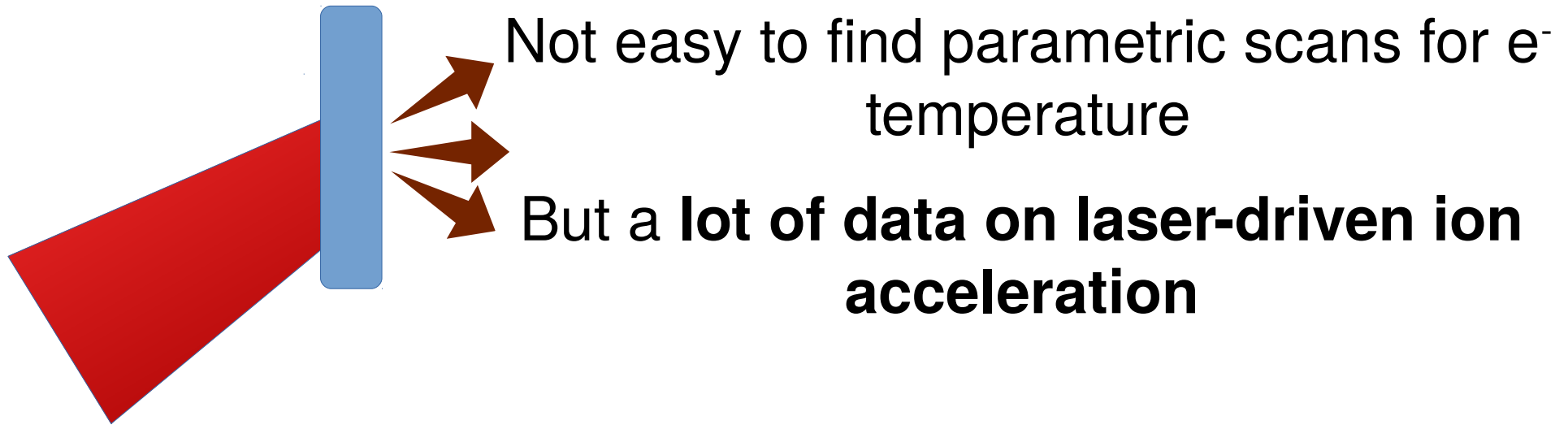


However, several issues of existing models (Angular dependence, polarization dependence...) and **no models for foam-attached targets**

L.Cialfi, L.Fedeli, M.Passoni, accepted with minor revisions, PRE



Electron-heating in foam-attached targets



L.Cialfi, L.Fedeli, M.Passoni, accepted with minor revisions, PRE



Electron-heating in simple targets

Write a model for $T_e(a_0, \text{pol})$

JxB heating

Vacuum heating

$$T_e [MeV] = 0.511 \cdot C_1(\text{pol}) \cdot \left(\sqrt{1 + \frac{a_0^2}{2}} - 1 \right) + 0.511 \cdot C_2(\text{pol}) \cdot \left(\sqrt{1 + 2 a_0^2 \sin^2 \theta} - 1 \right) \cdot \tan \theta$$



Electron-heating in simple targets

Write a model for $T_e(a_0, \text{pol})$

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2D/3D simulations to check model and fit parameters



Electron-heating in simple targets

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2D/3D simulations to check model and fit parameters

Plug T_e into existing model for ion acceleration

$$E_{max}(\text{ions}) = Z_i k_b T_e \left[\phi' - 1 + \frac{\beta(\phi', \xi)}{I(\phi', \xi) e^{\phi' + \xi}} \right] \quad \text{M.Passoni, M. Lontano. PRL 101 (2008)}$$



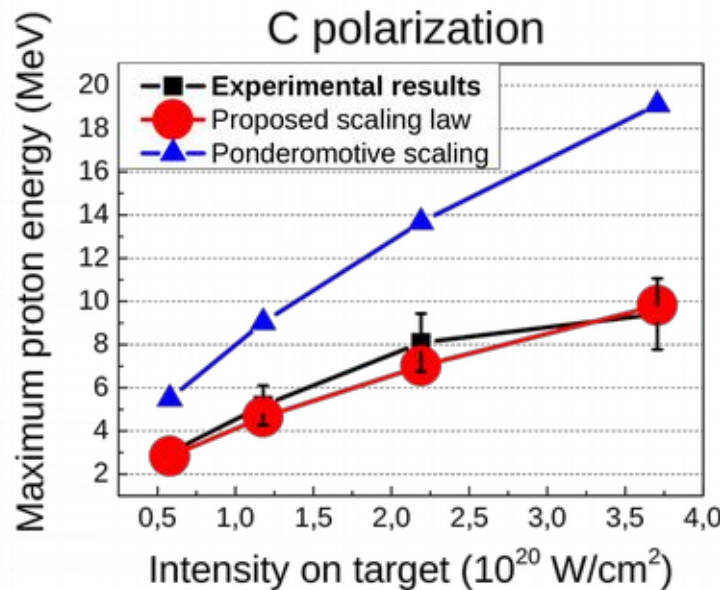
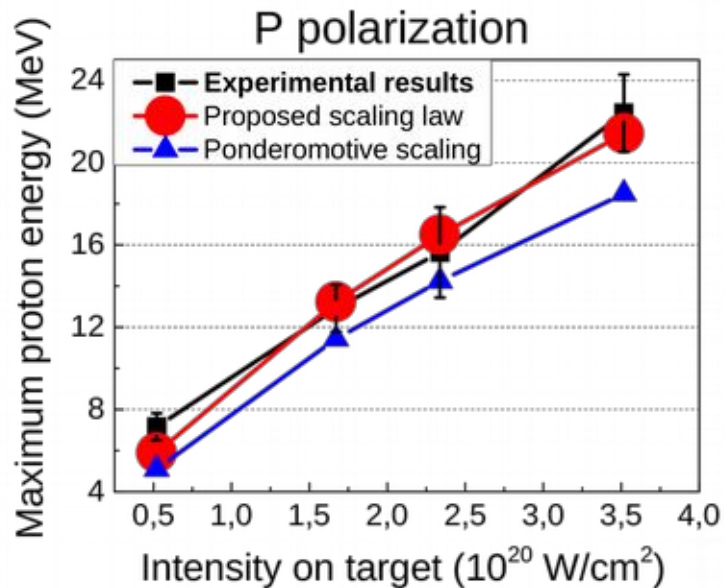
Electron-heating in simple targets

JxB heating

Vacuum heating

$$T_e [MeV] = 0.511 \cdot C_1(pol) \cdot \left(\sqrt{1 + \frac{a_0^2}{2}} - 1 \right) + 0.511 \cdot C_2(pol) \cdot \left(\sqrt{1 + 2 a_0^2 \sin^2 \theta} - 1 \right) \cdot \tan \theta$$

Benchmark with experiments

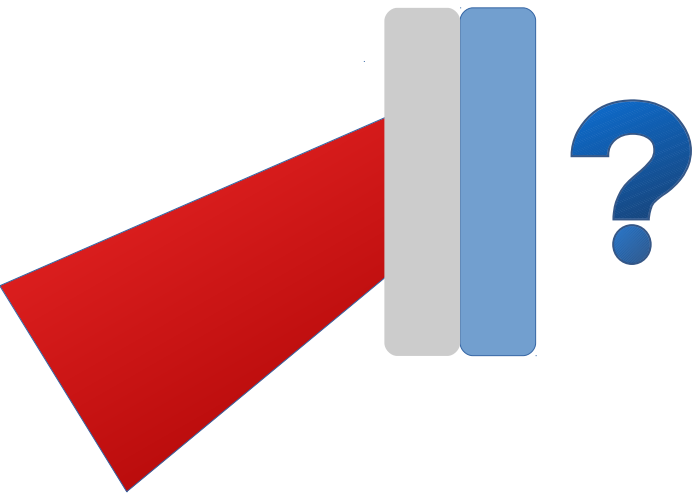


Exp. data

I. Prencipe et al.
PPCF 58 (2016)
M. Passoni et al.
PRAB (2016)

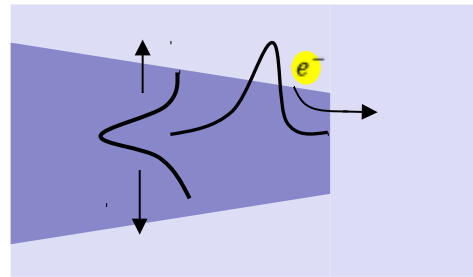


Electron-heating in near-critical plasmas



What about foam-attached targets?

APL Robinson et al, PPCF 53 (2011)



Pulse erosion

$$T_e \sim a_0^2$$

Ponderomotive expulsion $T_e \sim a_0$

L.Cialfi, L.Fedeli, M.Passoni, accepted with minor revisions, PRE



Electron-heating in near-critical plasmas



What about foam-attached targets?

2D Particle-In-Cell
simulations to obtain T_e

Investigation limited to
one particular setup

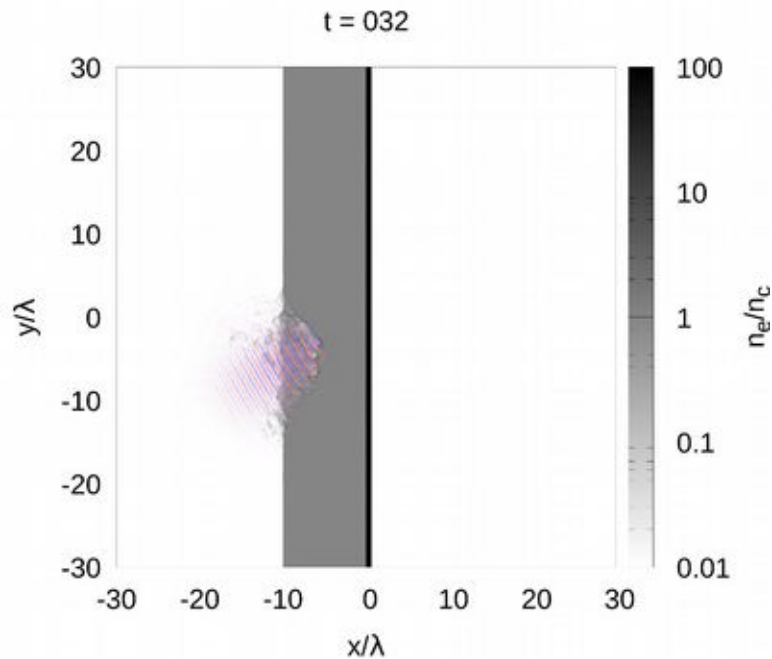


L.Cialfi, L.Fedeli, M.Passoni, accepted with minor revisions, PRE

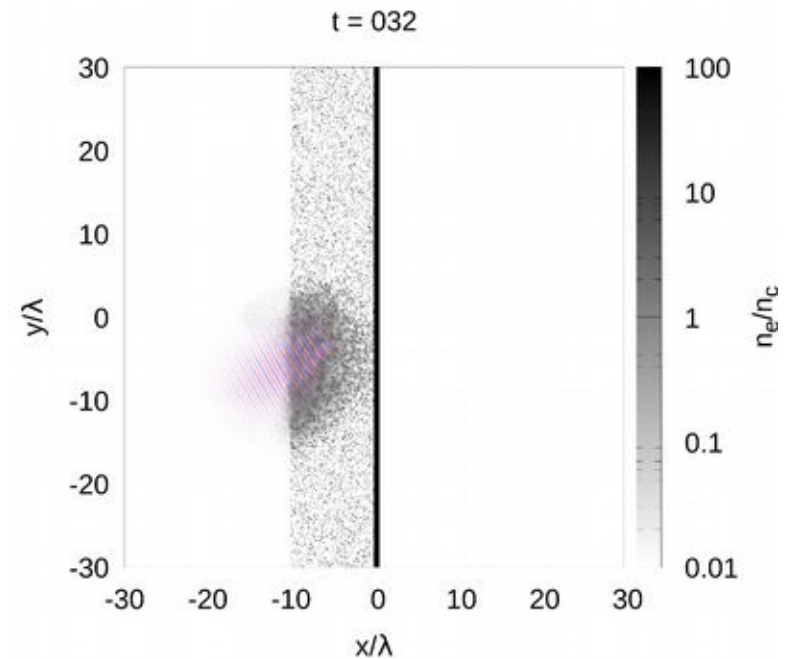


Electron-heating in near-critical plasmas

Two models for the foam



Homogeneous foam $n_e = n_c$



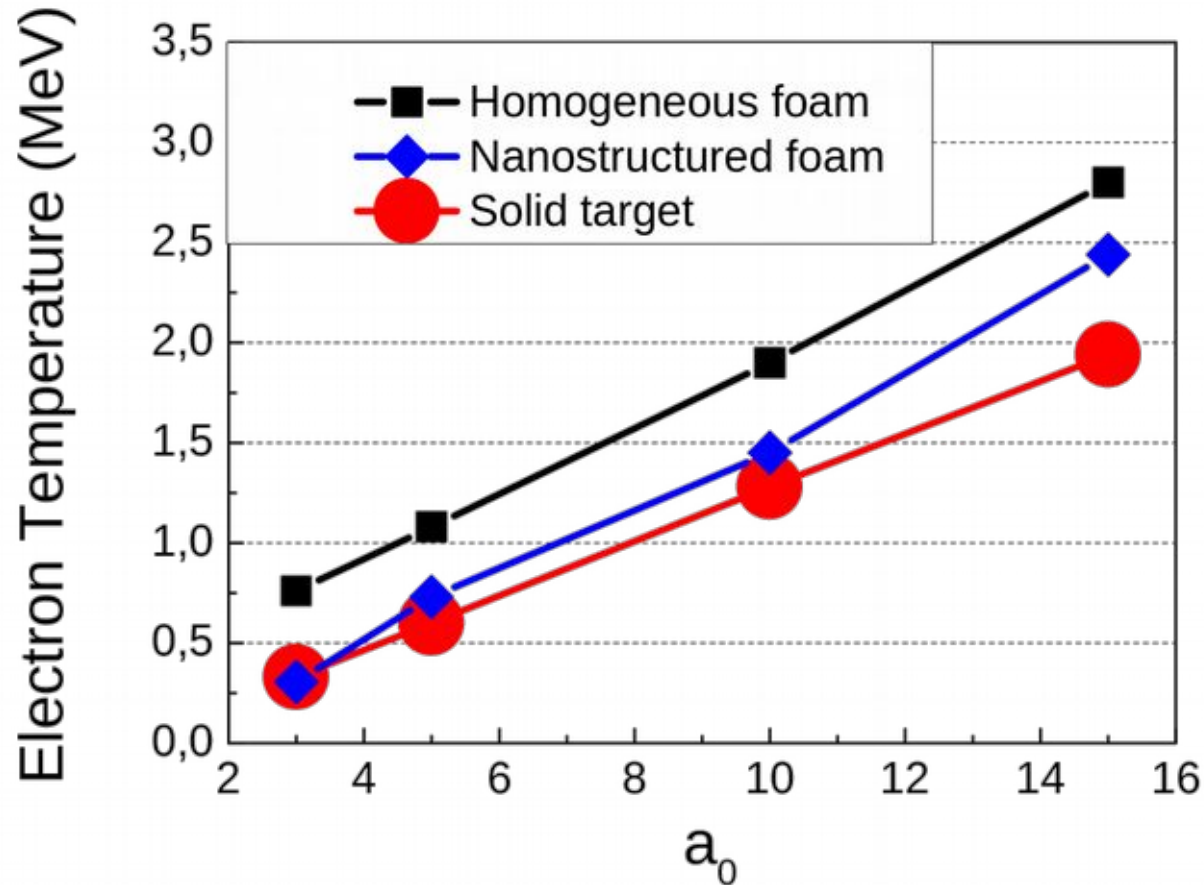
Rnd. Spheres $\langle n_e \rangle = n_c$
 $r = 10\text{nm}, n_e = 100 n_c$

L.Cialfi, L.Fedeli, M.Passoni, accepted with minor revisions, PRE



Electron-heating in near-critical plasmas

Simple linear fit: $T_e [MeV] = C_1 + C_2 a_0$

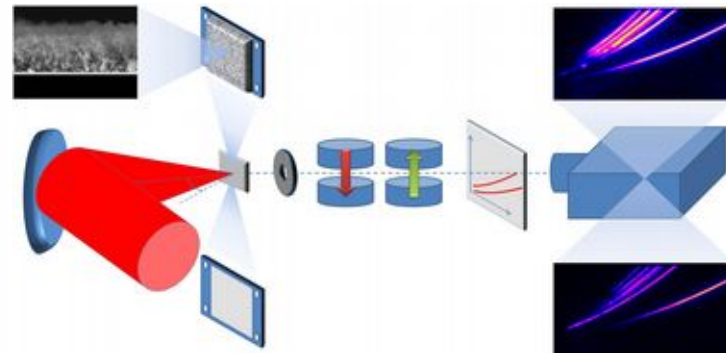
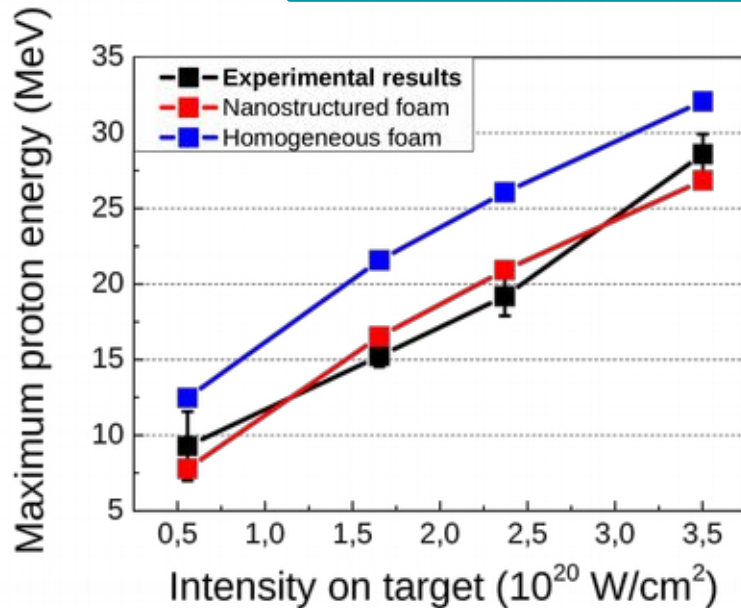
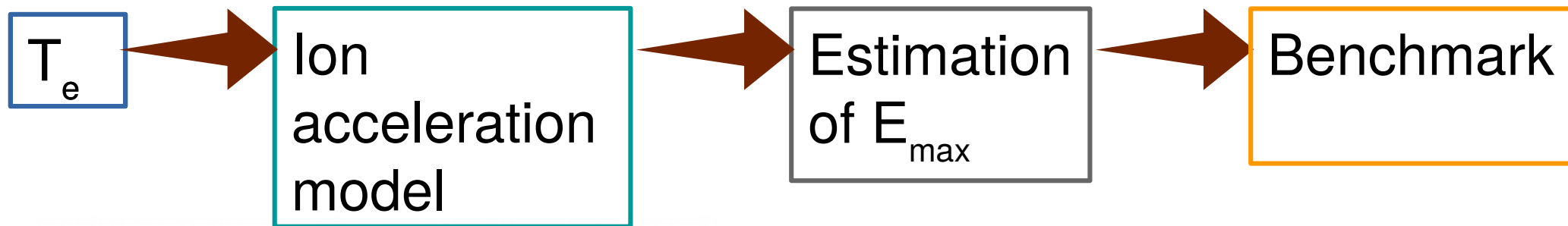


L.Cialfi, L.Fedeli, M.Passoni, accepted with minor revisions, PRE



Electron-heating in near-critical plasmas

Same idea of flat targets



L.Cialfi, L.Fedeli, M.Passoni, accepted with minor revisions, PRE



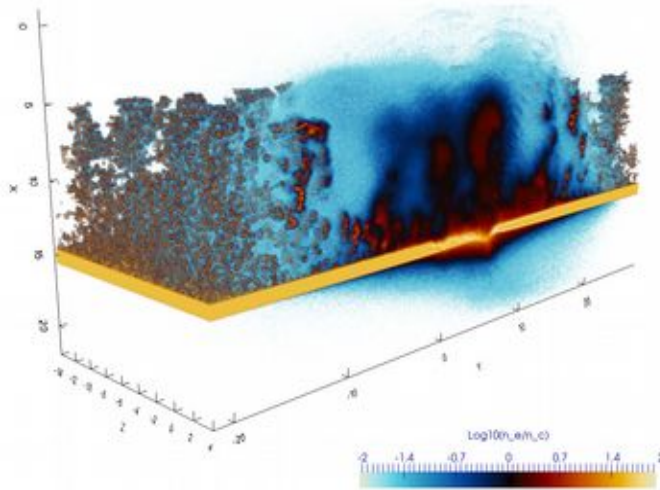
Nanostructured plasmas



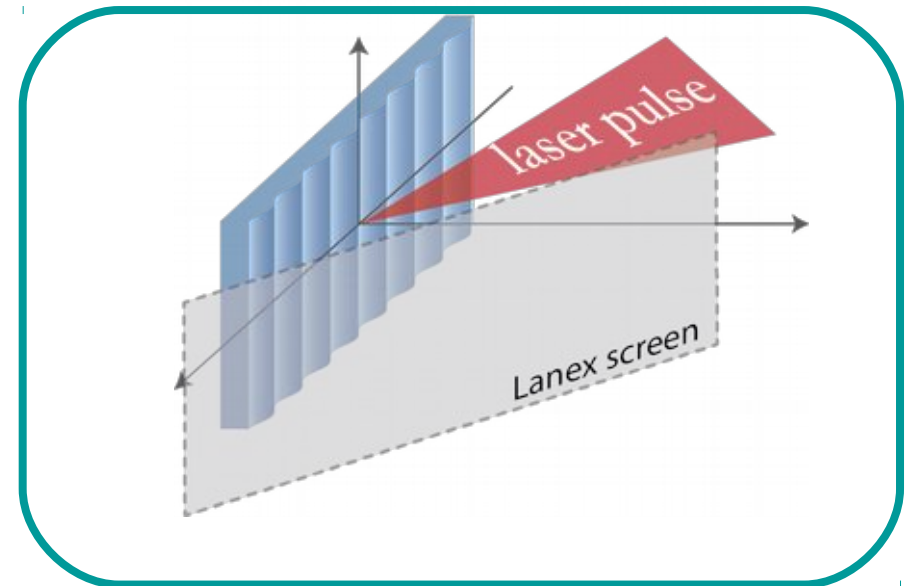
Nanostructured plasmas

If we irradiate a solid, nanostructured target with these lasers, **the structures might survive**

In some cases this is **incidental**



In other cases it is **desirable**



Nanostructured plasmas

Wide topic, growing interest in the community.

L.Fedeli et al. PRL 116 (2016)

T.Ceccotti et al. PRL 111 (2013)

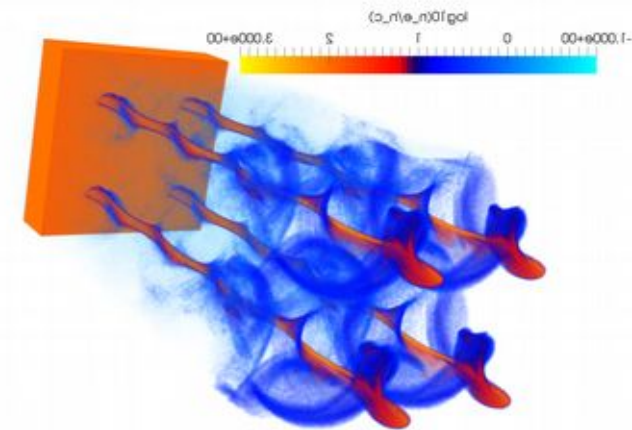
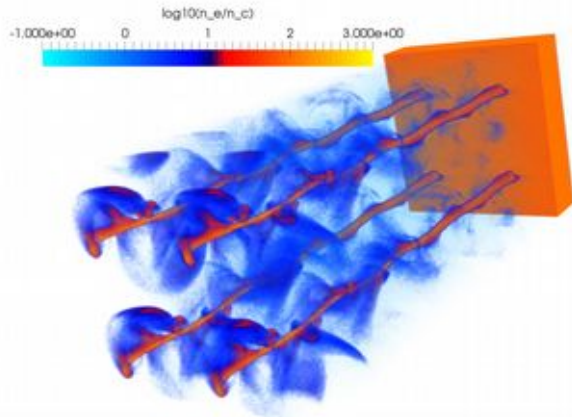
V.Kaymak et al. PRL 117 (2016)

S. Jiang et al. PRL 116 (2016)

K.Q.Pan et al. PoP 23 (2016)

M.A.Purvis et al. NatPhot 7 (2013)

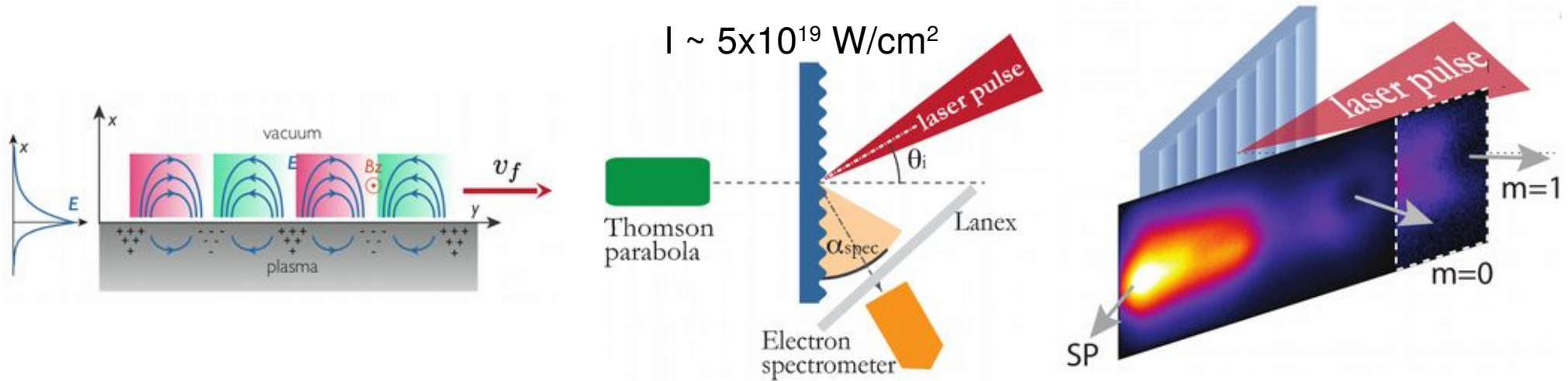
...



Nanostructured plasmas

High Field Plasmonics

Electron acceleration with a relativistic surface plasmon



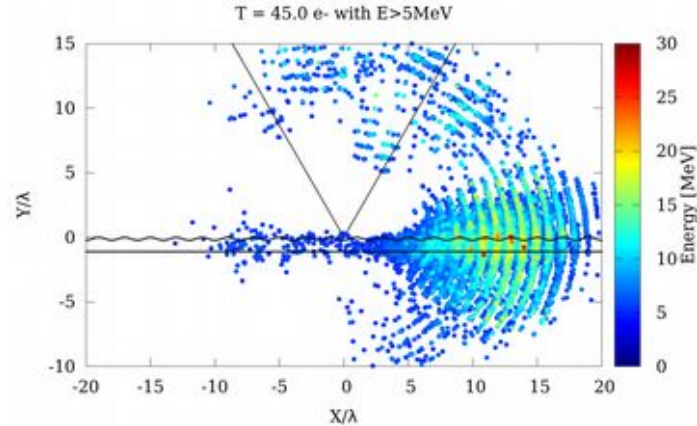
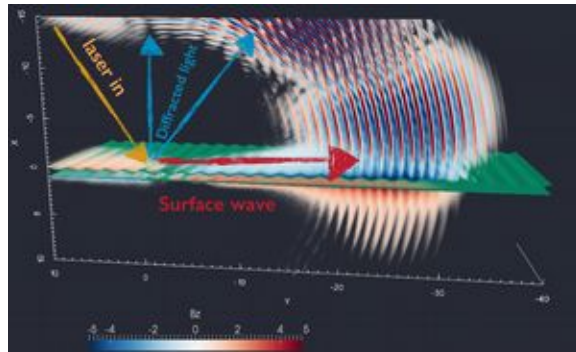
$$\frac{\omega}{c} \sin(\theta) = \frac{\omega}{c} \sqrt{\frac{1 - \omega_p^2 / \omega^2}{2 - \omega_p^2 / \omega^2}} \pm n \frac{2\pi}{d}$$

L.Fedeli et al. PRL 116 (2016)

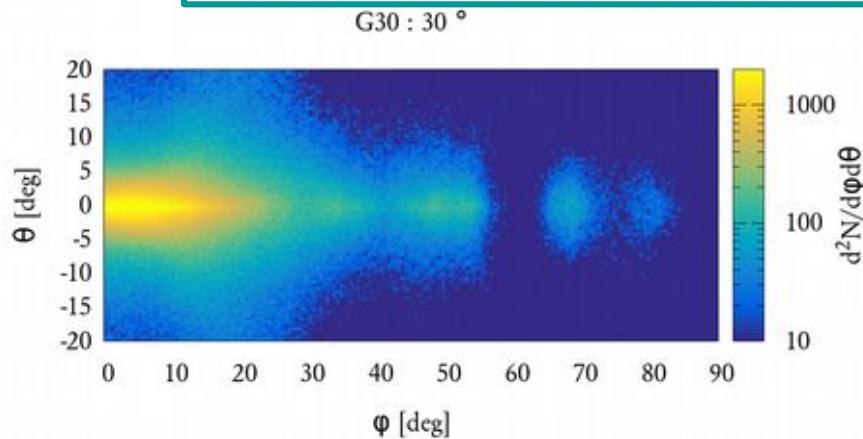


Nanostructured plasmas

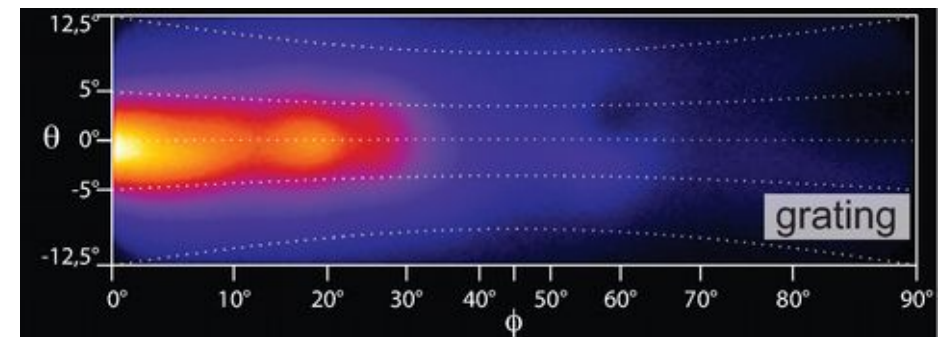
2D/3D PIC simulations confirmed the picture



And were able to reproduce exp.results



3D PIC Simulation



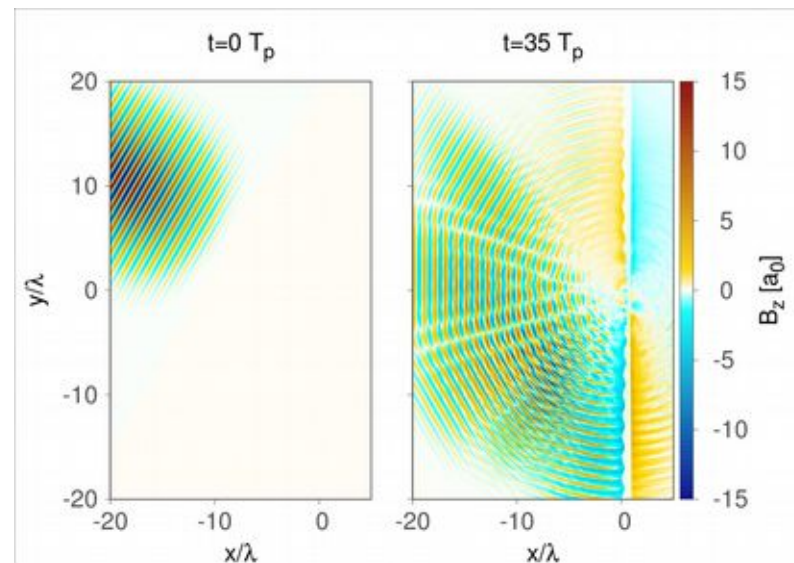
Exp. results



Other kinds of nanostructures plasmas

High Field Plasmonics

Enhanced high-order harmonic emission from irradiated grating targets



Dr A. Macchi

L. Fedeli et al. (to be submitted soon)

l'Observatoire de Paris Dr A. Sgattoni

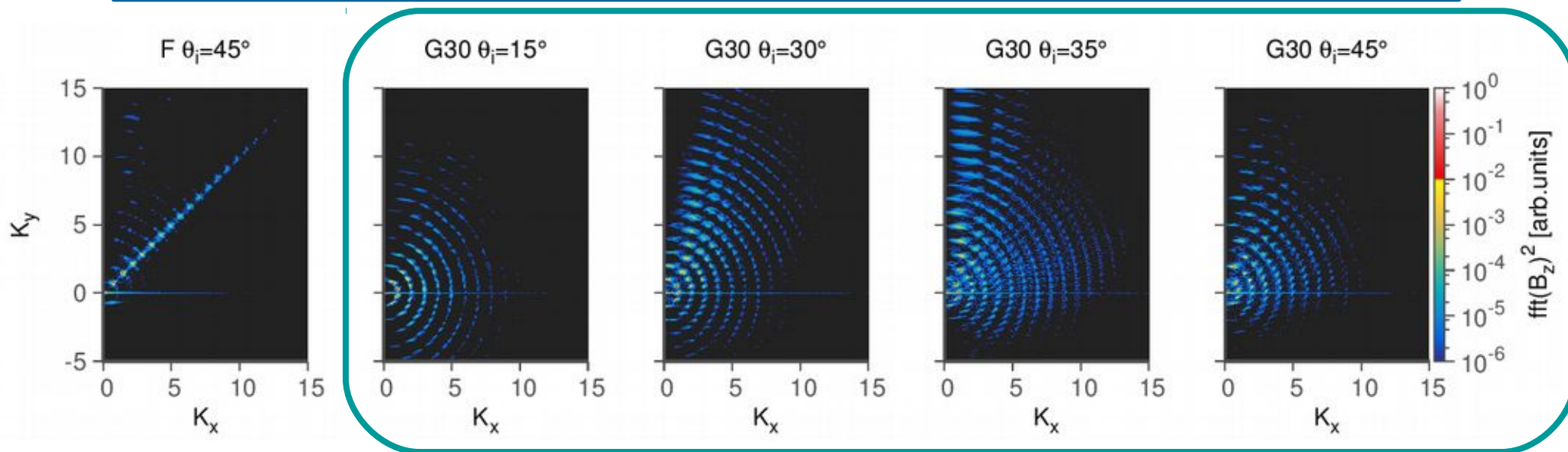


POLITECNICO MILANO 1863

Other kinds of nanostructures plasmas

High Field Plasmonics

Enhanced high-order harmonic emission from irradiated grating targets



Exp. Resonance @ 30°



Dr A.Macchi

L.Fedeli et al. (to be submitted soon)

l'Observatoire de Paris Dr A.Sgattoni



POLITECNICO MILANO 1863

Conclusions



Conclusions

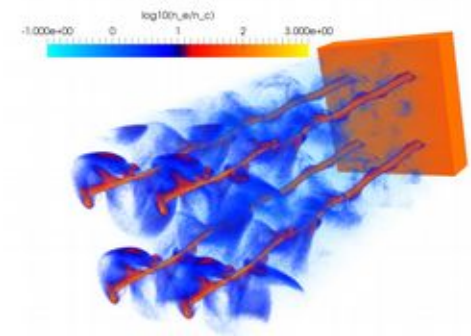
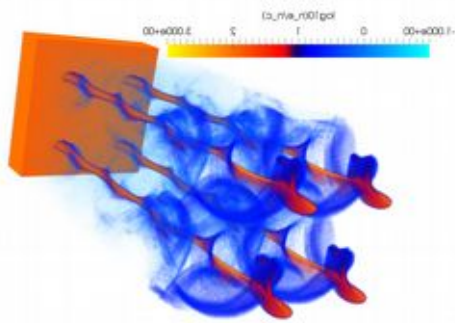
Ultra-intense, ultra-short, ultra-high contrast lasers allow to study **nanostructured plasmas**

Sometimes this is **desirable** (e.g. for gratings), sometimes it is **accidental** (e.g. for foams).

Nanostructure can strongly affect laser-plasma interaction and we **need simulations** to support and guide experimental activities

Since only recently ultra-short, ultra-high contrast lasers have become available, there are **many possible scenarios to study**.





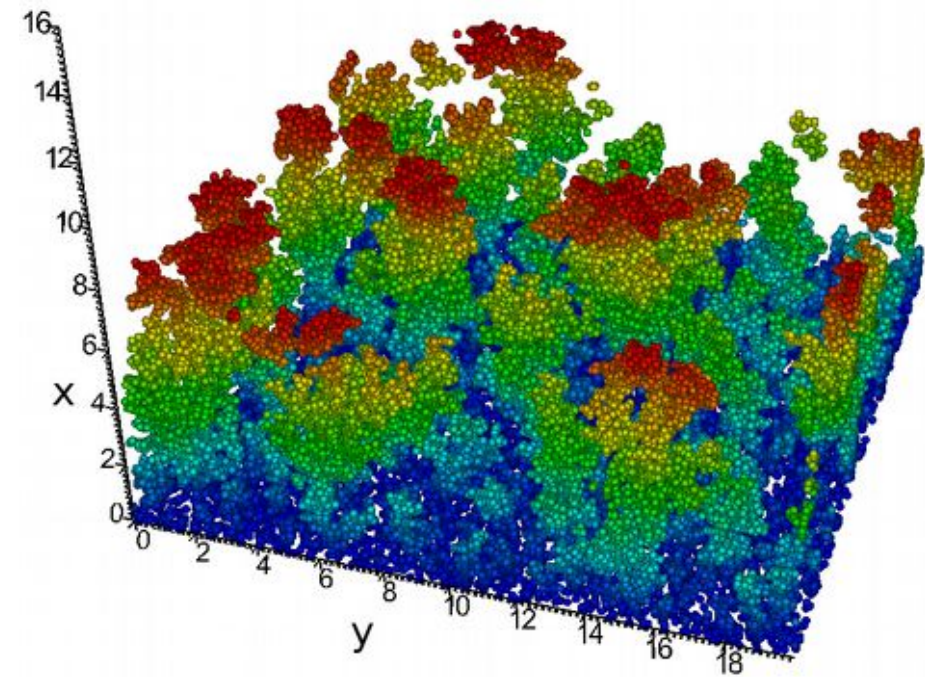
Thank you for your attention!



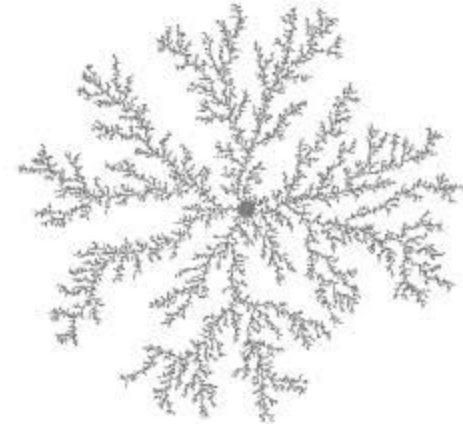


Diffusion-limited aggregation

How do we “build these structures”?



A very simple model



Which accurately describes many natural structures



T.A. Witten & L.M. Sanders PRL 47 (1981)

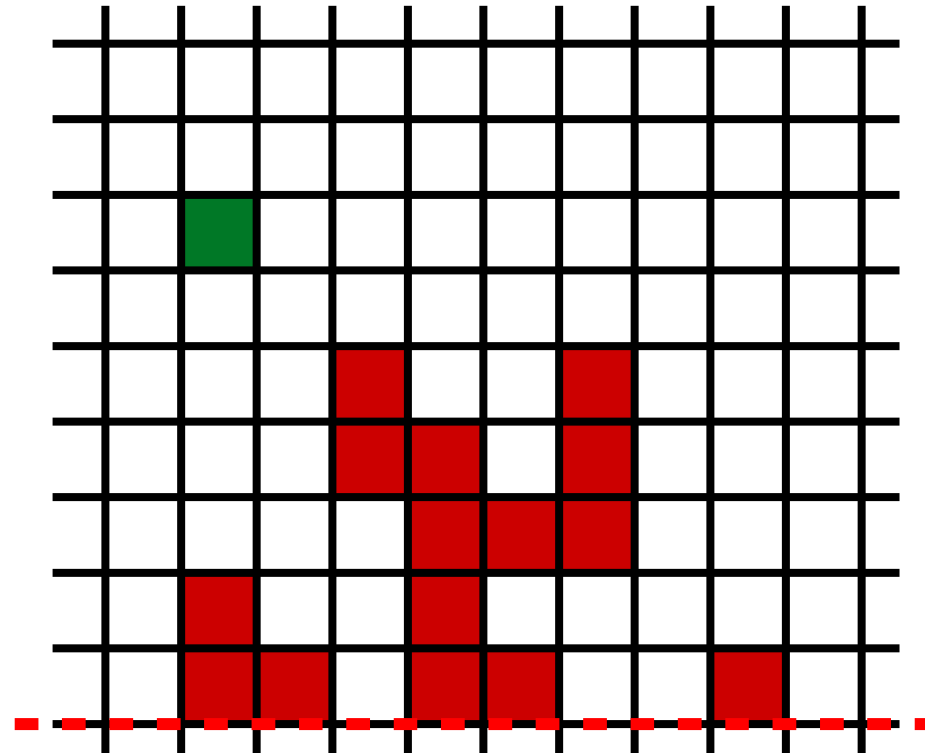


Diffusion-limited aggregation

 Moving particle

 Fixed particle

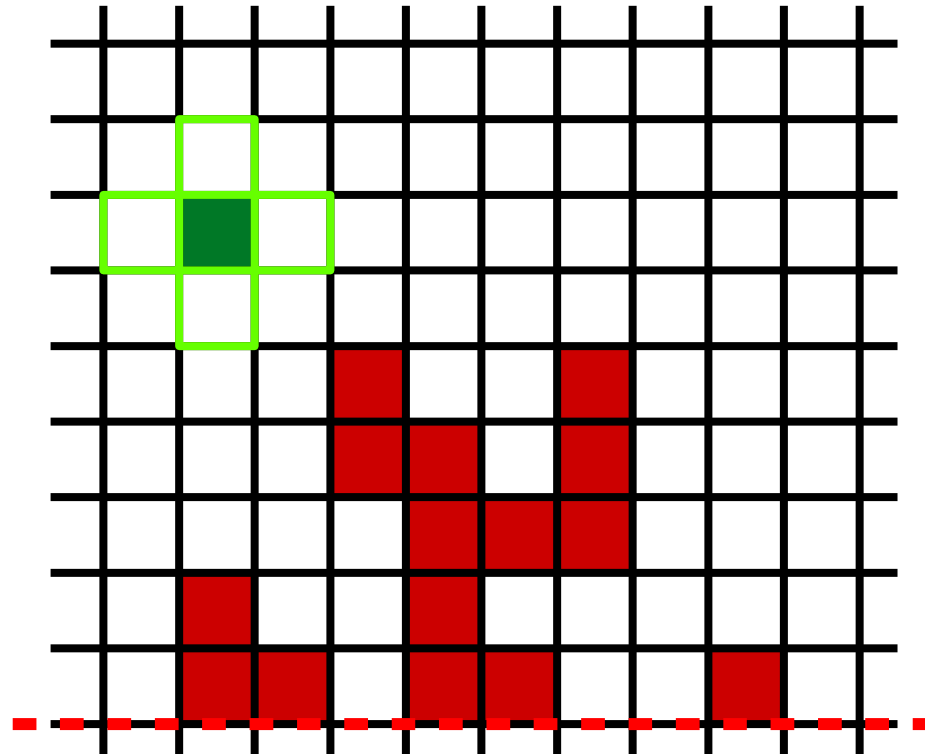
Substrate



Diffusion-limited aggregation

 Moving particle

 Fixed particle



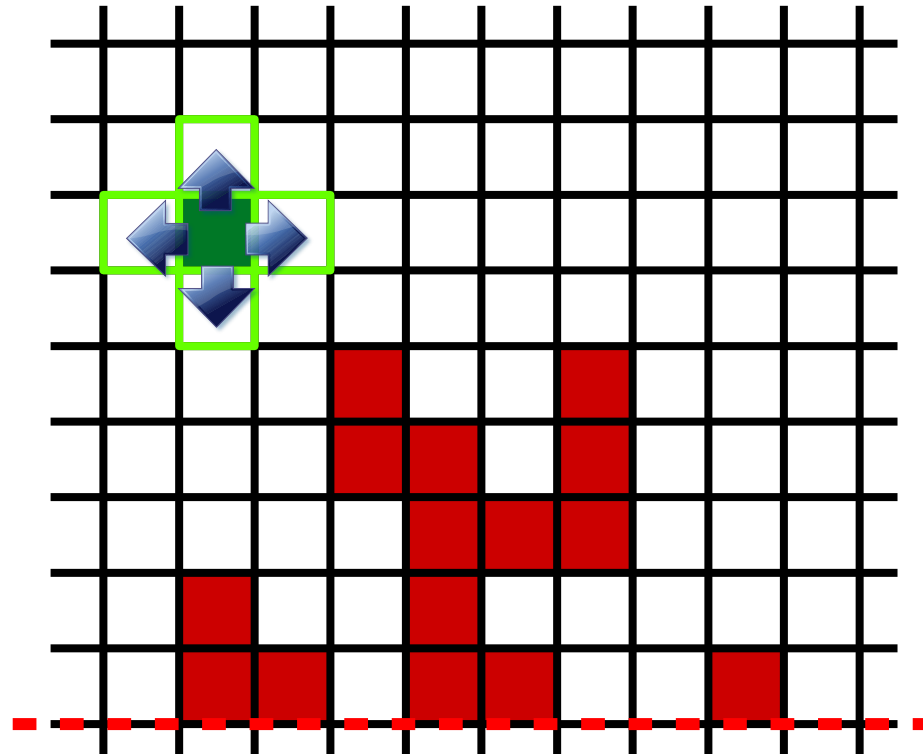
Check if surrounding
cells are free



Diffusion-limited aggregation

 Moving particle

 Fixed particle



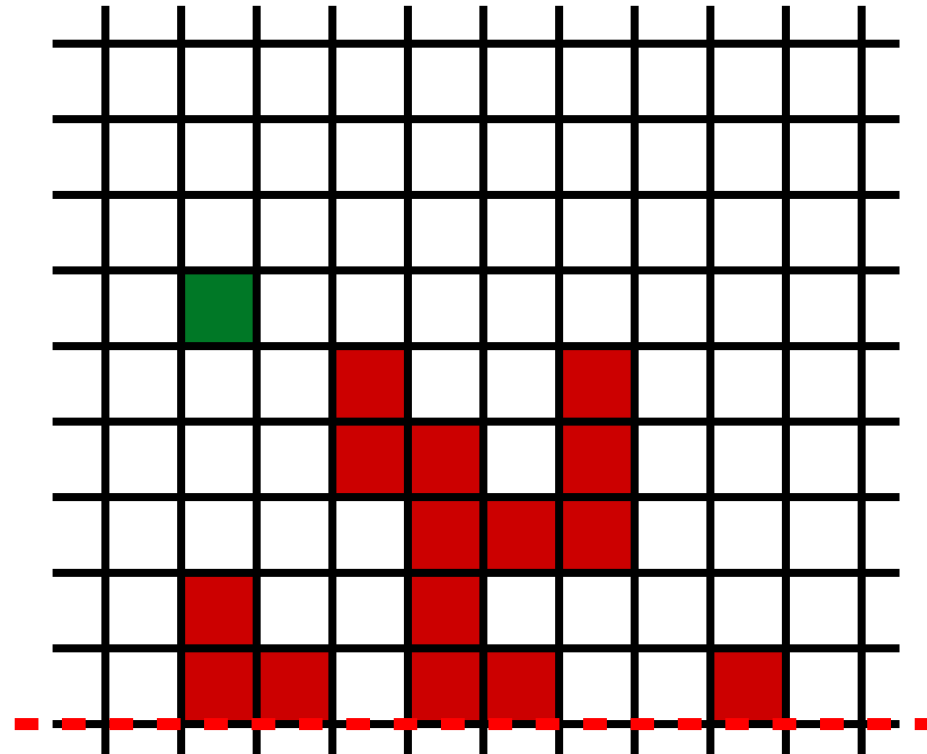
Random movement
on the grid



Diffusion-limited aggregation

 Moving particle

 Fixed particle



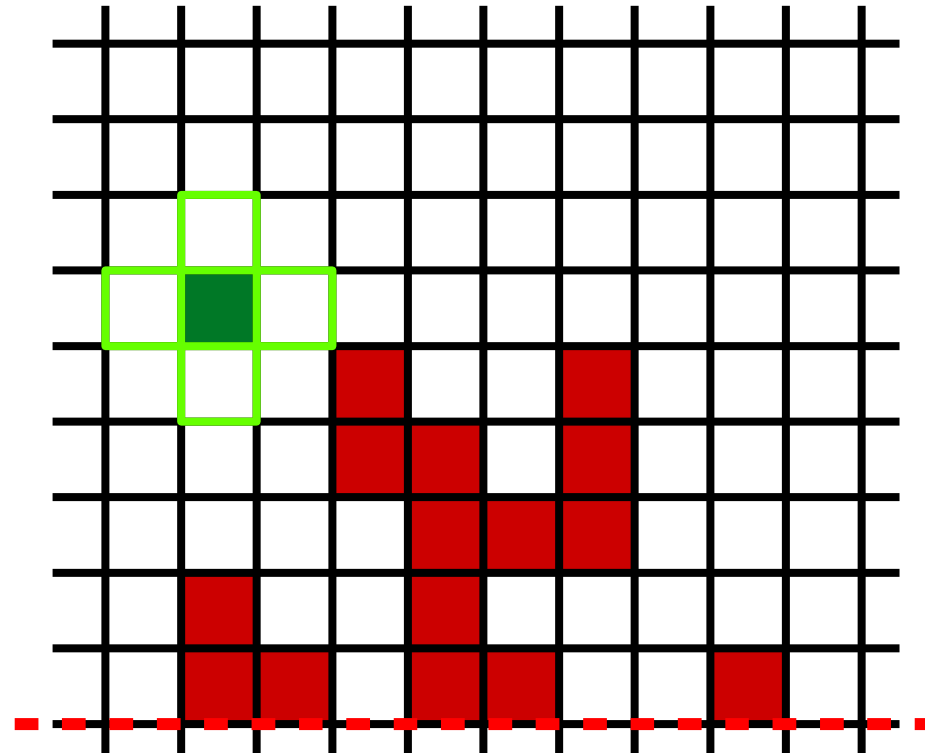
The particle moves



Diffusion-limited aggregation

 Moving particle

 Fixed particle



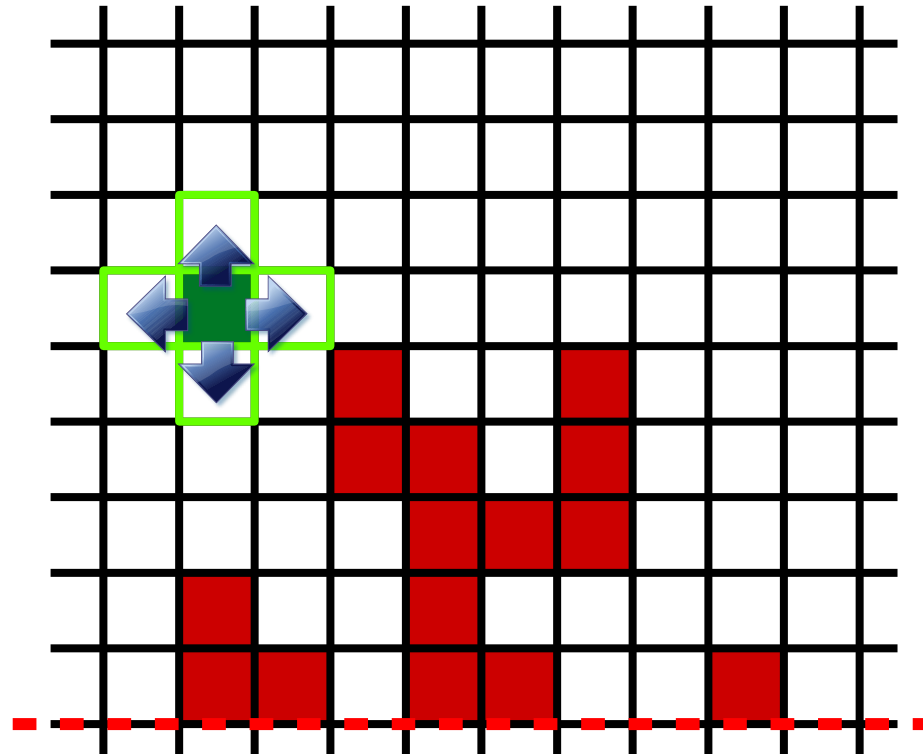
Check if surrounding
cells are free



Diffusion-limited aggregation

 Moving particle

 Fixed particle



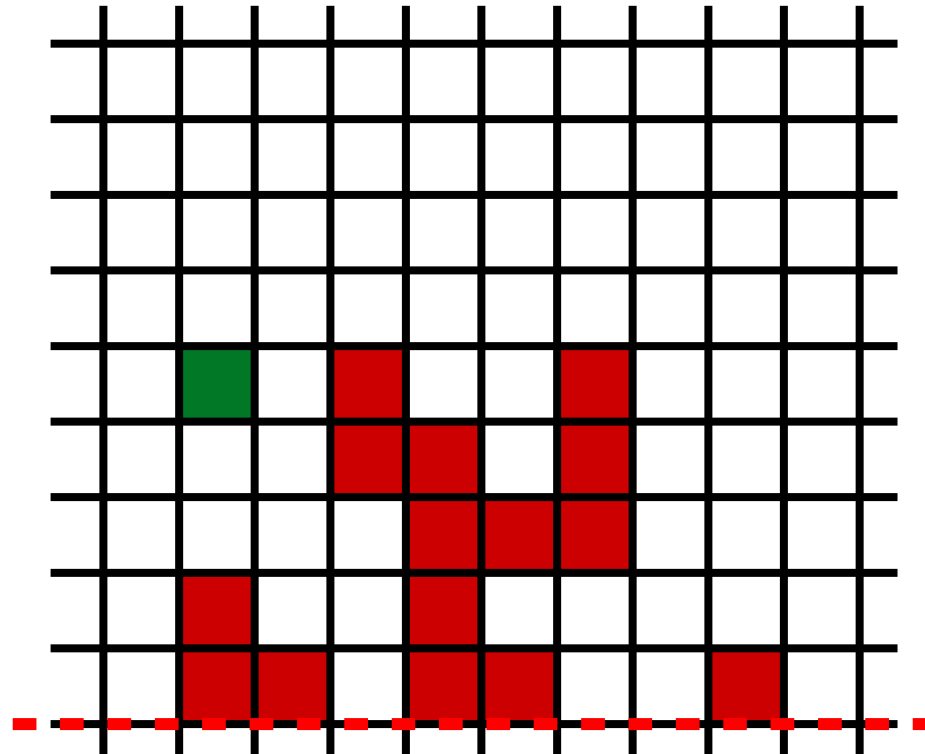
Random movement
on the grid



Diffusion-limited aggregation

 Moving particle

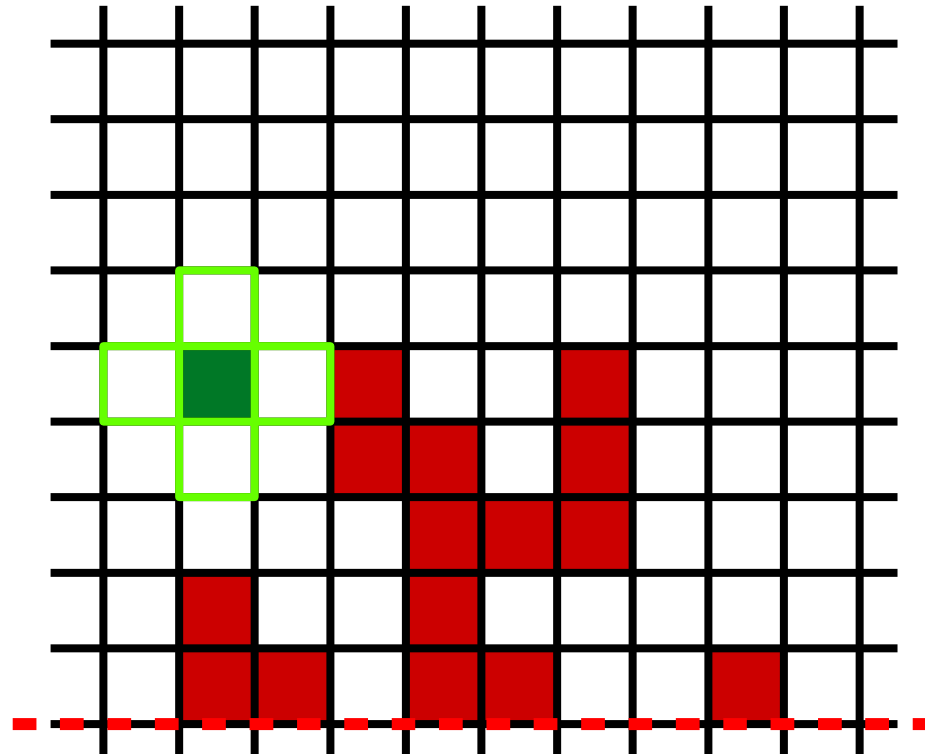
 Fixed particle



Diffusion-limited aggregation

 Moving particle

 Fixed particle



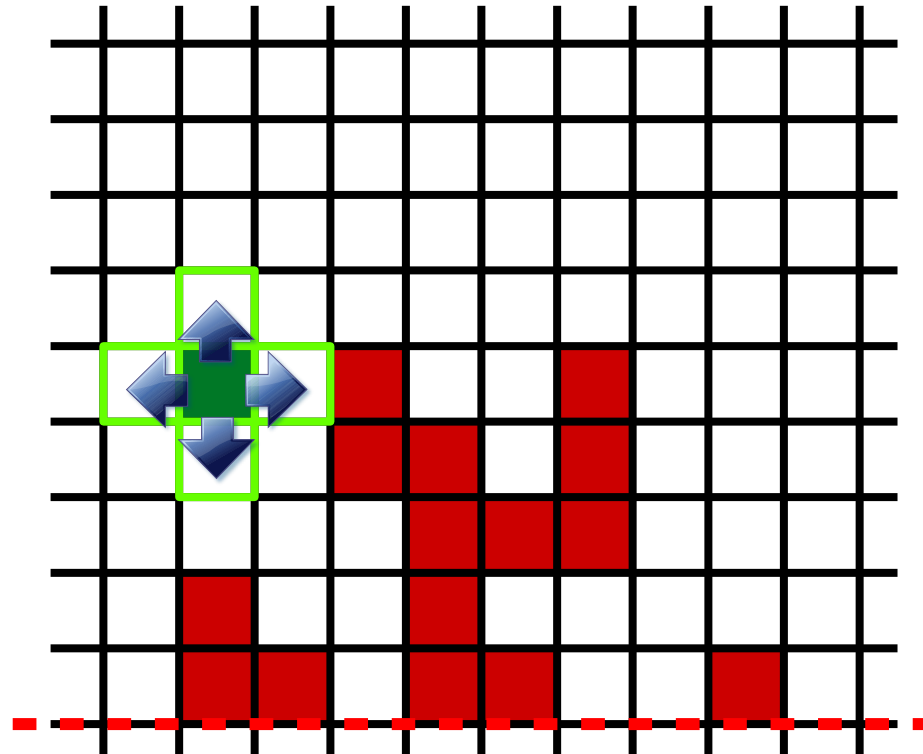
Check if surrounding
cells are free



Diffusion-limited aggregation

 Moving particle

 Fixed particle



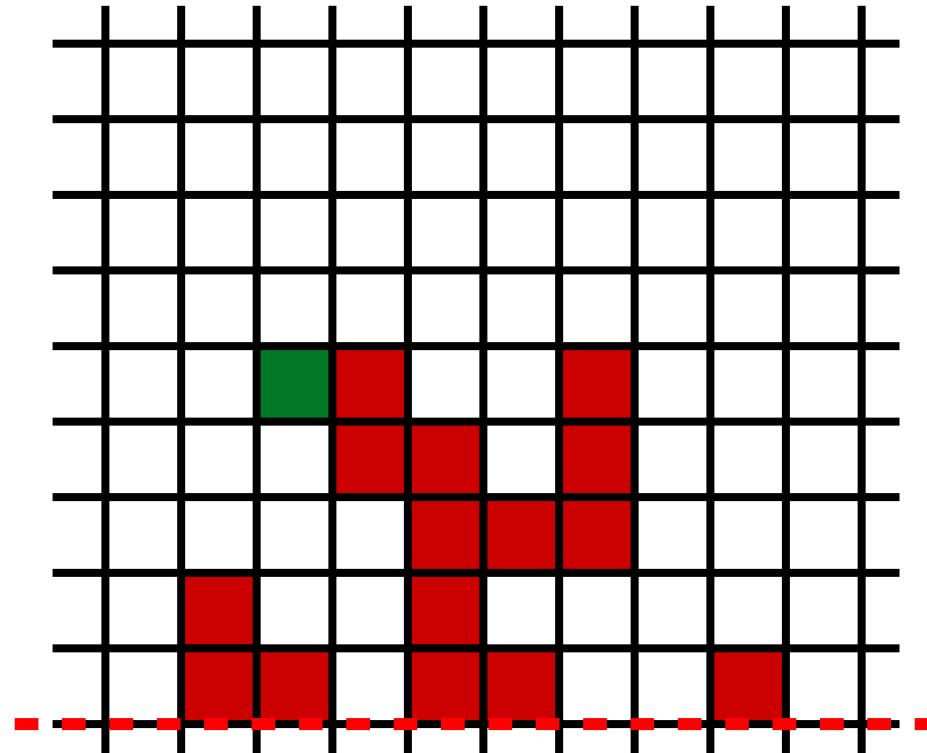
Random movement
on the grid



Diffusion-limited aggregation

 Moving particle

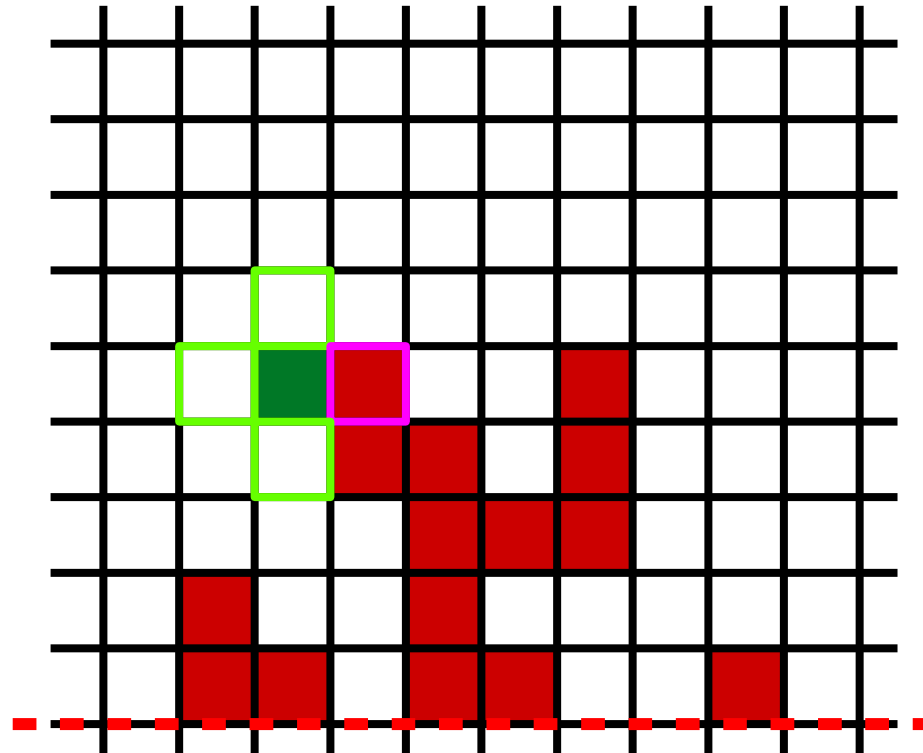
 Fixed particle



Diffusion-limited aggregation

 Moving particle

 Fixed particle



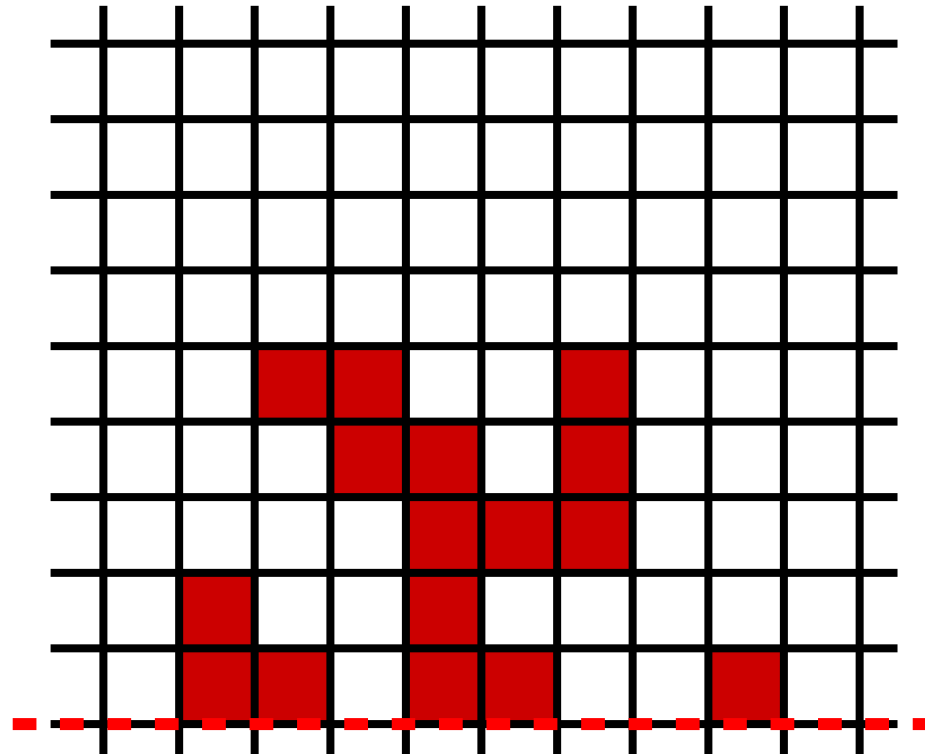
The particle touches a filled cell. It stops there



Diffusion-limited aggregation

 Moving particle

 Fixed particle



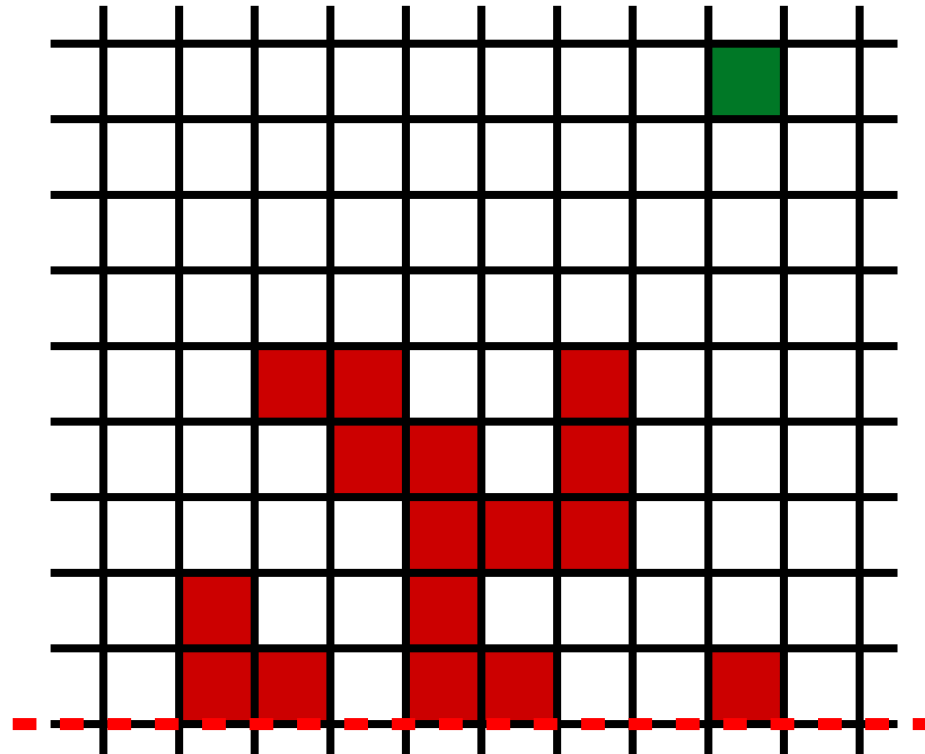
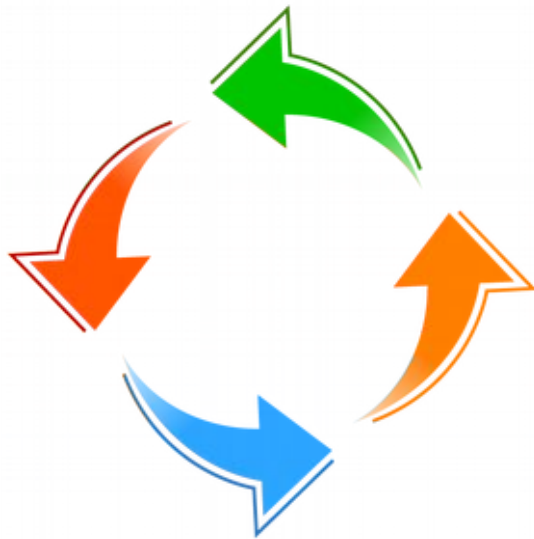
The particle touches a filled cell. It stops there



Diffusion-limited aggregation

 Moving particle

 Fixed particle



A new particle starts from the edge of the grid

